



Composition of Raster Images

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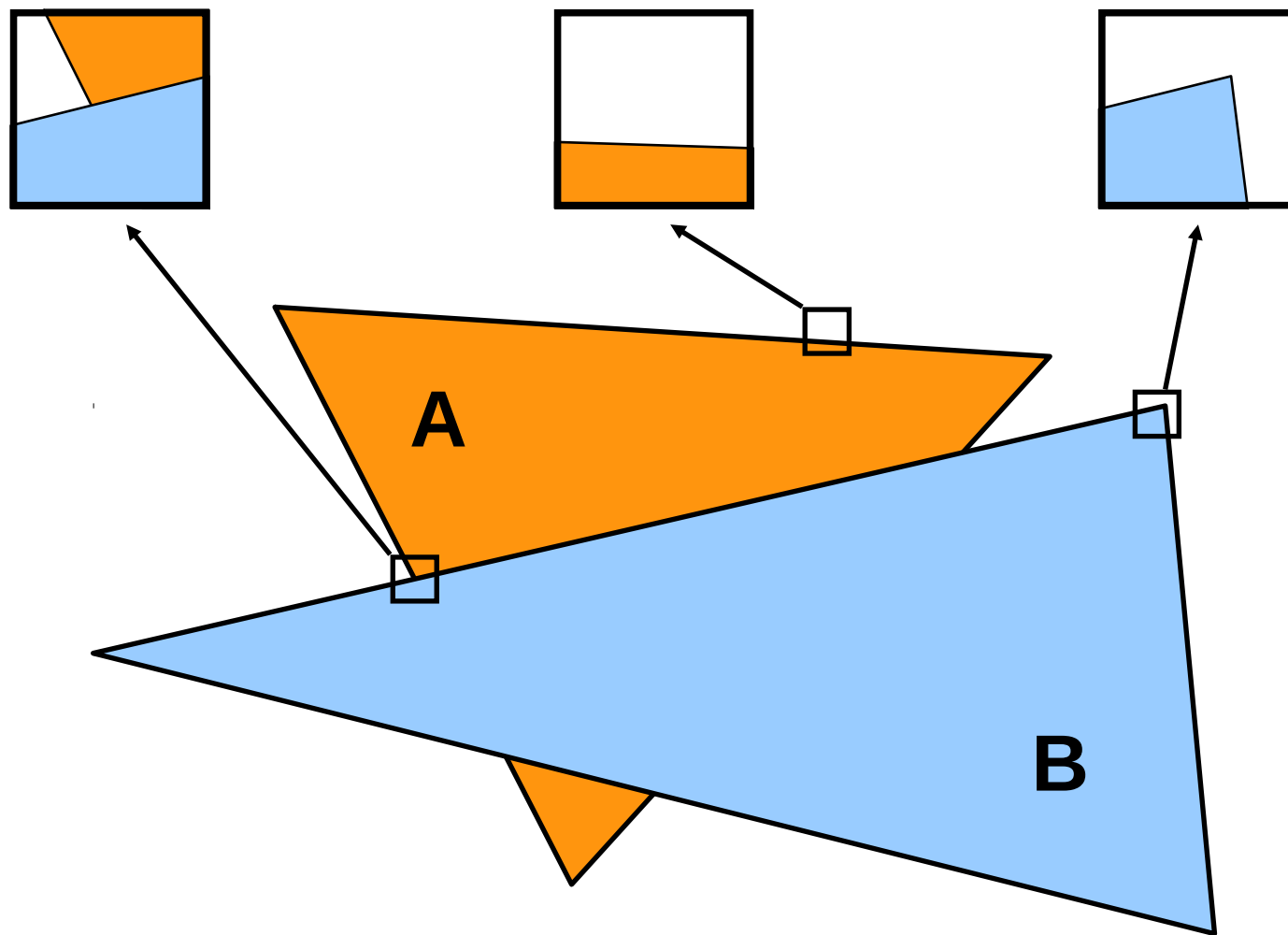


Image Composition

- **Superposition** of several real images
 - Inserting of objects into a different background, ...
- **Blending** of images, „**fade-in**”, „**fade-out**”
 - Animations, editing
- **Synthesis** of images
 - Composing an artificial images from several independently produced parts (e.g. background, foreground, hero character, fog, ...)



Coverage of the Pixel Area





Alpha Channel

- ◆ Measure of **pixel coverage** in percent
 - Stored as **transparency**:
 - $\alpha = 0$... totally transparent pixel (no effect on result)
 - $\alpha = 1$... opaque pixel („shows nothing beyond”)
- ◆ Values for α are stored in each pixel
 - Frequently integer representation ($0 \div 255$)
 - Quadruplet [**R, G, B, α**]
 - More frequent representation: [**R α , G α , B α , α**]

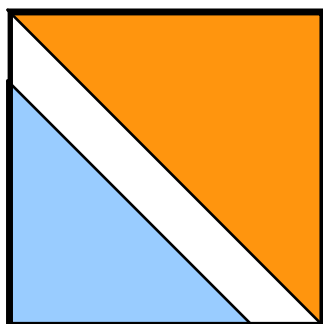


Compositing Two Images

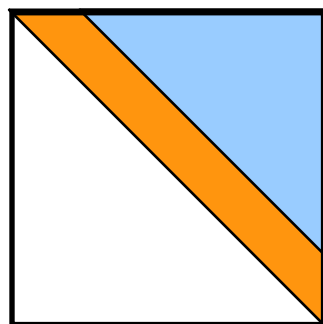
- Two input pixels $[A, \alpha_A]$ resp. $[B, \alpha_B]$
 - Result value: $[C, \alpha_C]$
- ? **how are these pixels composited ?**

$$\alpha_A = 0.5$$

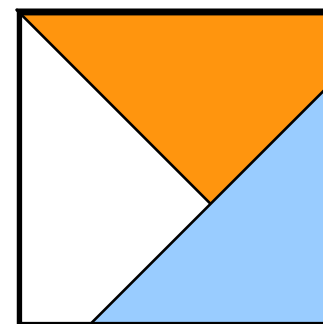
$$\alpha_B = 0.4$$



?



?

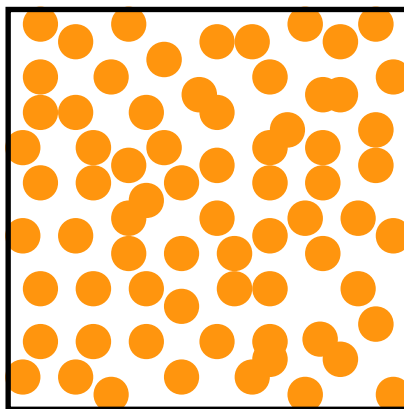




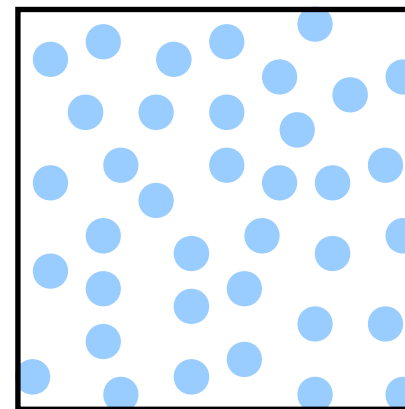
Pixel Coverage Model

- ◆ The pixel $[\mathbf{A}, \alpha_{\mathbf{A}}]$ is assumed to be **randomly covered** with colour \mathbf{A} with equal probability $\alpha_{\mathbf{A}}$
 - Independent of underlying shapes
 - Suitable in most cases

$\alpha = 0.5$



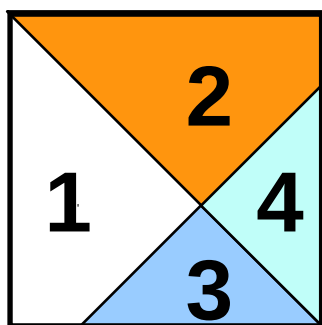
$\alpha = 0.2$





Overlap of Two Pixels

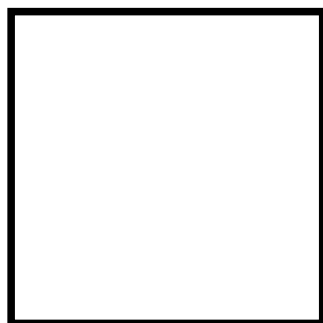
	Content	Area	Colour
1	<i>(empty)</i>	$(1 - \alpha_A)(1 - \alpha_B)$	0
2	A	$\alpha_A(1 - \alpha_B)$	0, A
3	B	$\alpha_B(1 - \alpha_A)$	0, B
4	A & B	$\alpha_A\alpha_B$	0, A, B



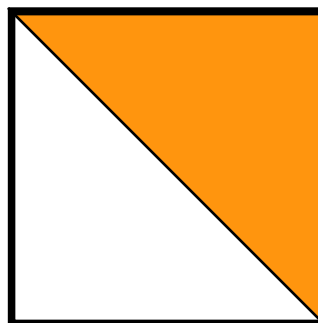
overall **12 possibilities**



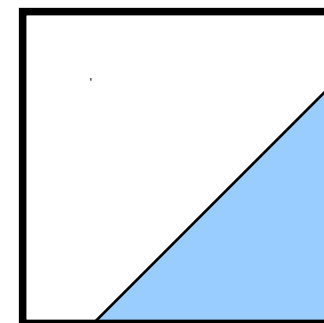
Combining Two Pixels



clear



A



B

Colours

(0,0,0,0)

(0,A,0,A)

(0,0,B,B)

F_A

0

1

0

F_B

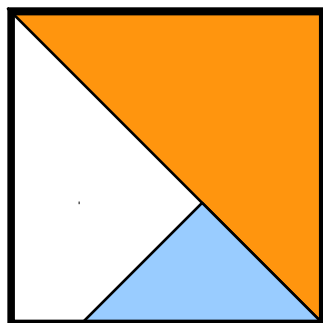
0

0

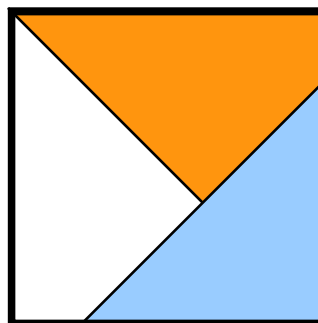
1



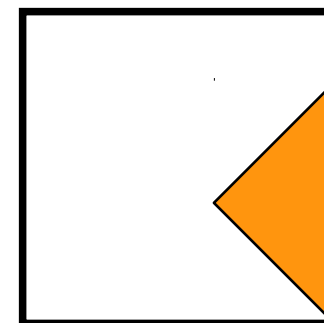
Combining Two Pixels



A over B



B over A



A in B

Colours

(0,A,B,A)

(0,A,B,B)

(0,0,0,A)

F_A

1

$(1 - \alpha_B)$

α_B

F_B

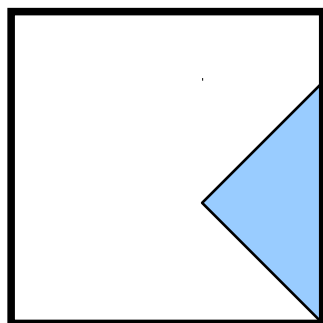
$(1 - \alpha_A)$

1

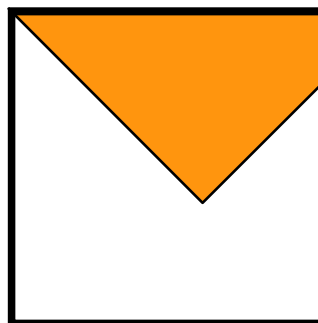
0



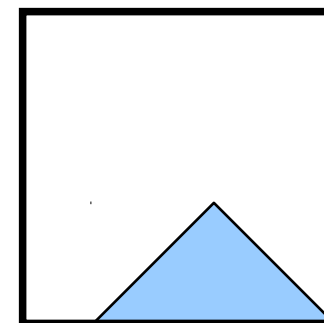
Combining Two Pixels



B in A



A held out by B



B held out by A

Colours

(0,0,0,B)

(0,A,0,0)

(0,0,B,0)

F_A

0

$(1 - \alpha_B)$

0

F_B

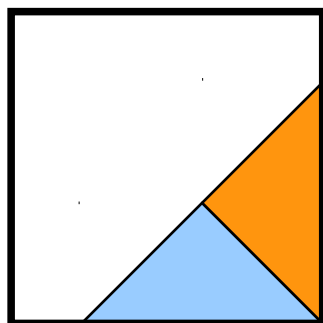
α_A

0

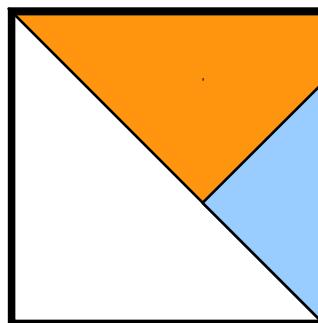
$(1 - \alpha_A)$



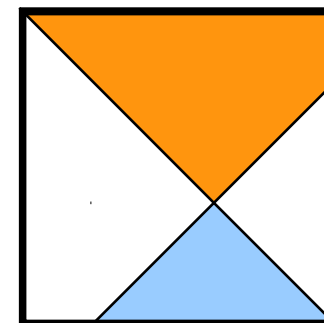
Combining Two Pixels



A atop B



B atop A



A xor B

Colours

(0,0,B,A)

(0,A,0,B)

(0,A,B,0)

F_A

α_B

$(1 - \alpha_B)$

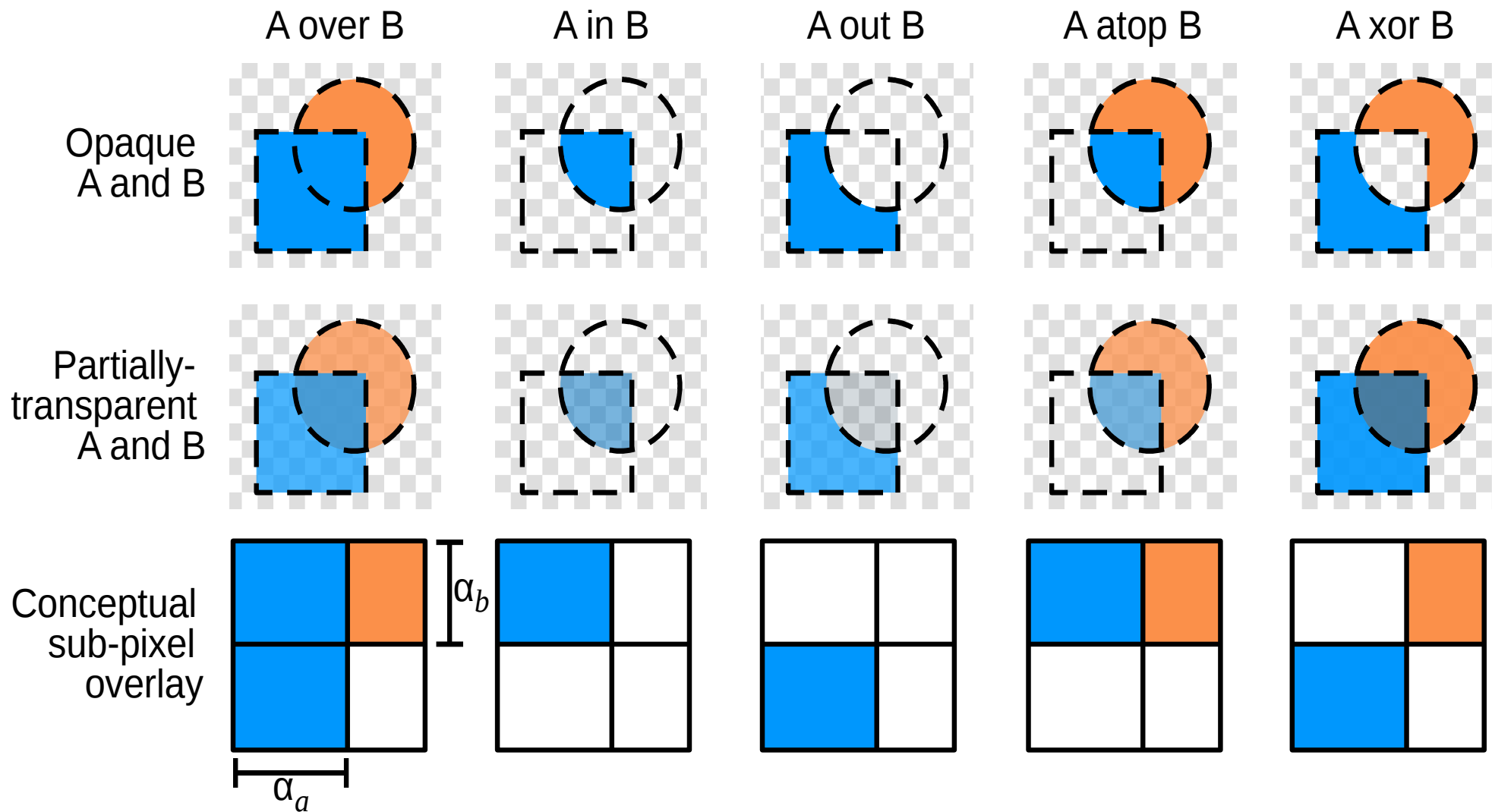
$(1 - \alpha_B)$

F_B

$(1 - \alpha_A)$

α_A

$(1 - \alpha_A)$





Implementation

- ◆ The four-tuple **RGBA** is **stored** in the form
[R α , G α , B α , α]
 - This is referred to as **pre-multiplied alpha**
- ◆ When using the values, alpha has to be **divided out**
 - E.g. when displaying the RGB values
- ◆ During pre mul alpha operations that involve **two pixels**, all four factors **F $_x$** are used
 - Advantage of pre-mul alpha: arithmetic ops work exactly like in the non-alpha case



Operations

◆ **Two pixel operation A op B:**

$$[F_A R_A + F_B R_B, F_A G_A + F_B G_B, F_A B_A + F_B B_B, F_A \alpha_A + F_B \alpha_B]$$

◆ Operator **darken** (A, ρ):

$$[\rho R_A, \rho G_A, \rho B_A, \alpha_A]$$

◆ Operator **fade** (A, δ):

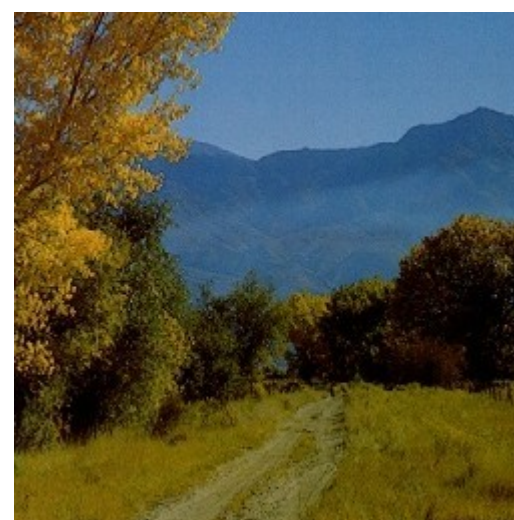
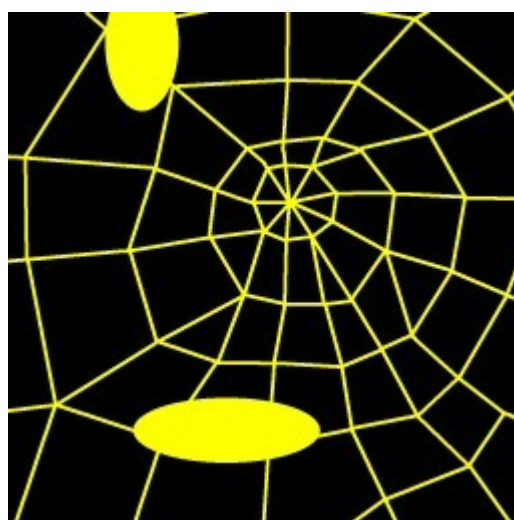
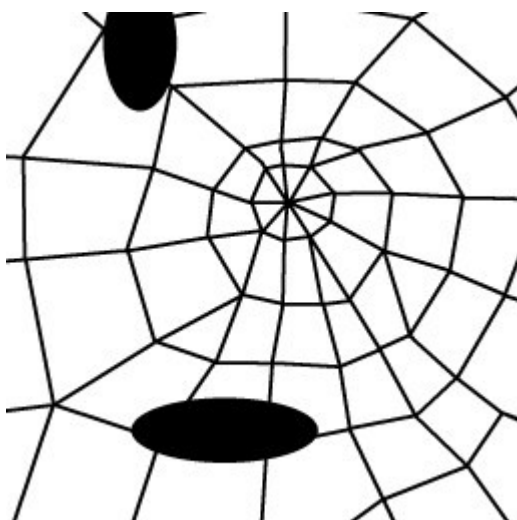
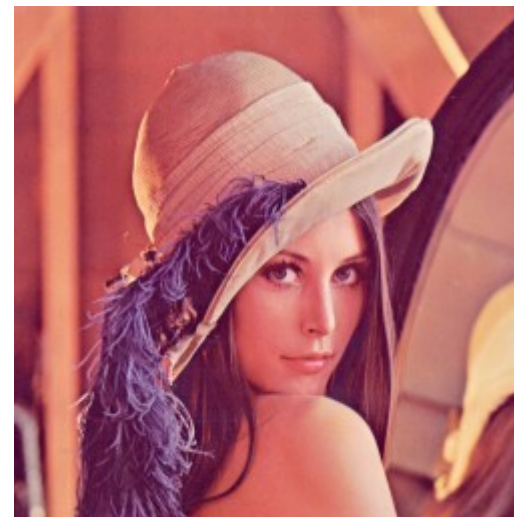
$$[\delta R_A, \delta G_A, \delta B_A, \delta \alpha_A]$$

◆ Operator **opaque** (A, ω):

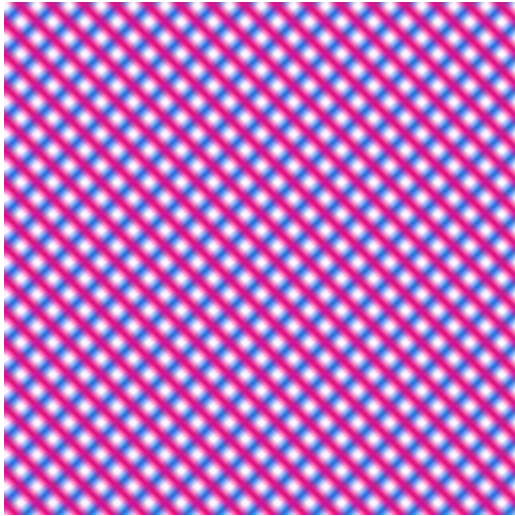
$$[R_A, G_A, B_A, \omega \alpha_A]$$



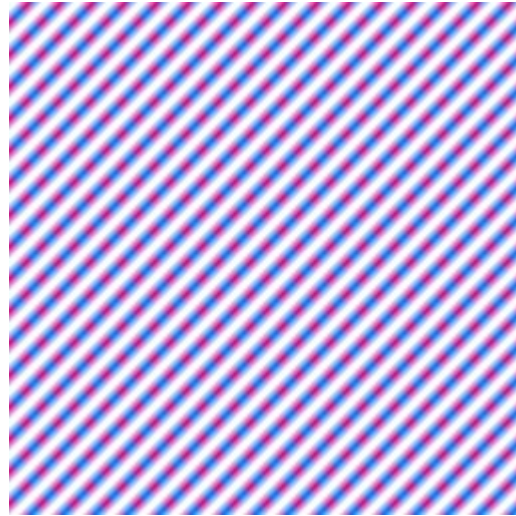
Example - Inputs



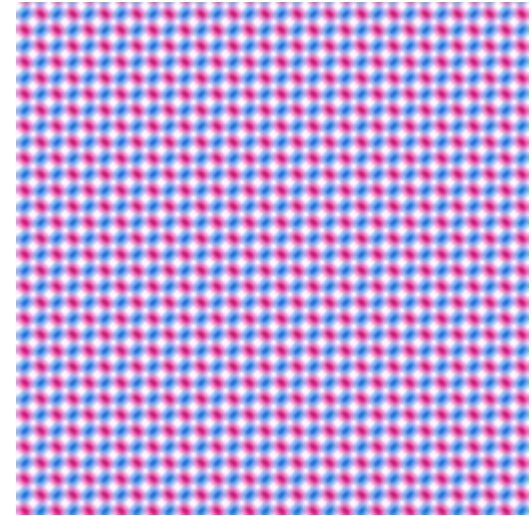
Example – binary operations I



1 over 2



1 atop 2



1 xor 2

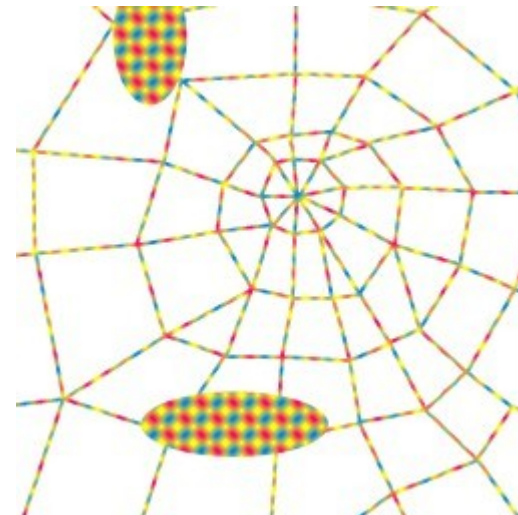
Example – binary operations II



1 in 2

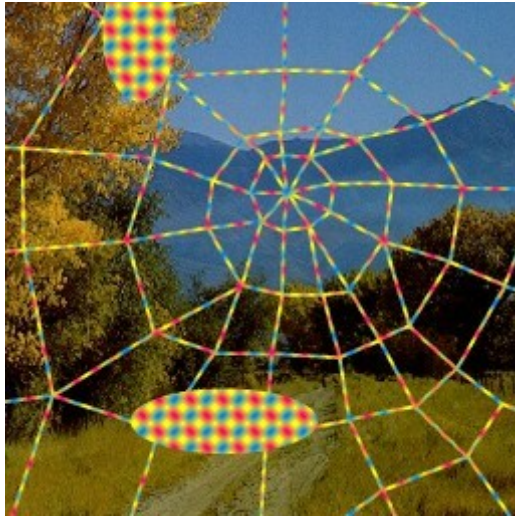


1 held out by 2



(1 xor 2) atop W

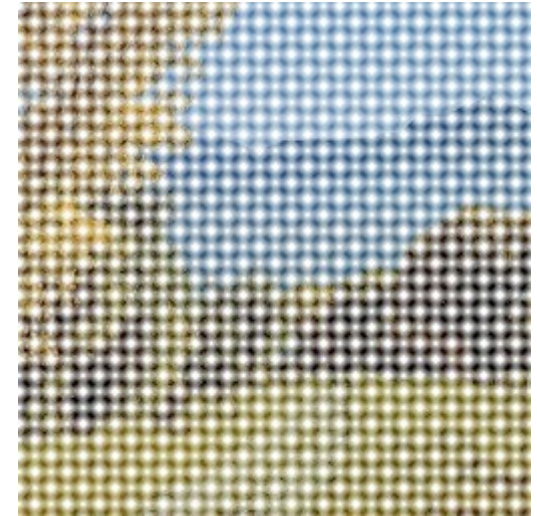
Example – binary operations III



$((1 \text{ xor } 2) \text{ atop } W) \text{ over } V$



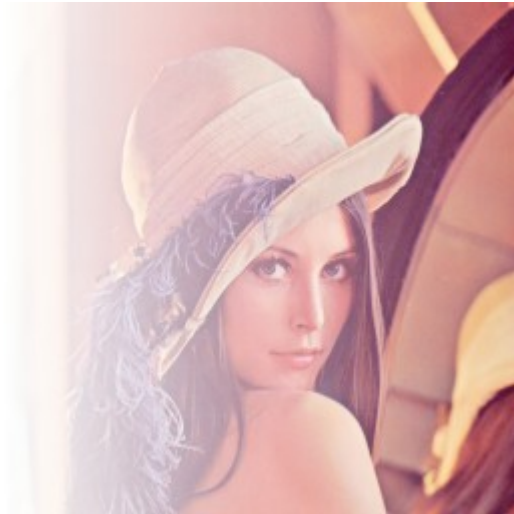
$(V \text{ atop } (1 \text{ xor } 2)) \text{ over } L$



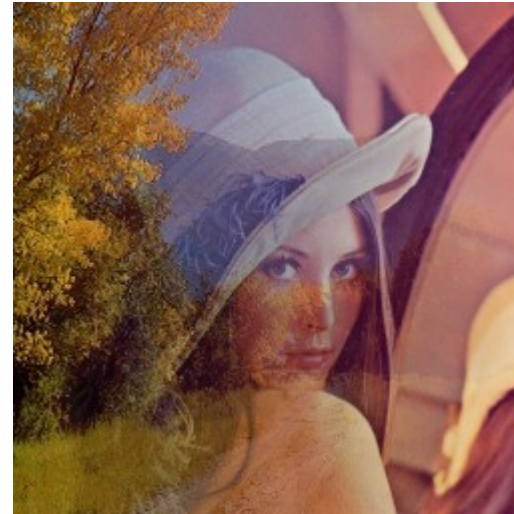
$V \text{ atop } (1 \text{ xor } 2)$



Example – Combinations



fade(L, horiz)



fade(L, horiz) over V



Operation „plus”

- **Addition: operator A plus B:**
 $[R_A + R_B, G_A + G_B, B_A + B_B, \alpha_A + \alpha_B]$
- ➔ **Example 1: combination of two images**
fade(A,t) plus fade(B,1 - t)
- ➔ **Example 2: burning tree**
(FFire plus (BFire held out by Tree)) over
darken(Tree,0.8) over Background

First use in the film Star Trek II (1982) – „Genesis Effect“:
<https://www.youtube.com/watch?v=Qe9qSLYK5q4>

End



Further information:

- **J. Foley, A. van Dam, S. Feiner, J. Hughes:** *Computer Graphics, Principles and Practice*, 835-843
- **T. Porter, T. Duff (Lucasfilm):** *Compositing Digital Images*, *Computer Graphics* 18(3), 1984