Supplementary Material for the SIGGRAPH 2012 Paper An Analytic Model for Full Spectral Sky-Dome Radiance

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1 Supplementary Figures

The figures that are shown on the following pages are not in the paper solely due to space constraints, but hopefully enable readers of the paper in assessing the quality of the data fitting we performed. All the charts in this supplement are for a ground albedo of 0; other albedo values are qualitatively similar.

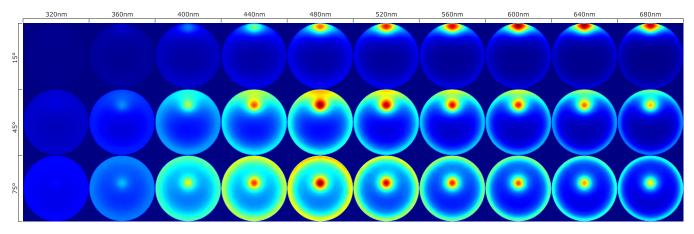


Figure 1: An alternate version of figure 7 in the paper. In this version, the radiance patterns for each waveband are all scaled to the same global scale for each solar elevation, so that the relative intensity of the wavebands can be seen. This version was not put in the paper because the individually scaled plots do a better job of showing the patterns for each waveband, which we deemed to be more important for the point we wished to make at that particular place in the paper. However, the relative magnitude of the wavebands is only visible in this version.

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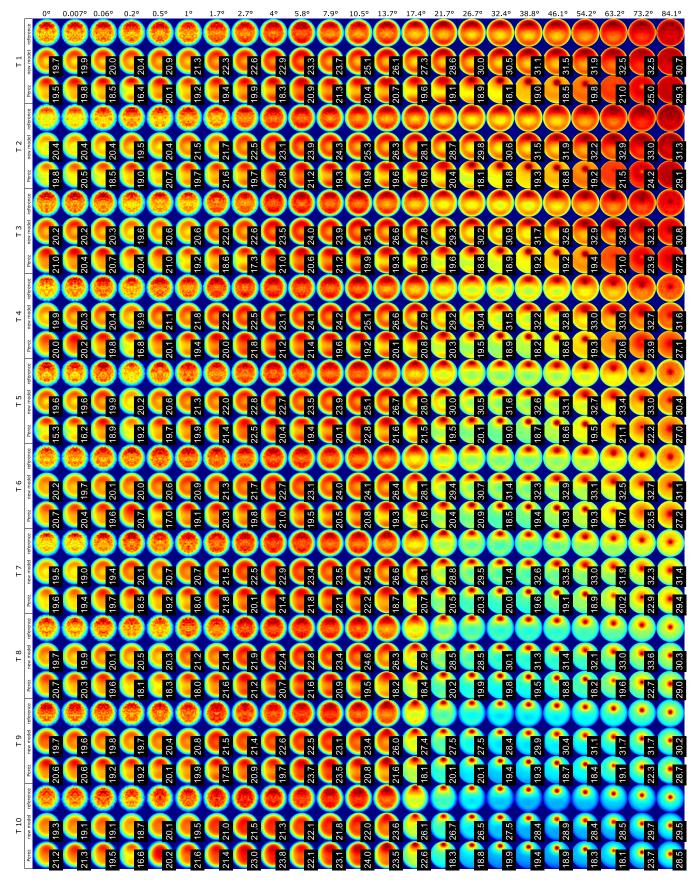


Figure 2: False colour result charts of the fitting process for 320nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output. Note the substantially different scattering patterns compared to the visible range that are in evidence for the ultra-violet part of the spectrum – the properties of Rayleigh scattering lead to UV emission being comparatively uniformly distributed across the sky dome.

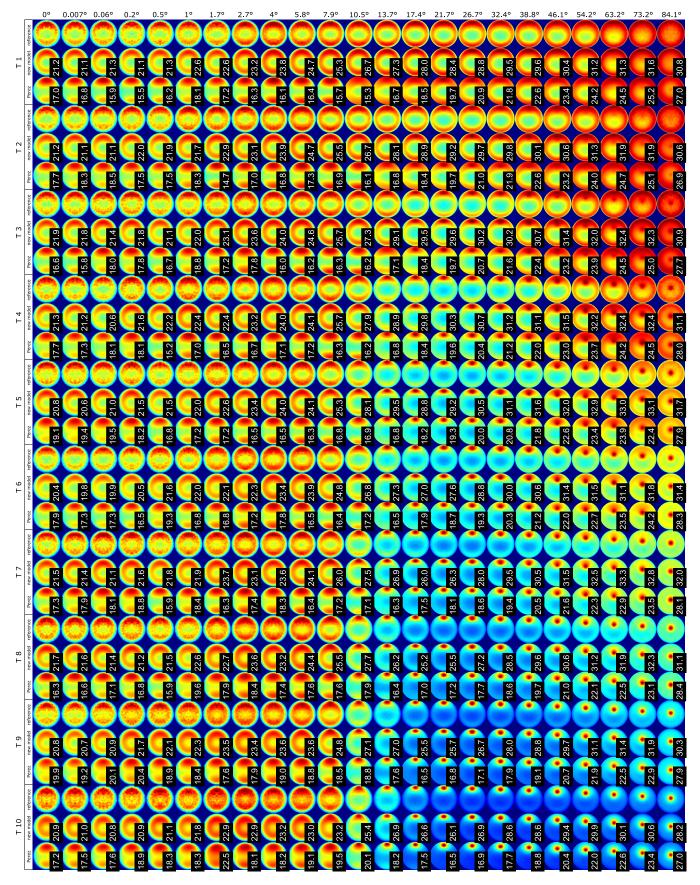


Figure 3: False colour result charts of the fitting process for 360nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

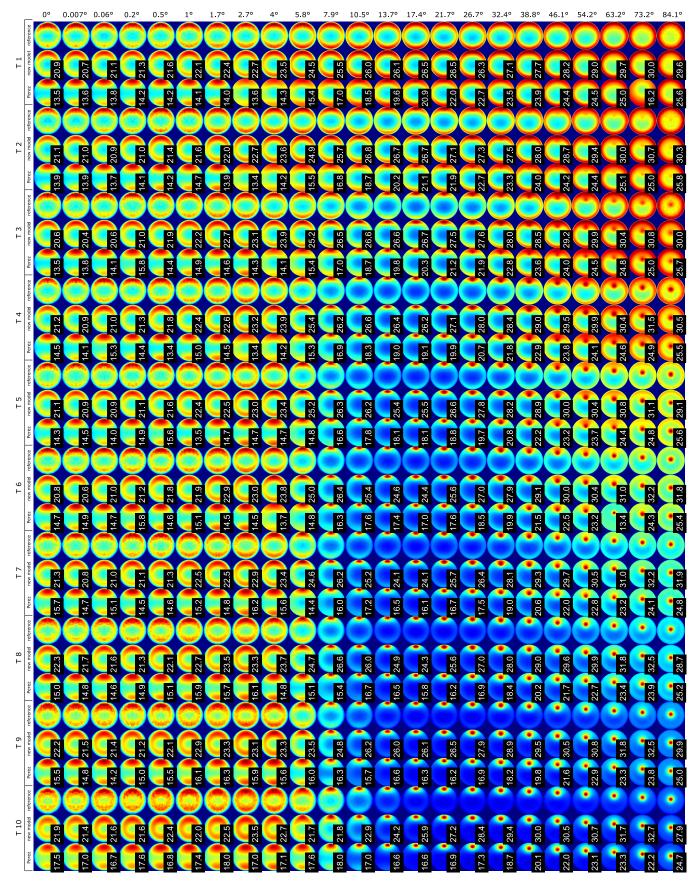


Figure 4: False colour result charts of the fitting process for 400nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

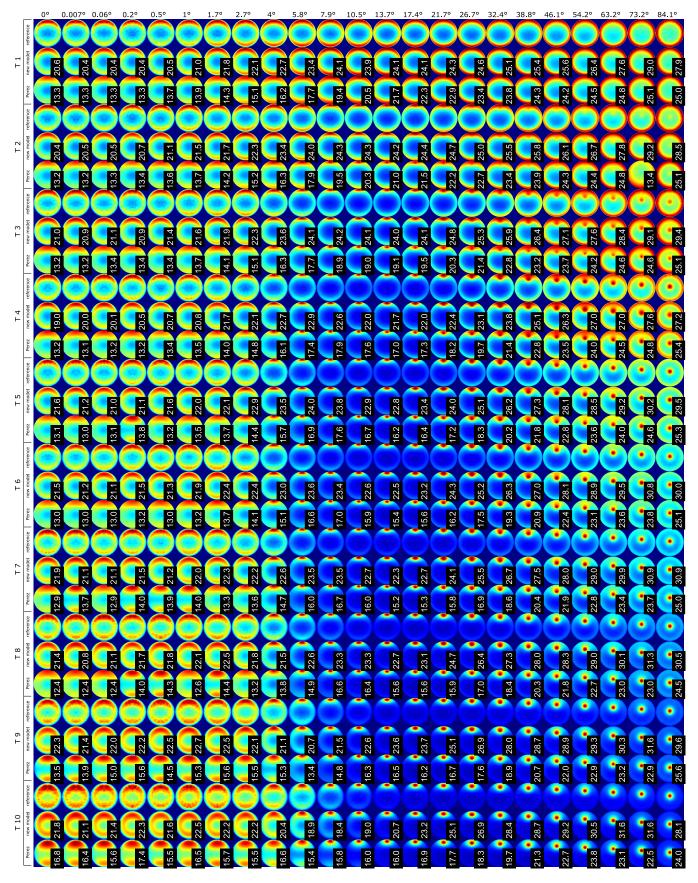


Figure 5: False colour result charts of the fitting process for 440nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

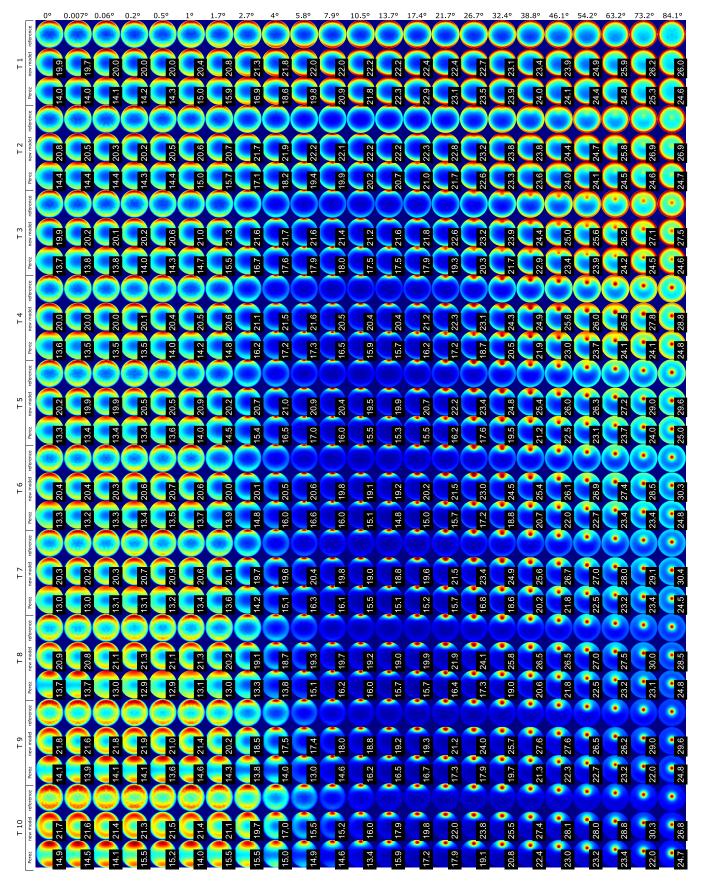


Figure 6: False colour result charts of the fitting process for 480nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

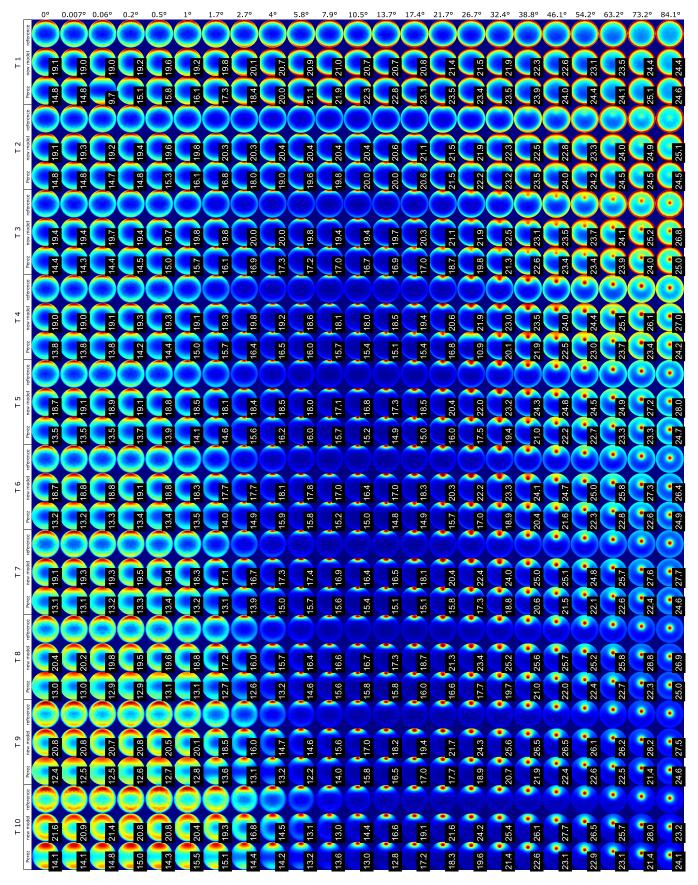


Figure 7: False colour result charts of the fitting process for 520nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

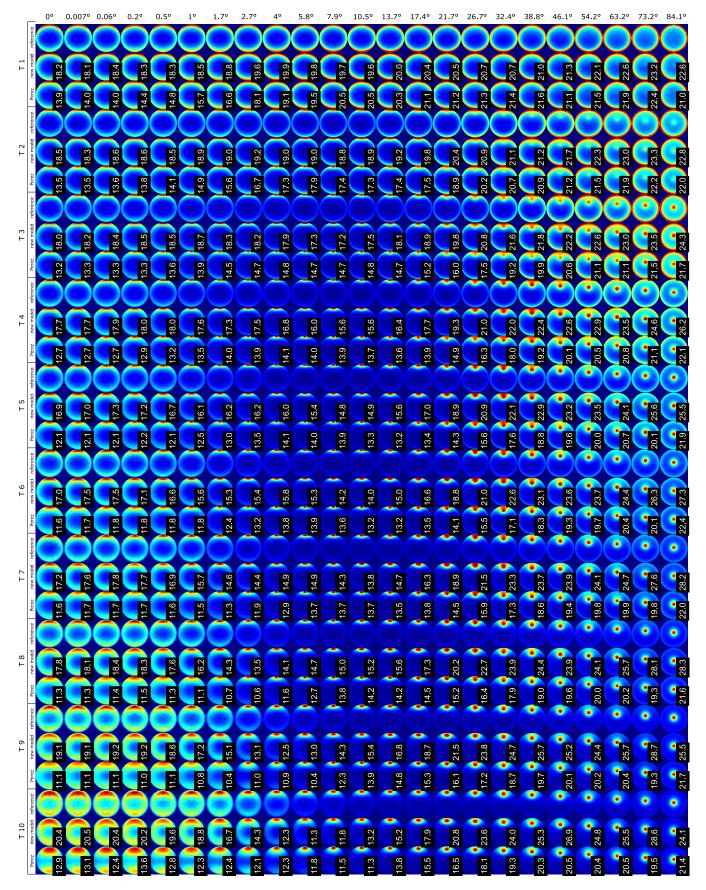


Figure 8: False colour result charts of the fitting process for 560nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

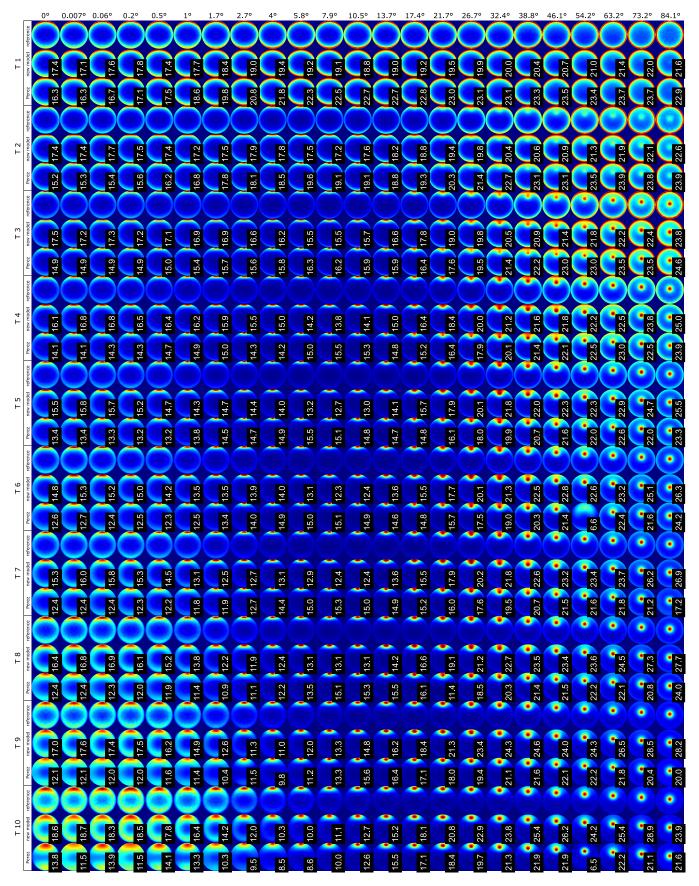


Figure 9: False colour result charts of the fitting process for 600nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

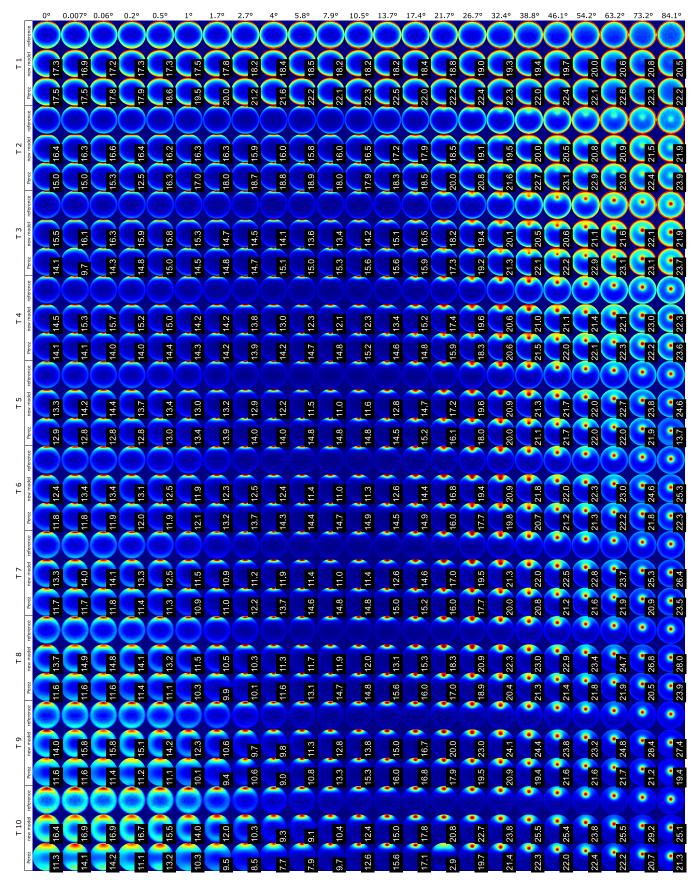


Figure 10: False colour result charts of the fitting process for 640nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

ſ	0°	0.007°	0.06°	0.2°	0.5°	1°	1.7°	2.7°	4°	5.8°	7.9°	10.5°	13.7°	17.4°	21.7°	26.7°	32.4°	38.8°	46.1°	54.2°	63.2°	73.2°	84.1°
		\bigcirc																					
Τ1	16.8	16.7	16.9	17.0	16.8	17.3	17.5	17.5	17.8		17.6		17.8	18.0	17.9	18.2	18.3	18.5	19.1	19.3	19.9	50.1	19.6
	Perez 18.3	18.4	18.6	18.8	18.9	19.3	20.6	20.7	21.3	51.7	51.6	51.0	51.3	51.6	20.7	51.3	50.8	51.6	21.7	21.4	51.3	21.4	20.9
	Leference	\bigcirc	\bigcirc																				$\overline{\mathbf{O}}$
Τ2	15.0	14.9	14.9	15.0	14.9	14.9	14.7	14.1	13.8	14.1	14.5	15.2	16.2	16.9	17.6	18.4	8:8	<u>94</u>	67	50.3			0.5
	Perez n 16.0		16.2	16.2	16.9	17.5	18.1	18.1	18.3	17.8	1	17.1	17.6	17.3	18.9	20.6	21.4	22.01	T-	5.2	54	53.8	2.6
	ference																						
Т 3	14.4	14.9	14.4	14.1	13.9	13.5	12.8	12.4	12.1	12.1	12.0	12.8	14.2	15.8	17.3	18.7	19.4		0:5	9.0		52.0	21:9
	Perez nev 14.3		14.7	14.3	14.6	14.6	14.5	14.7	15.1 12	14.9	14.8	14.8	14.7	15.3 15	16.6 17	19.1	20.9	<u>ب</u>	22.2	22.2	12.6	227	23.6
-	14	14	14	14	14	14	14	14	15	14	14	14	14	15	16	19	2	22.1	3				23
4	0	9	e	5	3			6	3	6		3	9	5	~	6			20.7	511	21.5		
F	ez new mo		2 14.3	8 13.5	3 13.3	3 12.7	3 12.4	3 11.9	9 11.3	7 10.9	1 10.7	9 11.3	7 12.6	9 14.5	9 16.8	18.9	5 19.8	3 20.5					1 23.5
-	Id. 0	14.0	14.2	13.8	13.8	13.6	12.8	12.3	12.9	13.7	14.1	14.9	14.7	14.9	15.9	18.0	20.5	21.6	21.5	21.8	22.3	21.0	23.1
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Ξ	12.5		13.4	13.0	12.3	11.6	12.1	11.5	10.9	10.3	10.1	10.8	11.9	13.9	16.4	18.6	20.3	21.2	21.4			23.4	22.9
-	ce Perez 12.7	12.7	12.9	13.2	13.0	13.6	13.6	13.1	4.3	14.2	14.2	3.7	14.8	14.8	16.2	18.2	20.2	21.6	21.5	21.4	21.8	20.4	23.1
	lel referen				$ \ge $																		<u> </u>
Τ6	10.8	12.0	12.2	11.7	11.0	10.8	11.0	11.4	10.7	10.1	9.8	10.3	11.6	13.9	16.3	18.8	20.2	21.2	21.8	52.1	52.1	23.7	24.9
	Perez	11.3	11.3	11.5	11.2	11.9	12.3	13.3	13.6	14.4	2.0	14.9	8.1	14.8	15.8	4.0	19.9	21.1	21.5	21.5	21.7	21.2	20.3
	reference																				<u> </u>	<u>•</u> (•
Τ7	new mode	12.6	12.5	11.8	10.7	9.4	9.7	10.7	10.9	10.5	10.0	10.4	11.7	13.8	16.3	18.9	20.7	.8 21.6	22.2	22.4	22.9	24.2	25.8
	Perez 11.0	T	10.9	10.7	10.4	6.6	10.7	12.2	13.4	14.5	14.9	14.6	14.7	14.9	15.9	3.5	19.9	20.8	21.2	21.1	21.5	21.1	15.5
	reference																			•	•	•	•
Τ8	12.1	13.3	13.1	12.6	11.6	9.8	9.2	9.5	10.4	10.7	10.6	11.0	12.4	14.7	17.4	19.9	21.5	22.4	22.7	22.6	23.0	26.2	23.1
	Perez 1	10.8	<u>9.3</u>	10.8	10.2	9.3	9.2	9.8	11.5	13.5	14.2	14.9	15.2	15.6	2.2	18.7	20.3	20.9	21.4	21.6	21.6	20.1	17.4
	eference	Õ					0													•	•	•	•
Τ9	13.6	14.0	14.2	13.5	12.6	10.9	9.5	8.6	<u>9.3</u>	10.6	11.9	13.2	14.7	17.0	19.6	22.0	23.4	23.6	23.0	23.4	25.3	27.9	26.3
	Perez nu 11.0		10.9	10.6	10.2					10.9	13.3	15.1	15.8	16.7	17.9		21.0 2	18.5 2	21.0	21.6	21.4	19.8	19.2
	ference	6	0			9.5	8.6	8.0	8.9							3.2	Ň		5	5	5	19	19
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								8.9	8.2	8.7		2 12.4	.8 15.1	.0 18.1	18.3 921.0	19.5	.1 24.2	21.1 25.1	15.6 24.1	.0 24.3	7 27.4	2 28.6	
	12. ⁷	10.7	10.6	10.5	10.2	12.4	8.5	7.7	7.0	7.9	9.9	13.2	15.8	17.0	18.	19.	21.1	21	15.	22.0	21.7	20.2	20.9

Figure 11: False colour result charts of the fitting process for 680nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

	09	° 0.007	° 0.06°	0.2°	0.5°	1°	1.7°	2.7°	4°	5.8°	7.9°	10.5°	13.7°	17.4°	21.7°	26.7°	32.4°	38.8°	46.1°	54.2°	63.2°	73.2°	84.1°
	reference		\bigcirc																		\bigcirc		
Τ1	new mode	16.3 16.0	16.5	16.6		17.5	17.5	17.0	16.8	16.8	17.0	174	17.5		17.9	18.0	17.8	17.9	18.2	19.0	19.6	19.5	18.9
	Perez	18.8 18.0	18.6	19.1	19.5	50.1	20.8	20.1	20.4	50.9	20.2	19.Z	20.6	20.2	Z07	50.9	50.8	207	50.1	21.6	212	51.6	20.7
	reference)		\bigcirc	\bigcirc																		$\overline{\mathbf{O}}$
Τ2	ew model	13.4	13.6	13.7	13.3	13.2	13.0	12.5	12.3	12.5	13.0	13.9	14.9	16.0	16.9		8:3	87	6 4	<u> </u>		<u>(0.3</u>	0.5
	Perez n	16.1 1 15 0 1		16.3	16.3	17.0	17.4	17.7	17.5 1	17.2	17.1	16.3	16.2	17.3	18.3	20.1	21.3	21.2	21.6	21.8	21.8	1.6	242
	ference																						
Т 3	v model re	12.5 12.6	12.8	12.5	12.0	1.5	FI	10.5	10.0	10.1	10.7	11.5	13.1	14.6	16.4	18.0	18.8	10.7	50.0	66		5155	
	erez nev	14.4 12		14.2	14.0 12	14.7	14.4	13.7 10	14.3 10			14.5	14.1 13	14.9	17.3 16	18.5 18	20.5 18	4	21.7	21.6	21.9	2	10
	rence P	14	14	14	14	14	14	13	14	14.4	6.3	14	14	14	-1	-18	2	N		5		No.	22
4	model refe	9		~		2	6	9	\prec	\prec	\prec	3				4			20.2	20.7	21.4		
F		3 12.6		4 12.6	9 11.8	3 11.5	10.9	10.6	9.9	9.5	9.5	3 10.3	11.7	13.7	16.2	9 18.4	3 19.7	20.1				1 22.3	52
	ance	13.3	13.3	13.4	12.9	12.3	11.6	12.0	11.8	12.6	13.6	13.8	7.8	8.5	10.0	17.9	20.3	21.0	21.4	21.5	21.9	22.1	23.0
ы	odel refere	\checkmark	\mathbf{X}	\prec	\prec	\prec	-	~	\prec		\prec	~	~							\sim		\leq	\prec
F		11.3		11.6	10.7	10.7	10.8	10.2	9.5	9.0	<u>9.1</u>	9.7	11.0	13.2	15.8	18.3	20.1	20.6	20.9			23.2	24.5
	ce Perez	12.6	12.6	12.5	12.9	13.1	12.7	12.3	12.5	13.3	0.9	14.6	14.2	14.2	16.0	4.0	20.3	11.2	21.7	21.5	21.7		21.6
	iel referen				$ \ge $																		<u> </u>
Τ6	new mod	10.1	11.3	10.5	6.6	9.7	10.4	10.3	9.6	8.8	8.8	9.4	10.9	13.1	15.6	18.4	20.1	21.2	21.3	21.5	21.9	23.5	24.7
	Perez	10.9	L F	11.0	11.1	11.6	12.8	12.4	4.0	2.6	14.5	14.6	14.4	9.6	16.3	18.4	20.1	21.4	21.2	21.2	21.1	19.6	20.1
	reference																					•	•
Τ7	new mode	9.5	10.7	10.3	<u>9.2</u>	8.7	8.9	9.6	<u>6.6</u>	9.2	9.1	9.6	11.0	13.1	15.7	18.4	20.2	21.4	21.8	22.0	52.1	24.2	25.9
	Perez	10.0	10.0	6.6	9.5	9.7	10.4	11.9	13.4	14.1	14.5	14.6	9.4	14.9	16.2	18.0	20.0	20.8	21.3	21:1	21.3	20.2	19.7
	reference																			•	•	•	•
Τ8	new model	10.5	11.3	10.7	6.6	8.6	8.1	8.9	<u>9.8</u>	9.8	9.6	10.2	11.7	14.0	16.8	19.3	20.8	22.1	22.4	22.7	23.0	25.3	26.6
	Perez	6.6		9.6	<u>9.0</u>	8.4	8.3	9.5	11.9	13.4	14.2	14.7	15.2	15.4	16.9	18.4	20.3	21.0	21.2	21.3	20.9	20.3	16.7
	eference			Ő				3											•	•	•	•	•
Τ9	w model	11.7	12.3	11.7	10.7	9.3	8.2	7.8	8.8	10.1	11.4	12.4	14.0	16.2	19.1	21.3	22.6	23.0	23.0	23.0	24.1	27.0	23.9
	Perez no	10.0 1								10.9	13.5	15.1		16.4	17.8	19.3 2	20.8	20.9	13.1 2	21.5	21.2	19.5	18.6
	ference		6.6	9.6	9.2	8.3	9.8	7.4	8.7				0.4				50	50	13	51	21	10	18
T 10	r model ret	13.3		13.0	12.0							<u>е</u>	0	<u>6</u>		نه	<u>,</u>	•	•	•	• <u>@</u>	• •	• m
F	arez new					6 10.6	0.6	5 7.8	7.5	8.4	2 10.0	5 12.3	6 14.8	9 17.9	2 21.0	19.5	20.7 923.9	21.2 24.7	15.1 23.7	8 24.1	3 26.8	8 28.4	3 25.3
	Pe	12.4	12.2	9.7	9.4	11.6	7.6	10.5	6.7	7.7	10.2	13.5	15.6	16.9	18.2	19.	20.	21.	15.	21.8	21.3	17.8	20.3

Figure 12: False colour result charts of the fitting process for 720nm. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

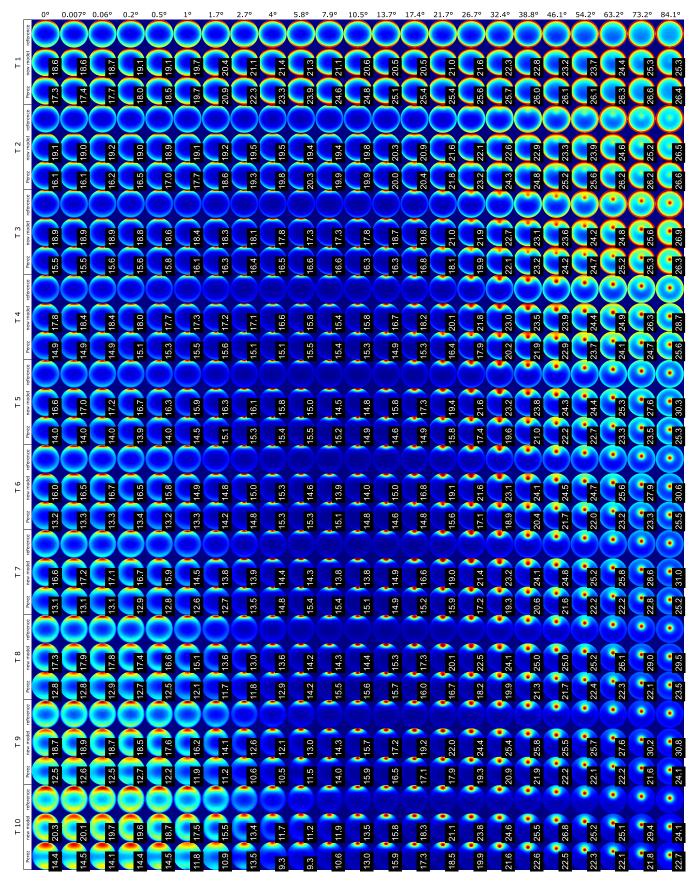


Figure 13: False colour result charts of the fitting process for the X channel of the XYZ model. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

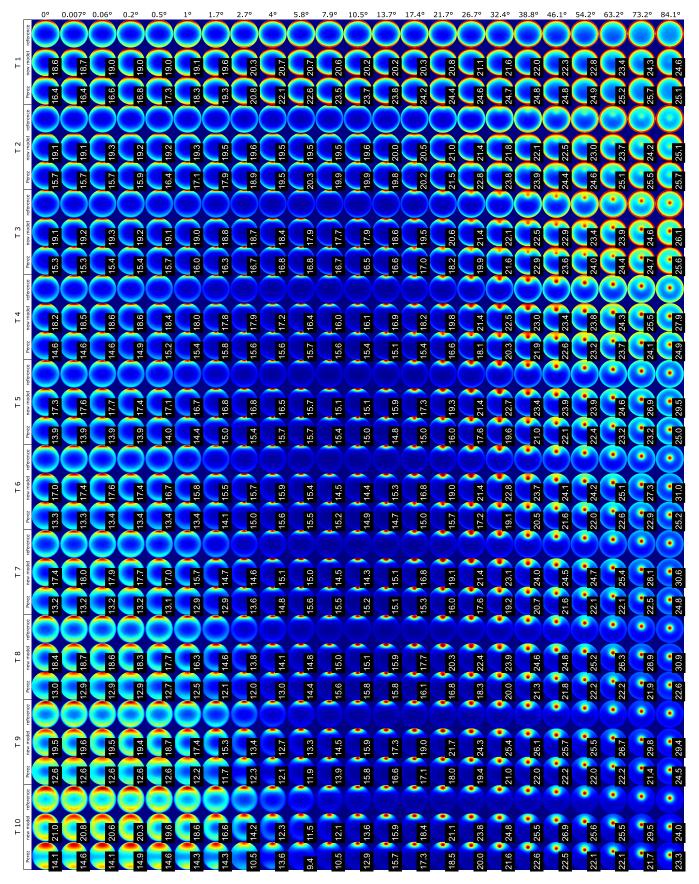


Figure 14: False colour result charts of the fitting process for the Y channel of the XYZ model. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

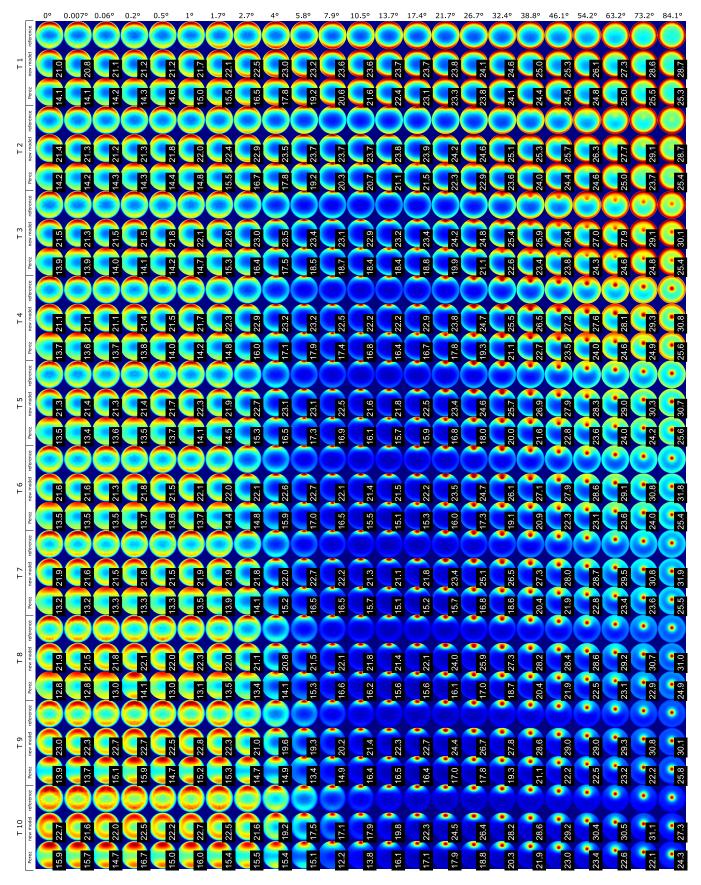


Figure 15: False colour result charts of the fitting process for the Z channel of the XYZ model. The rows labeled "ref" are results of the brute force reference simulation, those labeled "new model" are the output of the new model proposed in the paper. Rows labeled "Perez" are the output of the original Perez formula, with distribution parameters fitted specifically separately for each combination of turbidity/elevation. T indicates the turbidity value. Logarithmic SNR measurements are shown for each model output.

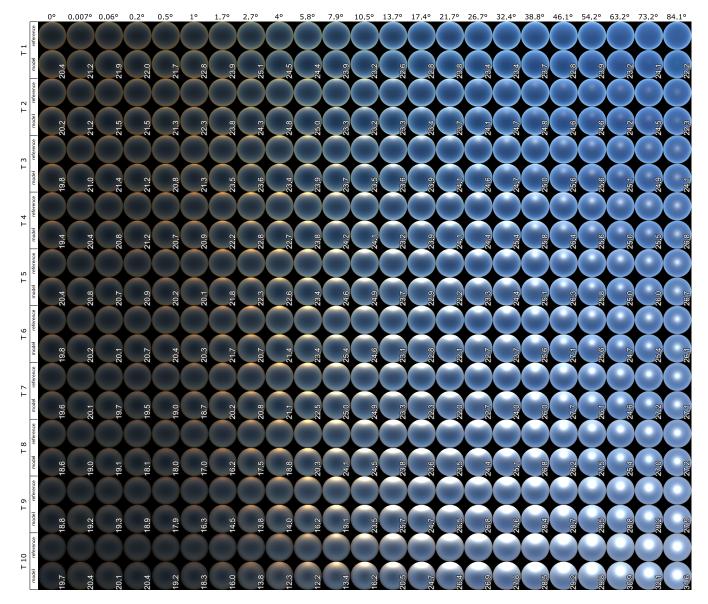


Figure 16: Outputs of the brute force path tracer, converted to sRGB compared to outputs of the new spectral model.Logarithmic SNR measurements in $L^*a^*b^*$ are shown for each model output.