



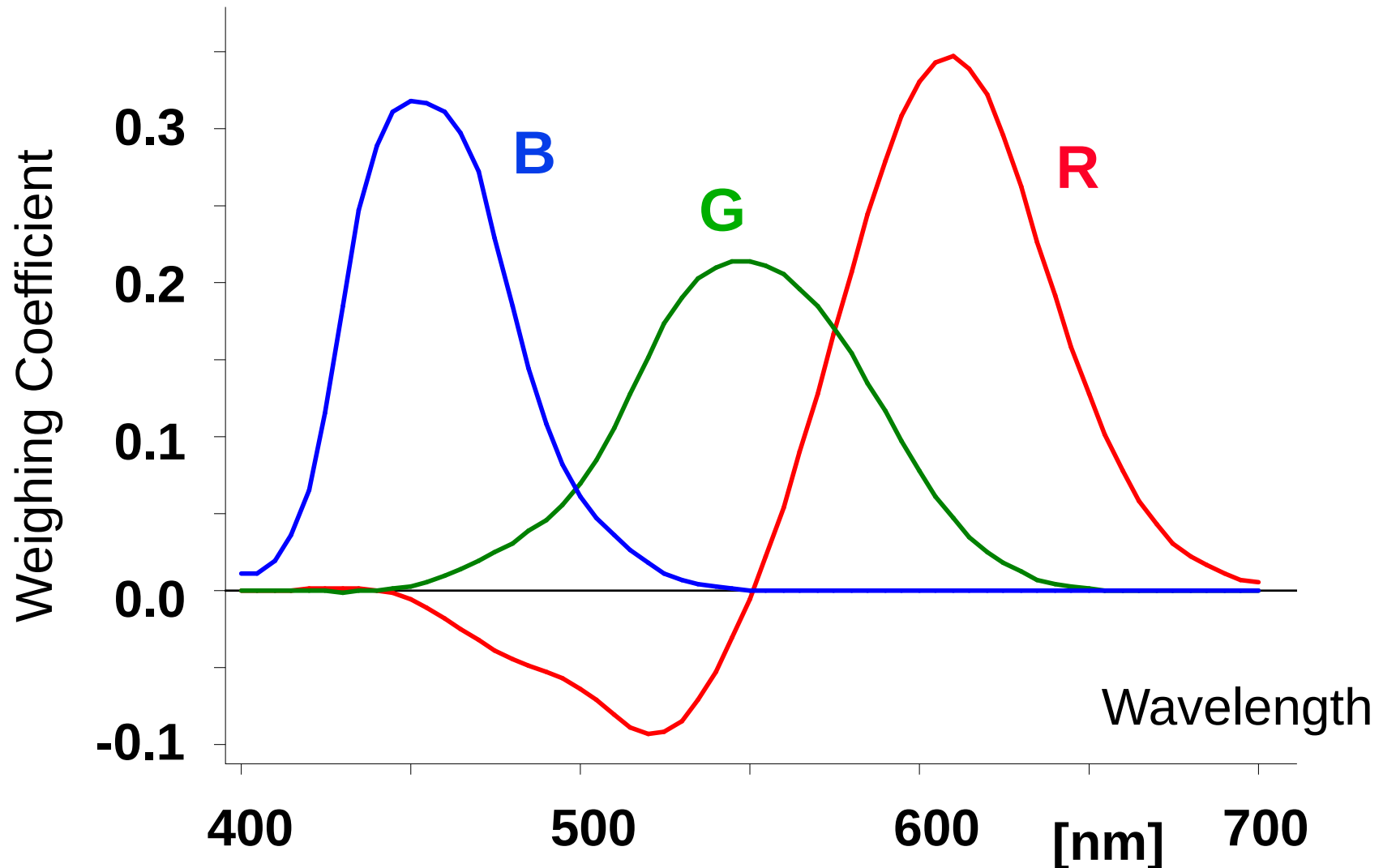
# Colour Spaces

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# Conversion of Spectral Data

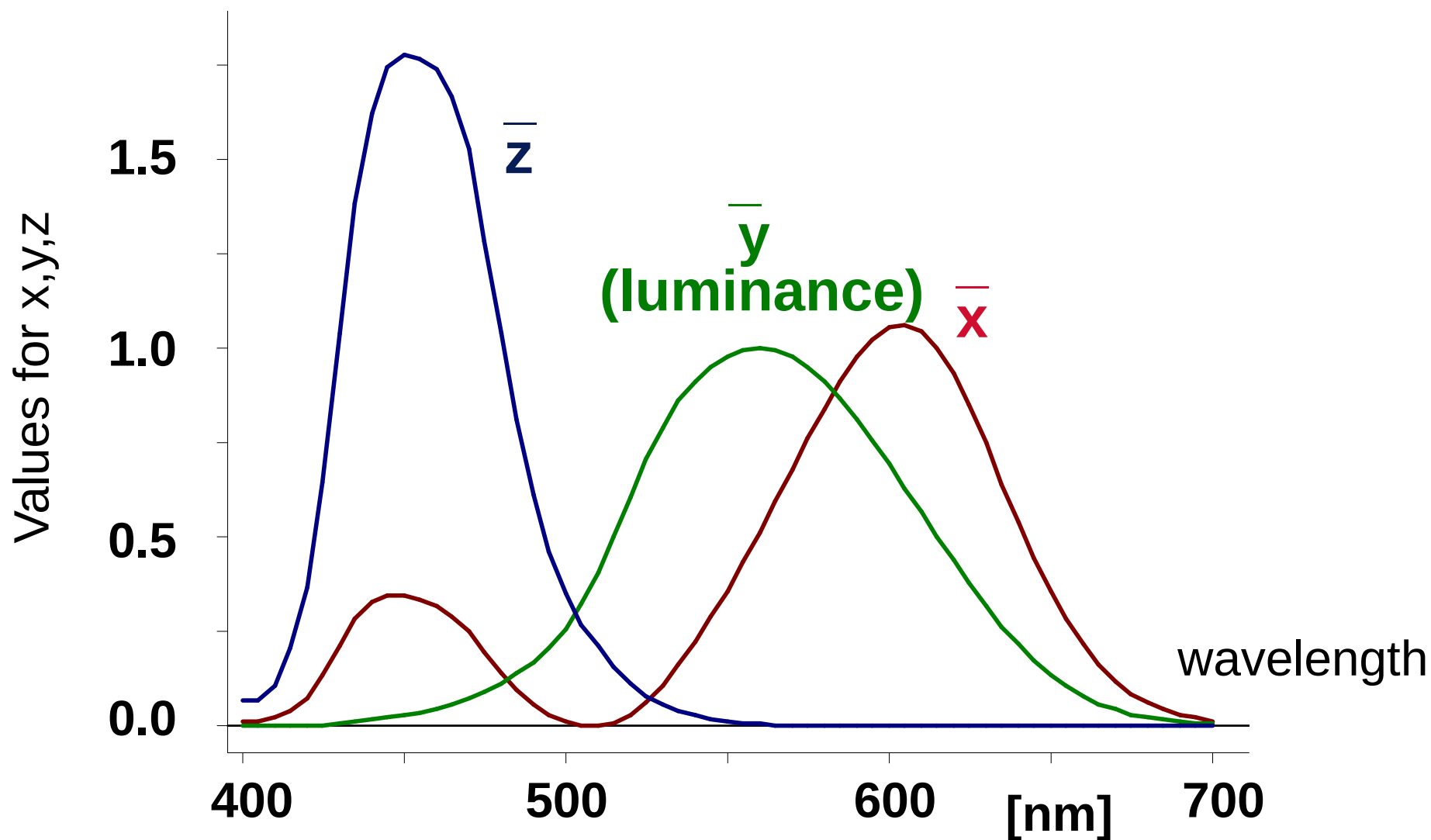


# Virtual Primary Colours X,Y,Z

- ♦ The *Commission Internationale de l'Éclairage (CIE)* in 1931 defined three virtual primaries **X, Y, Z**, the **convex combination** of which can describe all visible colours
  - X, Y, Z are defined via their spectral response curves **x, y, z** (tabulated in 1nm intervals)
- ♦ The relationship between R,G,B and X,Y,Z spaces is **linear**
  - Unambiguously defined by  $3 \times 3$  matrices



# CIE XYZ Response Curves



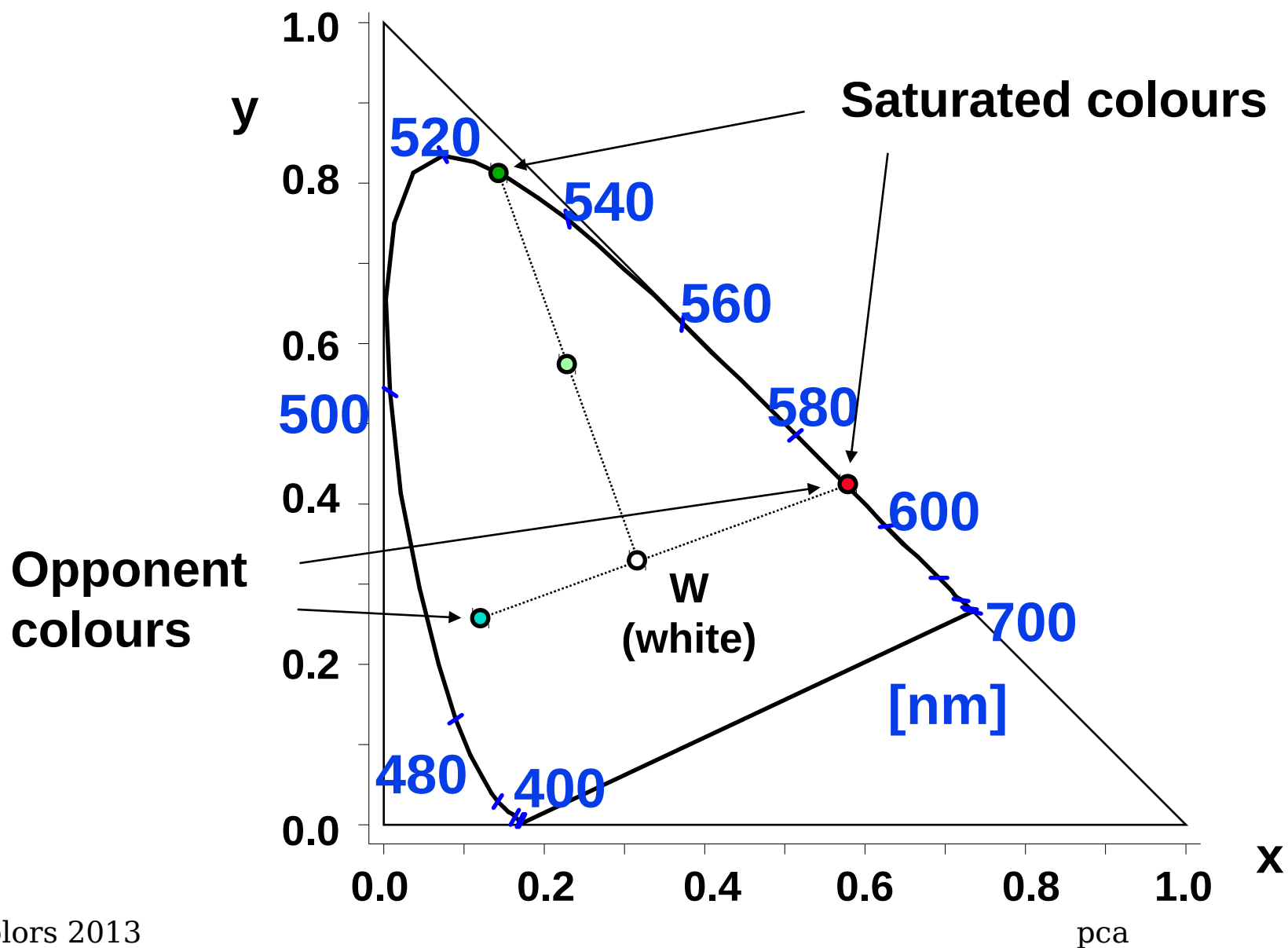


# CIE $x, y$ Colour Space

- **Normalised colour coordinates  $x, y, z$ :**
  - $x = X/(X+Y+Z)$ ,  $y = Y/(X+Y+Z)$ ,  $z = Z/(X+Y+Z)$
  - $x, y, z$  only carry information about hue and saturation, luminance is omitted
- The **CIE  $x, y$**  diagram does not use the  $z$  coordinate
  - Not independent of the others ( $z = 1 - x - y$ )
- The system is not **perceptually uniform** (like e.g. the uniform **CIE  $u, v$**  system)



# CIE x,y Chroma Diagram





# RGB Primaries

- Corresponds to **three types of phosphors**:

$$\mathbf{R} = [ 0.628, 0.346 ]$$

$$\mathbf{G} = [ 0.268, 0.588 ]$$

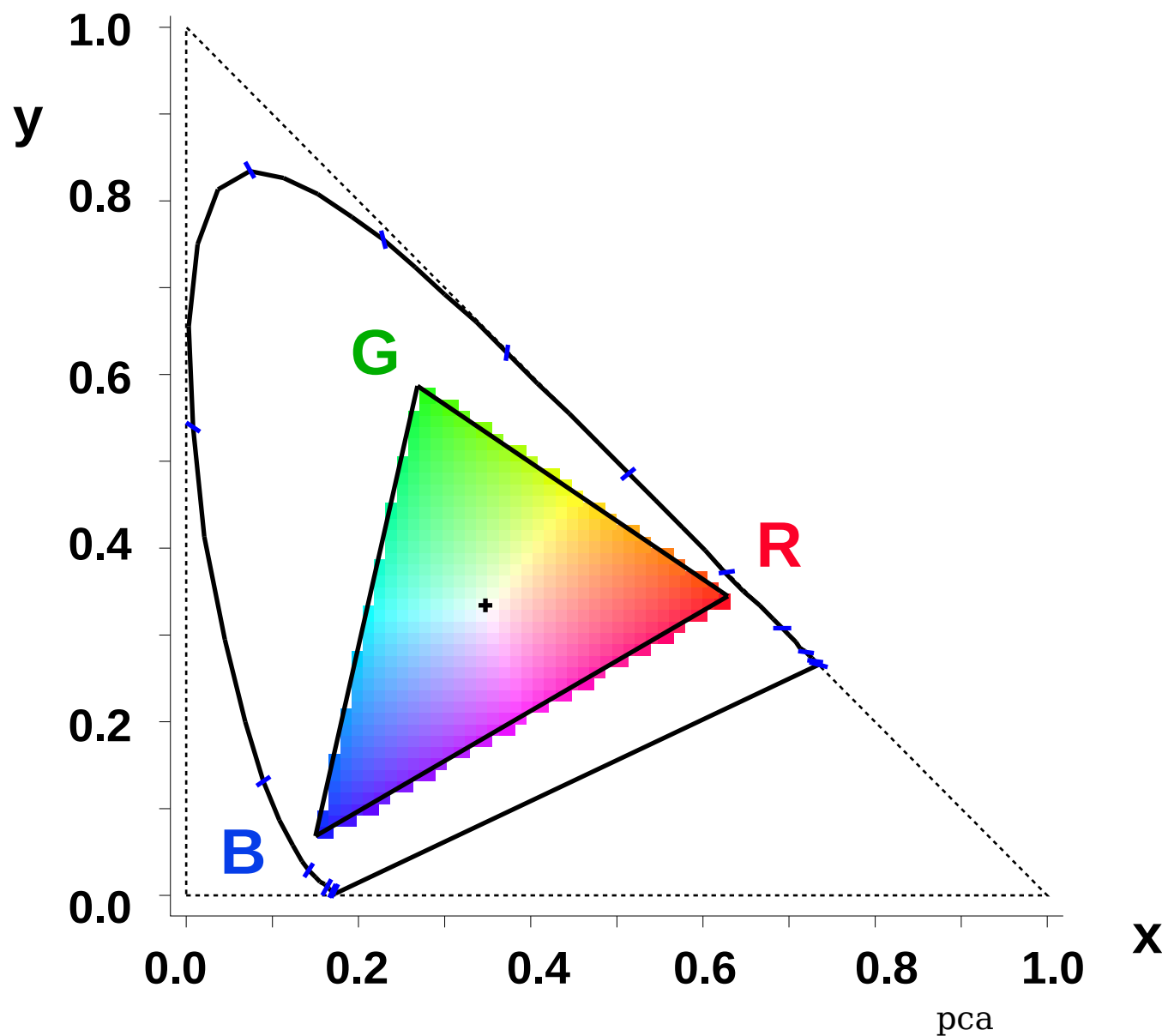
$$\mathbf{B} = [ 0.150, 0.070 ]$$

– white  $\mathbf{W}(D_{6500}) = [ 0.313, 0.329 ]$

- Equal energy white  $\mathbf{W}$  has the coordinates [ **1/3, 1/3** ]
- White  $\mathbf{R}$  for the **NTSC** TV norm: [ **0.31, 0.316** ]

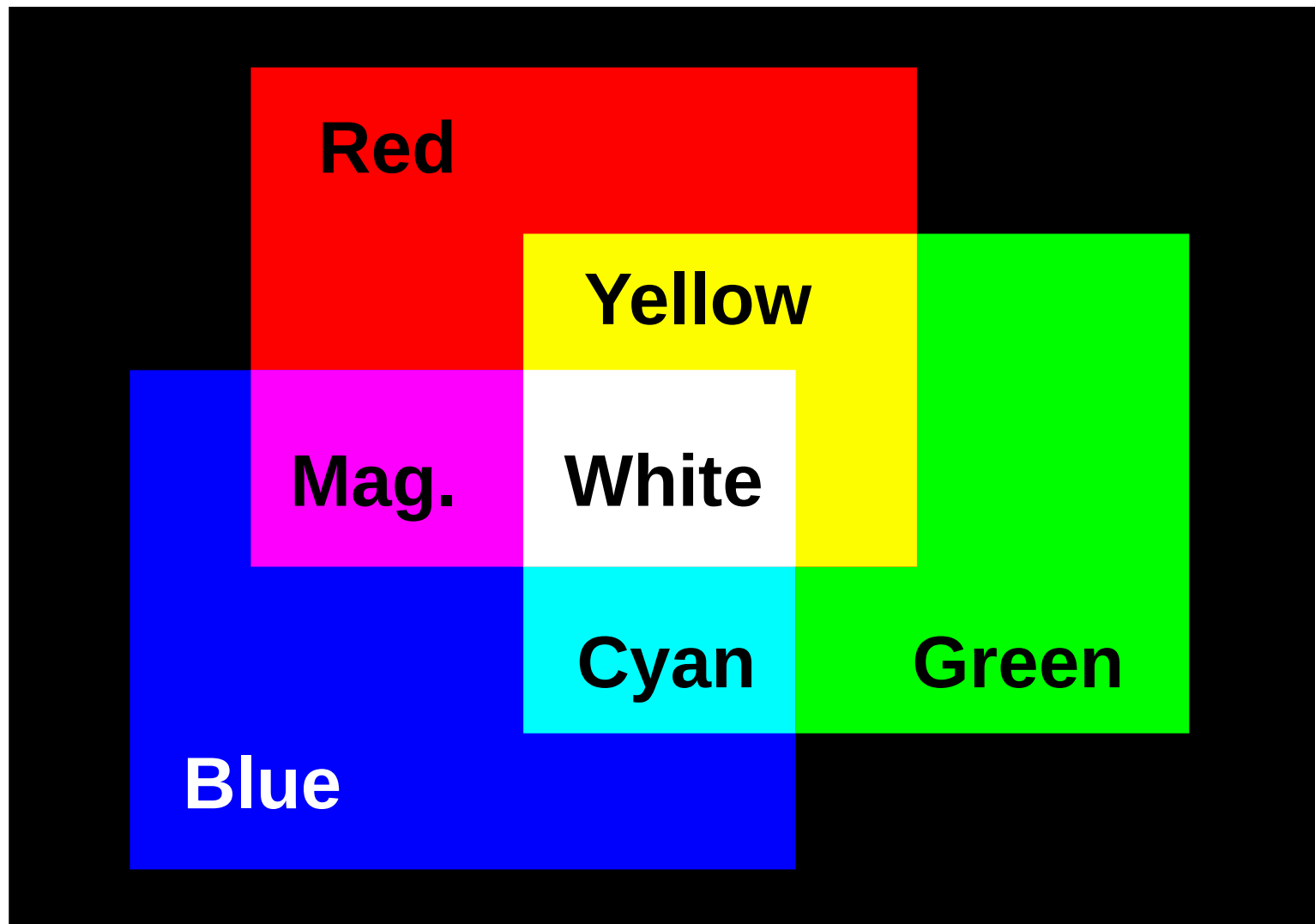


# Monitor Gamut in CIE x,y





# Additive Colour Mixing (RGB)

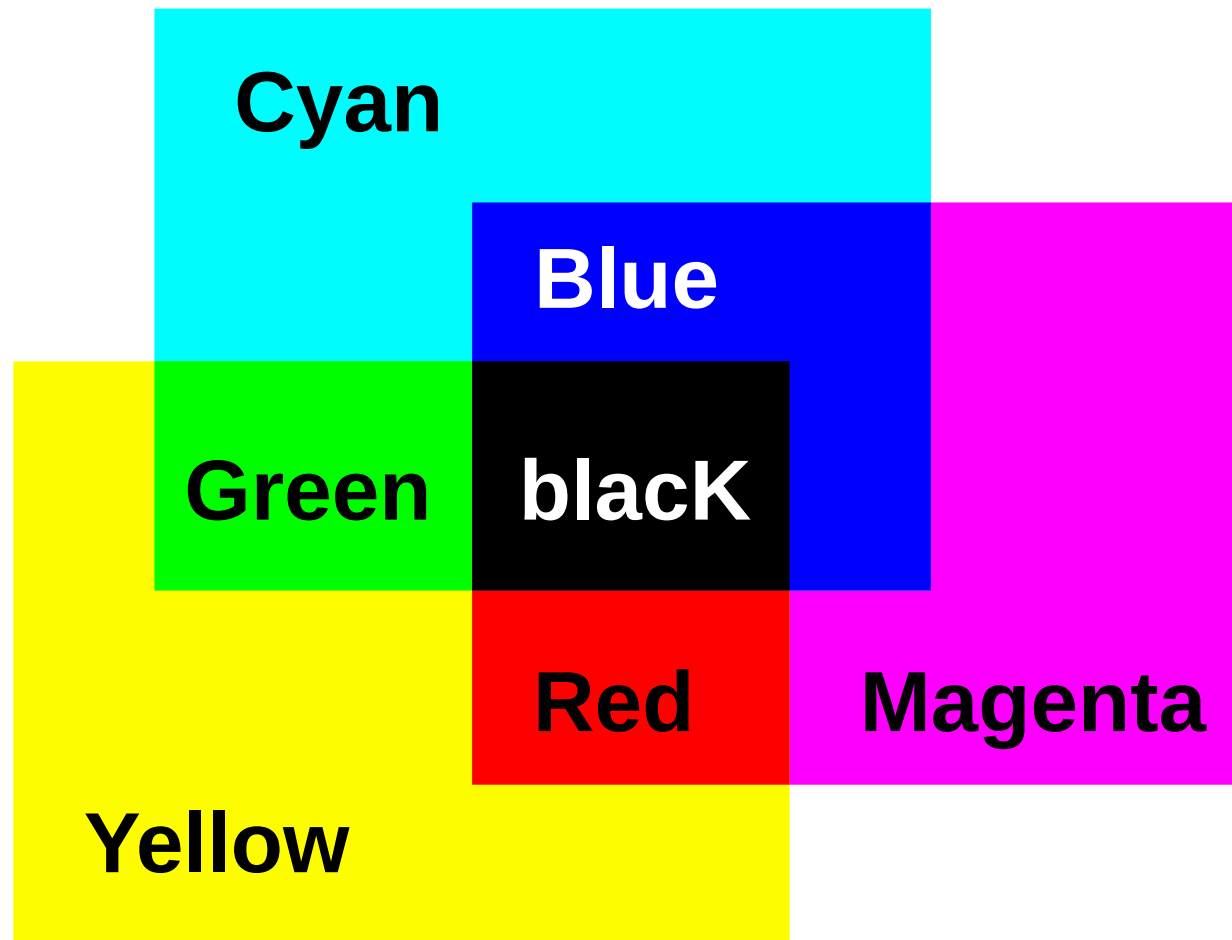




# The CMY(K) Colour System

- Used in **2D/3D print** (and chemical photography)
  - Everywhere, where controlled absorption of light is used to determine object appearance
- Colours are mixed **subtractively**
- Basic colours are **C** (cyan), **M** (magenta), **Y** (yellow)  
These match the classical print primaries
  - **C, M, Y** are counterparts to **R, G, B**

# Subtractive Colour Mixing (CMY)





# The CMY(K) Colour System

◆ Conversion between **CMY** and **RGB**:

$$- \mathbf{C} = \mathbf{1} - \mathbf{R}, \mathbf{M} = \mathbf{1} - \mathbf{G}, \mathbf{Y} = \mathbf{1} - \mathbf{B}$$

◆ In addition to **C**, **M**, **Y** there is also frequently a **black component K**:

– Composite black is not as deeply black as genuine K

– Black ink is cheaper than the coloured ones

$$\mathbf{K}' \approx \min(\mathbf{C}, \mathbf{M}, \mathbf{Y}), \mathbf{C}' \approx \mathbf{C} - \mathbf{K}, \mathbf{M}' \approx \mathbf{M} - \mathbf{K}, \mathbf{Y}' \approx \mathbf{Y} - \mathbf{K}$$



# The YIQ Colour System

- ◆ Used for **TV broadcasts and signals**
  - Defined by the **NTSC** in 1953
  - Compatible with black and white TV sets

$$\begin{bmatrix} Y \\ I \\ Q \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ 0.596 & -0.275 & -0.321 \\ 0.212 & -0.528 & 0.311 \end{bmatrix} \cdot \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

- ◆ The **(I,Q)** signals are perceptually less important
  - Consequence: these signals are allocated less bandwidth



# The HSV Colour System

## ■ User-oriented

- Intuitive parameters: „hue”, „saturation”, and „value”

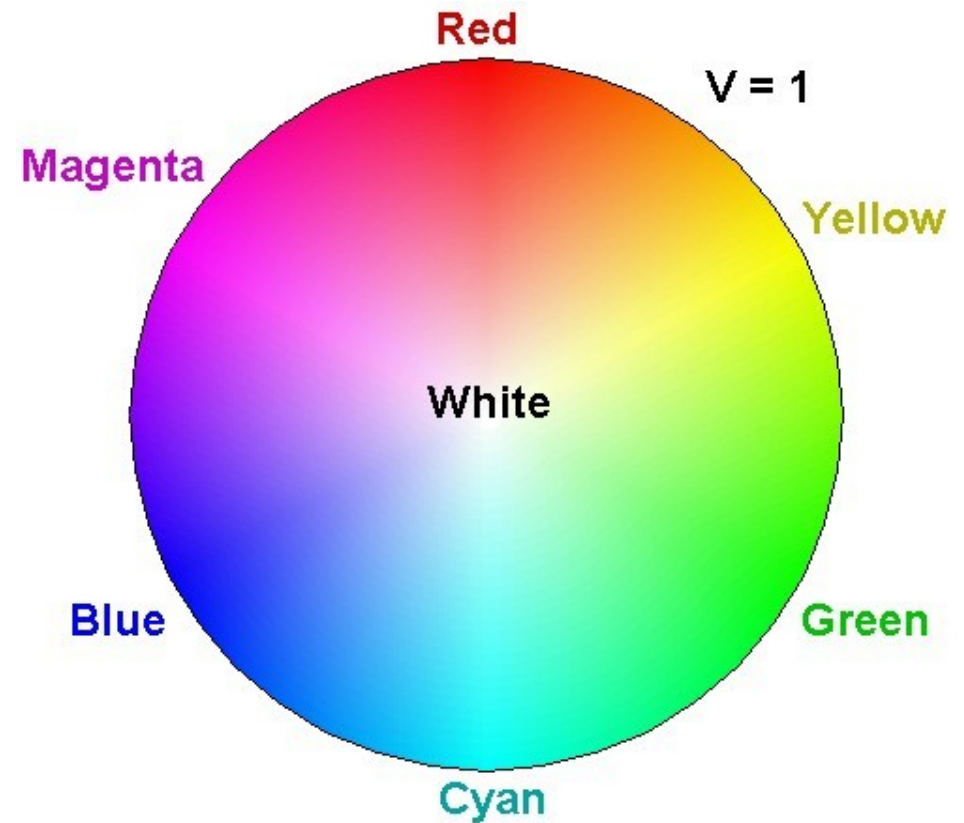
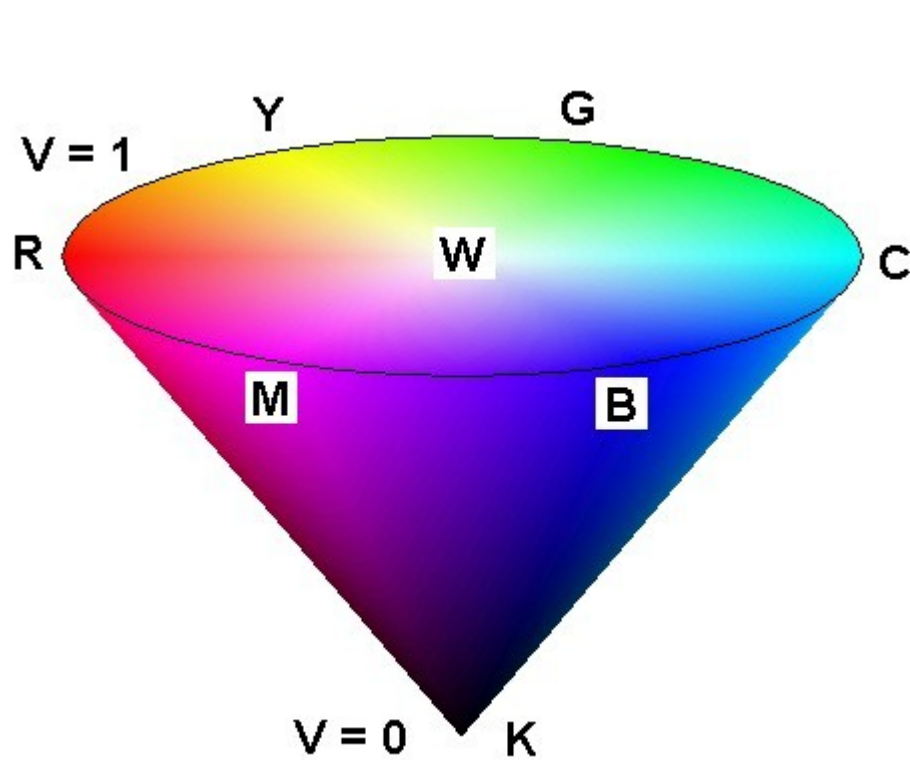
## ■ Description of the components:

- **H**: main hue, range **0°** to **360°**

- **S**: saturation, range from **0** (white) to **1** (spectral colour)

- **V**: luminance, range **0** (black) to **1**

# Colour Circle





# Translation RGB → HSV

```
procedure RGB2HSV ( R,G,B : real; var H,S,V : real );  
var min, max, delta : real;  
begin  
  min := minimum(R,G,B); max := maximum(R,G,B);  
  V := max; delta := max - min;  
  if max <> 0.0 then S := delta/max  
    else S := 0.0;  
  if delta <> 0.0 then  
    begin                                     { chromatic case }  
      if R = max then H := (G - B)/delta else  
      if G = max then H := 2 + (B - R)/delta  
        else H := 4 + (R - G)/delta;  
      H := H * 60.0;                            { conversion to degrees }  
      if H < 0.0 then H := H + 360.0;  
    end;  
  end;
```





# Translation HSV → RGB

```
procedure HSV2RGB ( H,S,V : real; var R,G,B : real );  
var i, f, p, q, t: real;  
begin  
  if S = 0.0 then  
    begin                                     { achromatic case }  
      R := V; G := V; B := V;  
    end                                     else  
    begin                                     { chromatic case }  
      if H = 360.0 then H := 0.0;  
      H := H/60.0;                             { 0 <= H < 6 }  
      i := trunc(H);                            { number of slices: 0 <= i <= 5 }  
      f := H-i;                                { 0 <= f < 1 }  
      p := V * (1.0 - S);  
      q := V * (1.0 - S*f);  
      t := V * (1.0 - S*(1.0 - f));  
      ...
```



# Translation HSV $\rightarrow$ RGB

```
...
case i of                { six options: }
  0: (R, G, B) := (V, t, p); { short for 3x " := " } }
  1: (R, G, B) := (q, V, p);
  2: (R, G, B) := (p, V, t);
  3: (R, G, B) := (p, q, V);
  4: (R, G, B) := (t, p, V);
  5: (R, G, B) := (V, p, q);
  end;
end;                { chromatic case }
end;
```



# Other Colour Systems

- **HLS** („hue”, „lightness”, „saturation”)– Similar to **HSV**, double cone
- **Company standards**– e.g. **TekHVC** (Tektronix)
- **Colour systems and atlases:**
  - **PANTONE**<sup>®</sup> (Pantone Inc.)
  - **Munsell Book of Colour**
  - **Ostwald system** (1931)



# Literature

- **G. Murch: *Human Factors of Color Displays*, in Advances in Computer Graphics II, Springer, 1986, 1-27**
- **J. Foley, A. van Dam, S. Feiner, J. Hughes: *Computer Graphics, Principles and Practice*, 579-599**

# End



Further information:

- Lecture A. Wilkie: ***Introduction to Colour Science***  
(NPGR025)