

# Procedural Modelling of Urban Road Networks

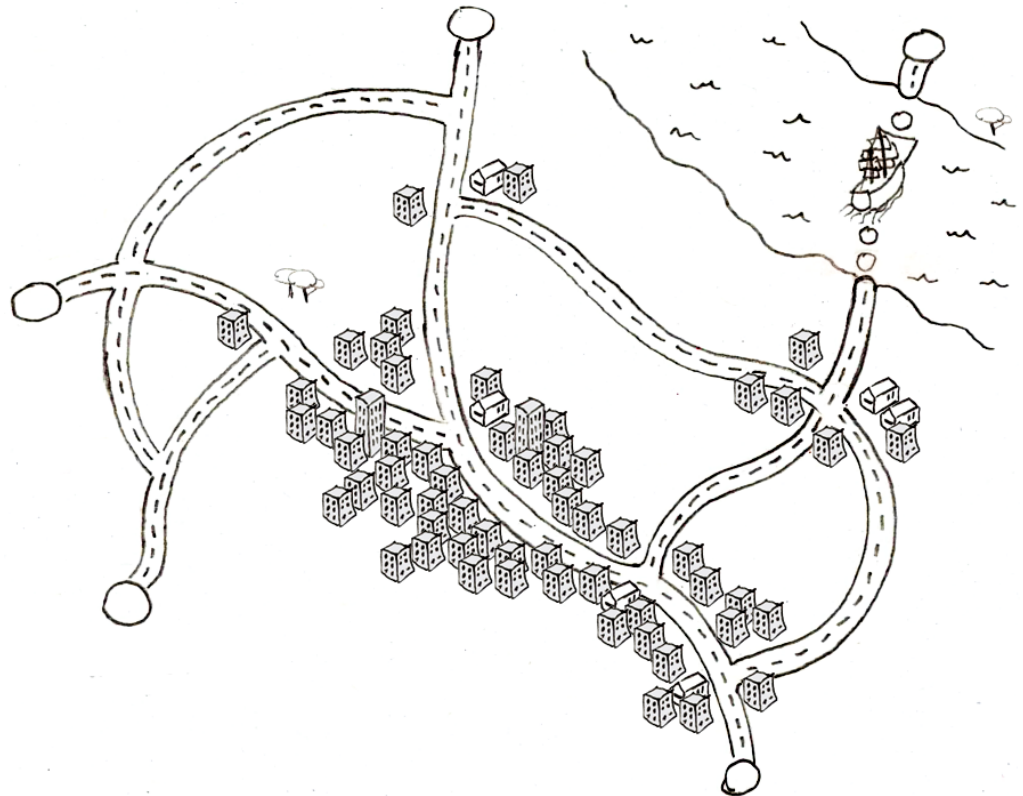
Jan Beneš, Alexander Wilkie, Jaroslav Křivánek



Computer Graphics Group at  
Charles University in Prague

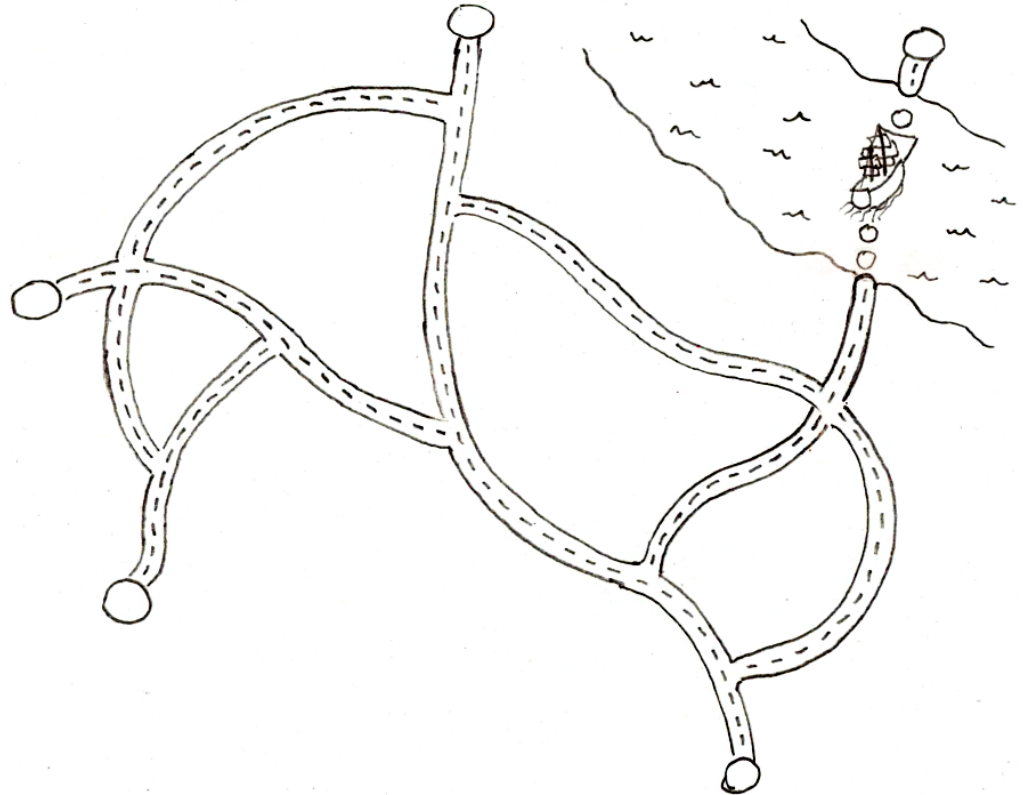
# Context

- Growing Cities



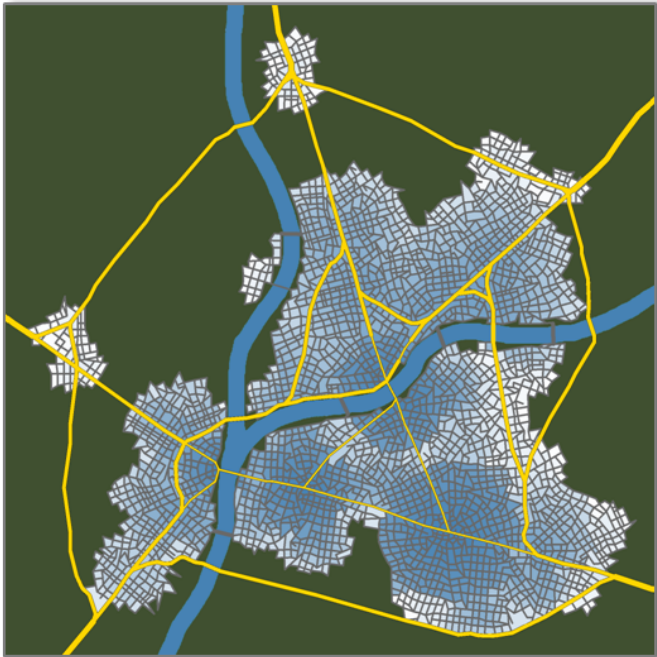
# Context

- Growing Cities
- Really mean roads
- Even if we say cities



# Goal #1

## Cities with a realistic structure



# Goal #1

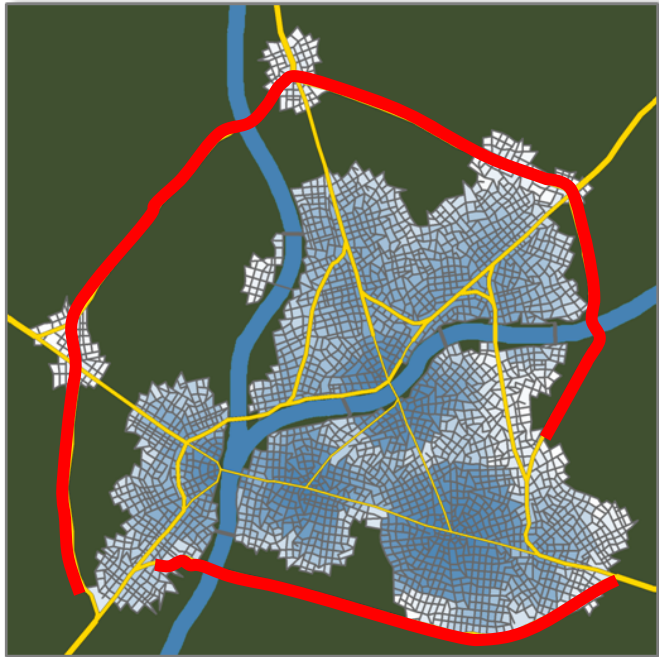
## Cities with a realistic structure



- Suburbs

# Goal #1

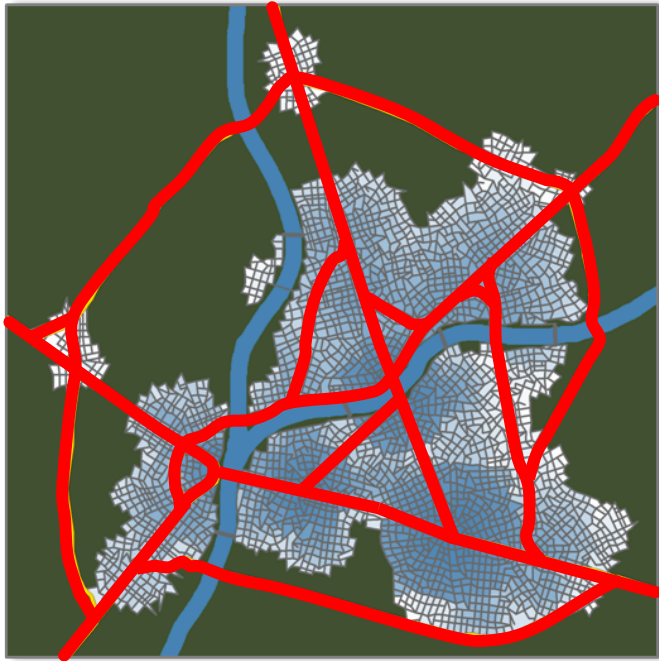
## Cities with a realistic structure



- Suburbs
- Belt roads

# Goal #1

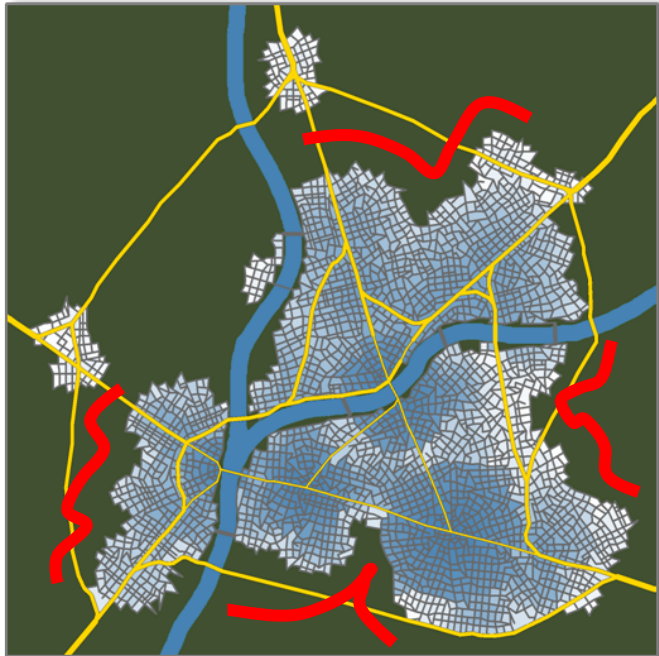
## Cities with a realistic structure



- Suburbs
- Belt roads
- Meaningful main roads

# Goal #1

## Cities with a realistic structure

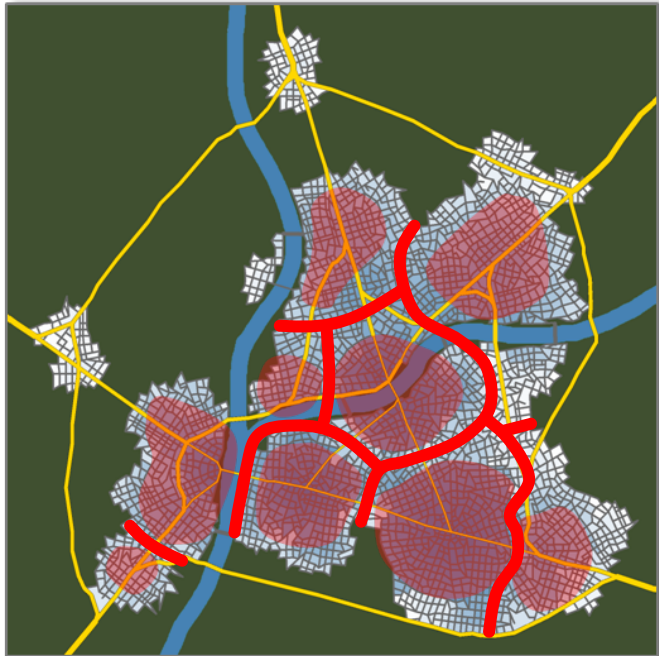


- Suburbs
- Belt roads
- Meaningful main roads
- Irregularities



# Goal #1

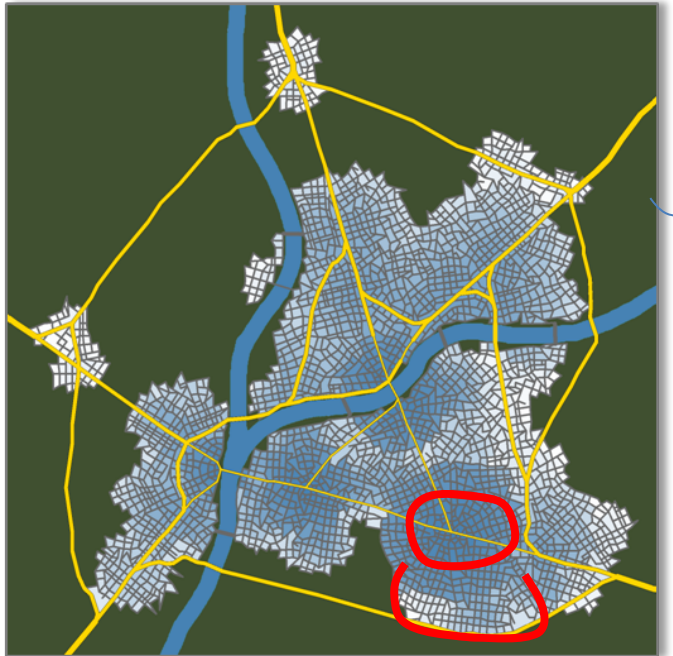
## Cities with a realistic structure



- Suburbs
- Belt roads
- Meaningful main roads
- Irregularities
- Agglomerations / Conurbations

# Goal #1

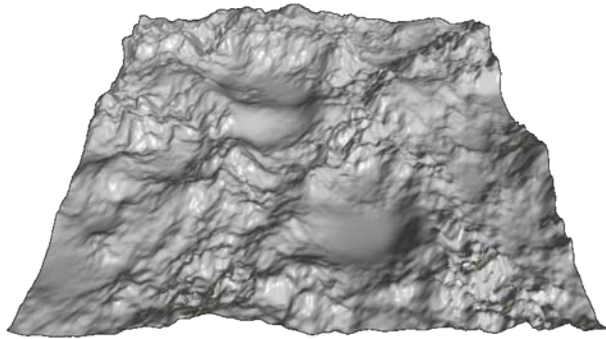
## Cities with a realistic structure



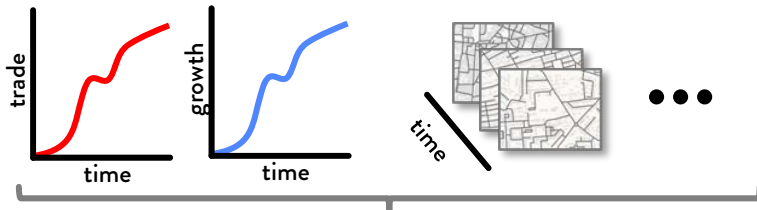
- Suburbs
- Belt roads
- Meaningful main roads
- Irregularities
- Agglomerations / Conurbations
- Changing street patterns

# Goal #2

## Cities with minimal input



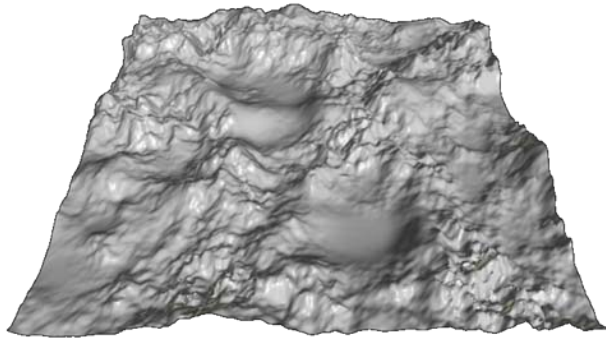
elevation map



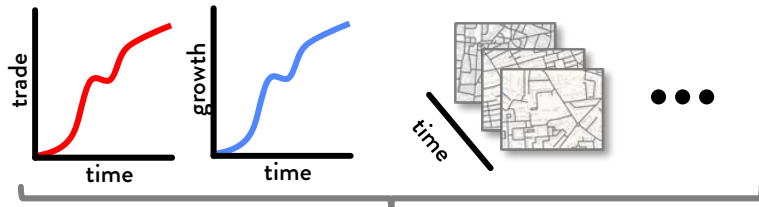
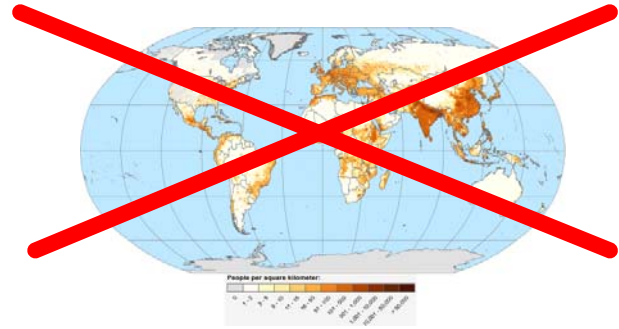
*“Historical Context”*

# Goal #2

## Cities with minimal input



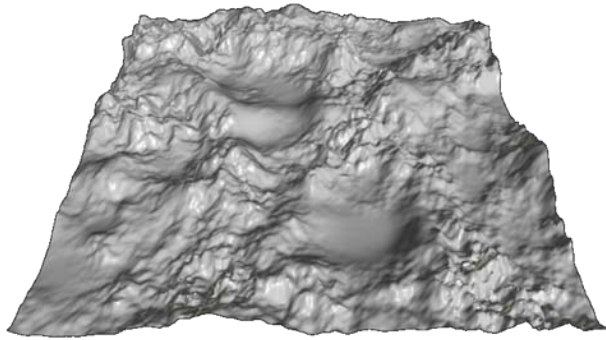
elevation map



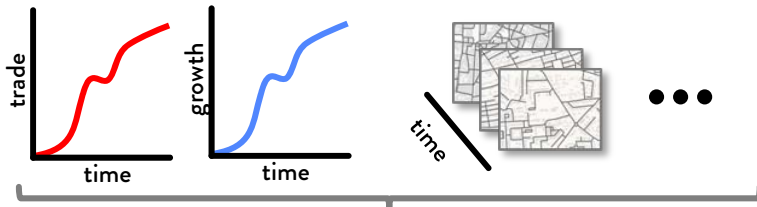
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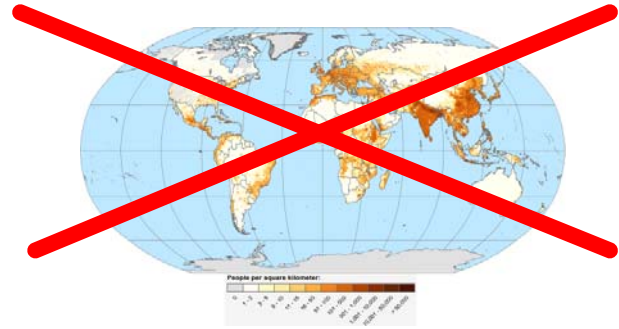
## Cities with minimal input



elevation map



*“Historical Context”*



# Previous Work

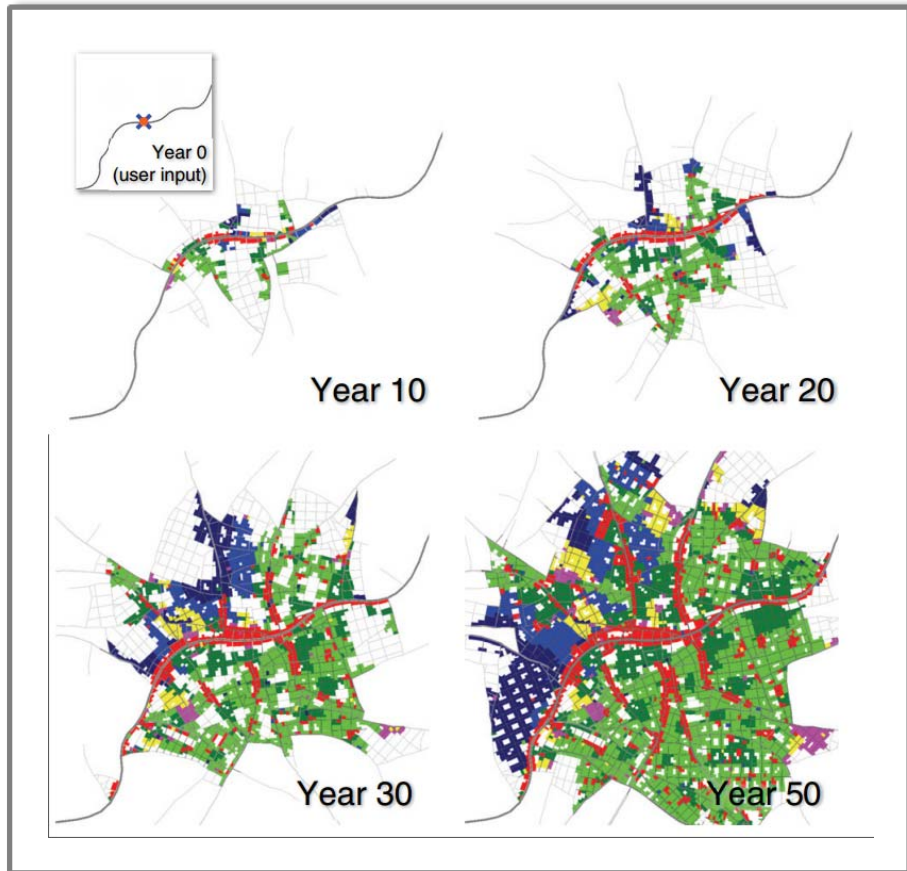
What we build on

# Existing Methods



- Procedural cities [Muller01]
- User-guided
- Input maps
  - Population
  - Street patterns
- No growth

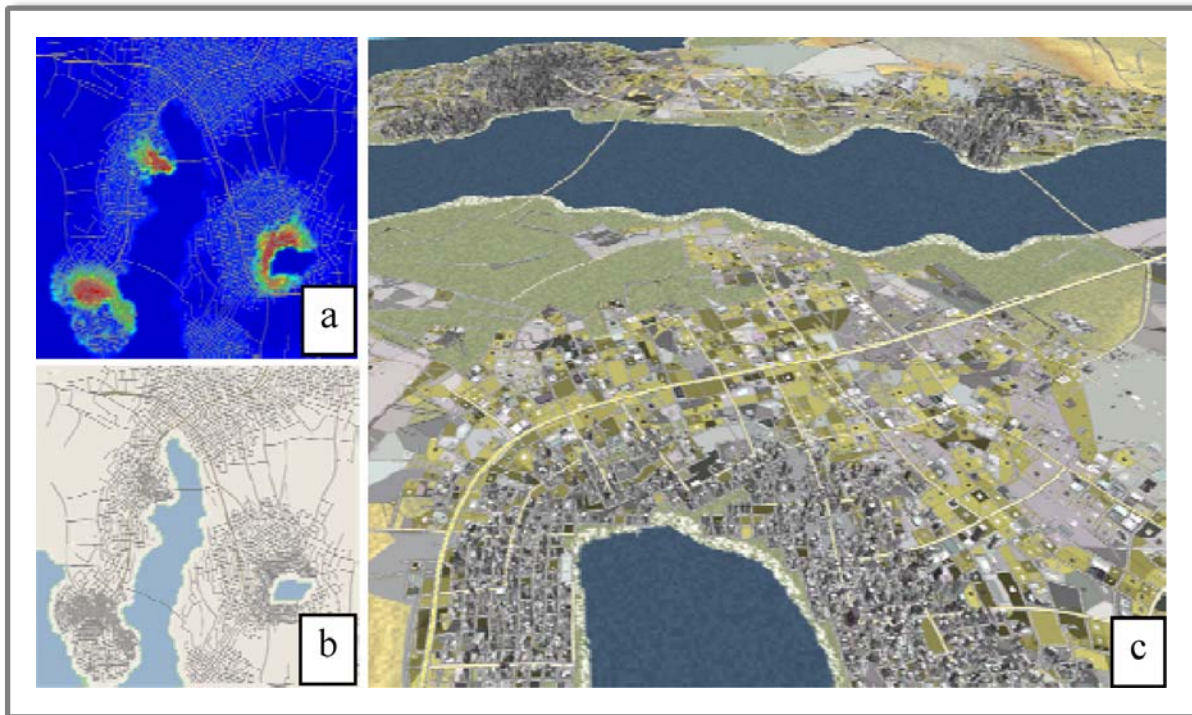
# Existing Methods



- [[Weber09](#)]
- City growth
- Local traffic simulation
- Controllable
- Automatic

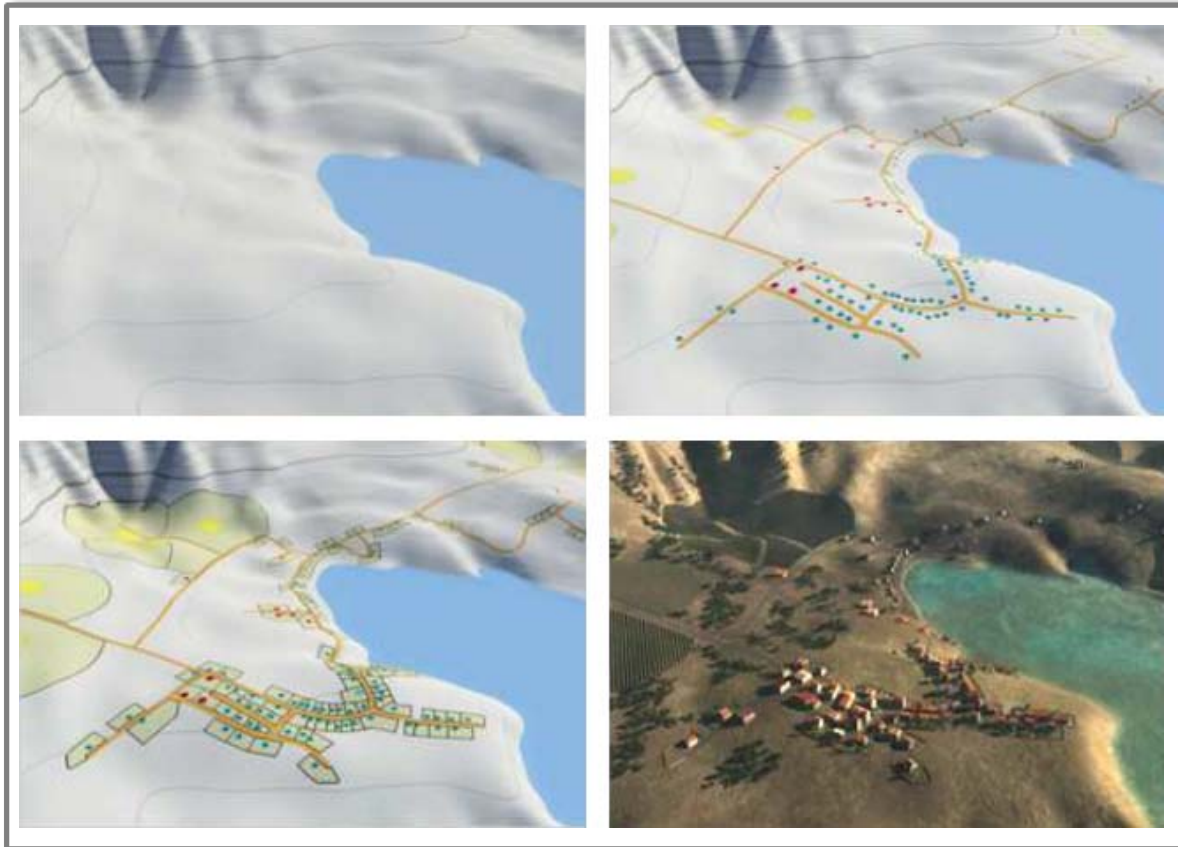


# Existing Methods



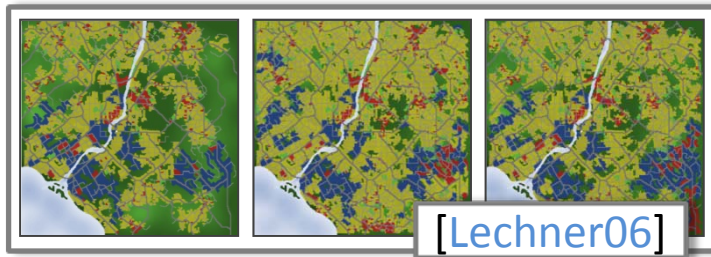
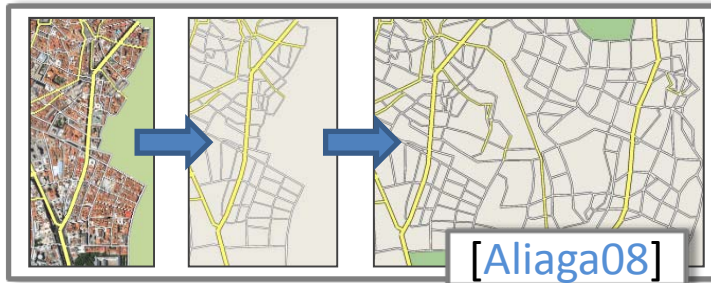
- [[Vanegas09](#)]
- Interactive
- Input
  - Highways
  - Demographic maps
  - Constraints
- Dynamical system

# Existing Methods



- [[Emilien12](#)]
- Villages
- Settlement positioning
- Sparse road networks

# Existing Methods



- Example based
  - [Aliaga08], [Yu12]
- Land use
  - [Lechner06]
  - [Gronewegen09]
- Interpolation
  - [Krecklau12]
- Other aspects
  - [Vanegas12], [Chen08], [Yang13], [Lipp11], [Galin11]

# Our Contributions

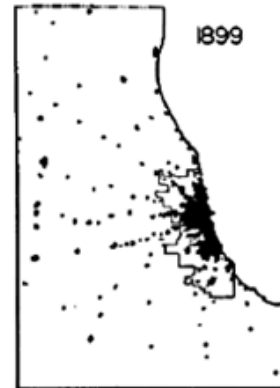
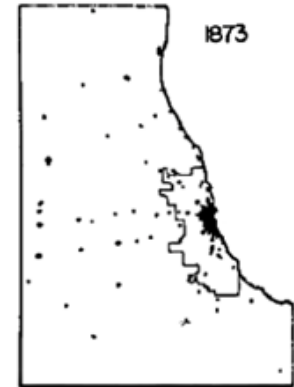
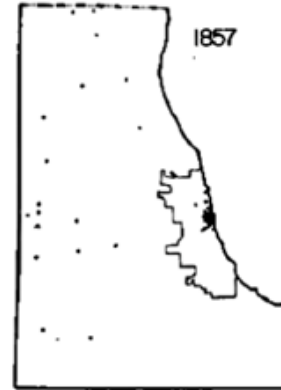
- More realistic city structure
  - Consider the neighbourhood
  - Trade driven major roads
  - Water and terrain
  - Settlement placement & city shape
  - Agglomerations/conurbations

# Rationale

From first principles

# City Shape

- What drives city shape?
  - Populated areas [[Hoyt39](#)]
  - Railways, stations
  - Similar for highways [[TT95](#), [Gar92](#)]
- Where does growth happen?
  - Accessible, e.g. stations
  - Well suited for service, e.g. intersections & ports
- “*Nuclei of growth*”

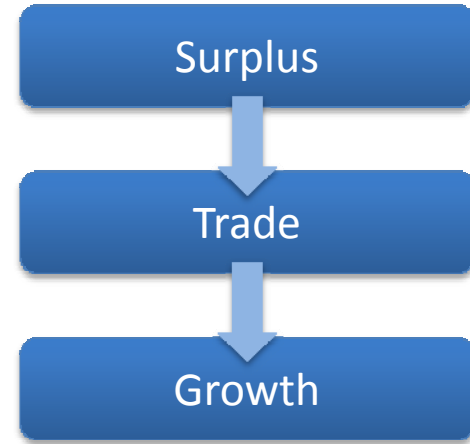


# Major Roads

- Nuclei of growth
  - Major road intersections
  - Ports
  - Both on major roads

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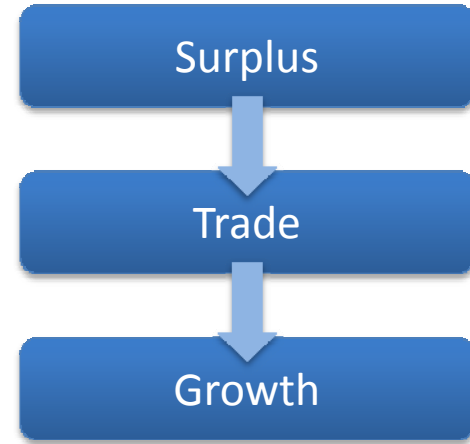


**Trade is a  
consistent and key  
factor in city growth**



# Major Roads

- Nuclei of growth
  - Major road intersections
  - Ports
  - Both on major roads
- Major roads
  - Simulate trade
  - *between* cities
  - [Childe50]



**Trade is a  
consistent and key  
factor in city growth**

# Minor Roads



Historic



Early 20<sup>th</sup> century



Late 20<sup>th</sup> century

**Minor road pattern  
changes with time**

- Simplifying assumption
- Also changes with:
  - Land use, terrain, etc.

# Method Overview

# Method Overview – First steps

- Preparing a city



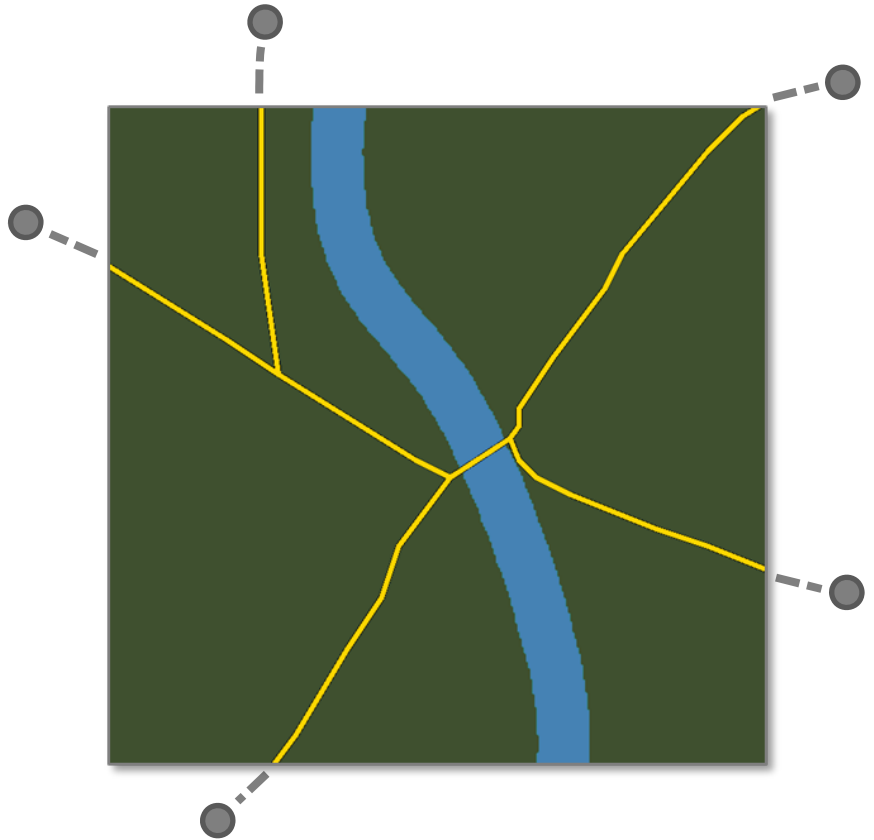
# Method Overview – First steps

- Preparing a city
  - Neighbouring Cities



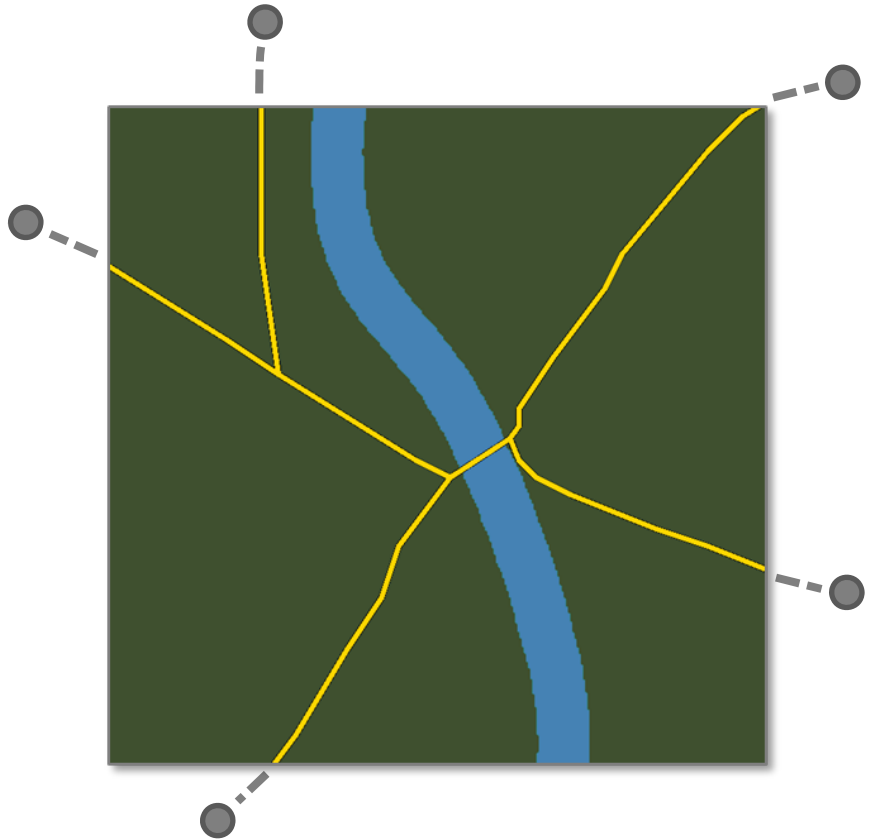
# Method Overview – First steps

- Preparing a city
  - Neighbouring Cities
  - Connect by major roads
  - Initial Road network



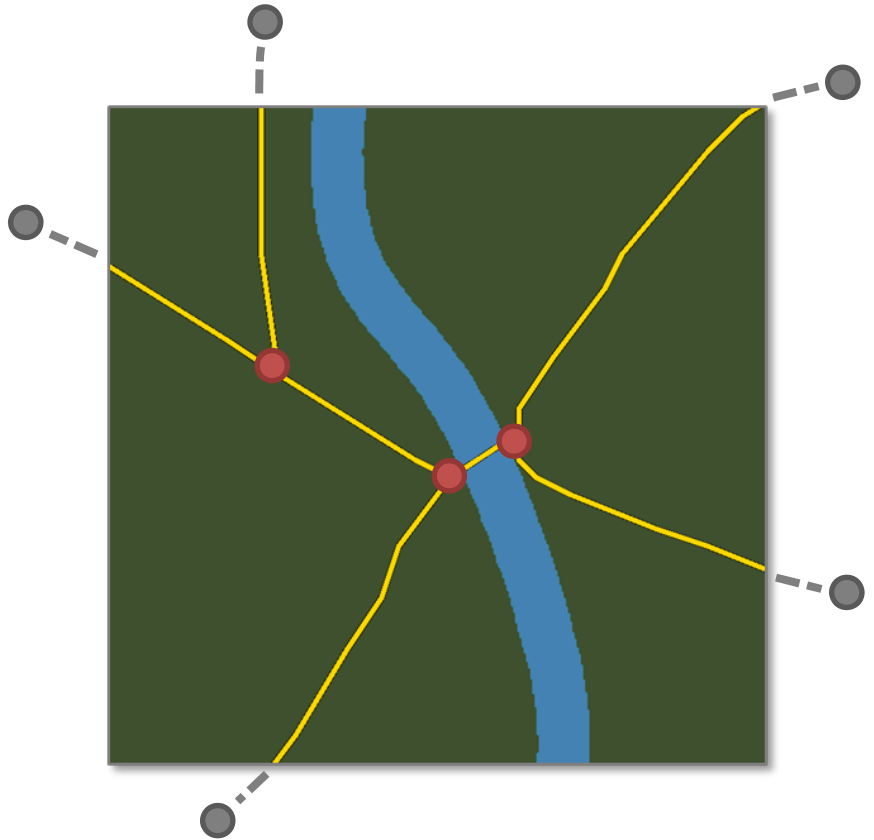
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- Preparing a city
  - Neighbouring Cities
  - Connect by major roads
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- Growing a city:



# Method Overview – First steps

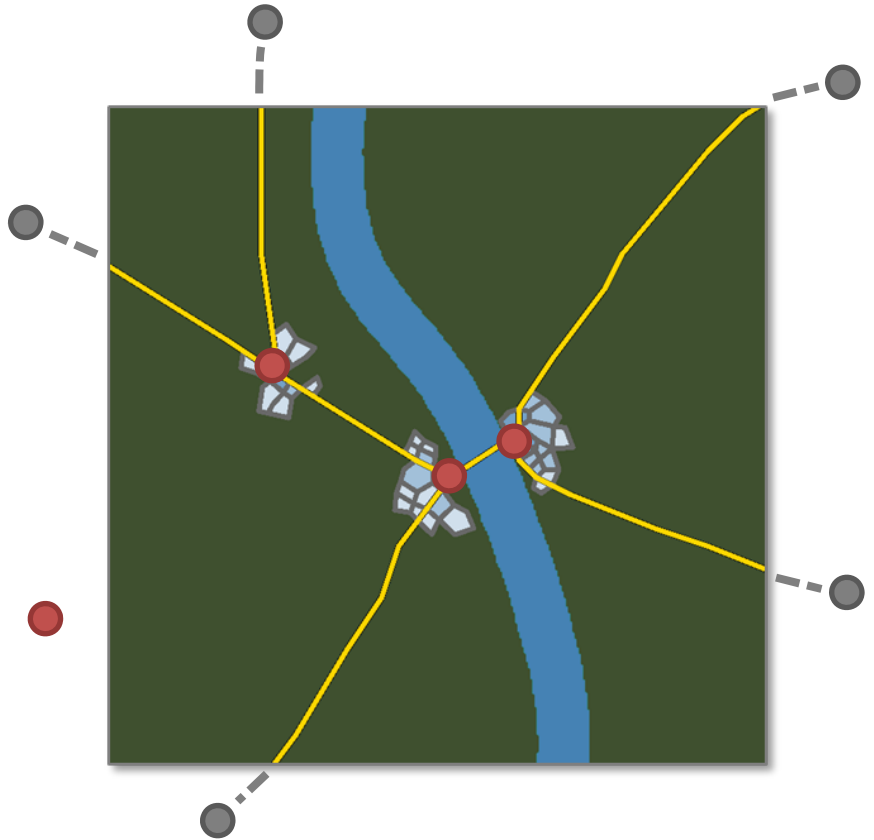
- Preparing a city
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- Growing a city:
  1. (Re)generate ●





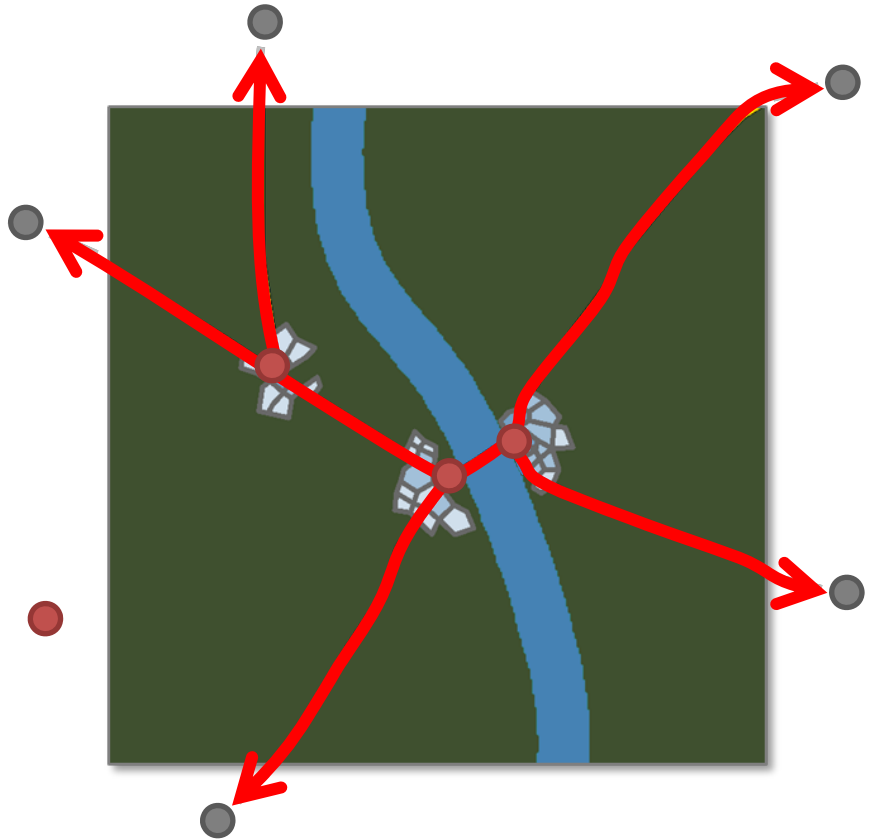
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- Preparing a city
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  - Connect by major roads
  - Initial Road network
- Growing a city:
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  2. Grow minor roads close to ●



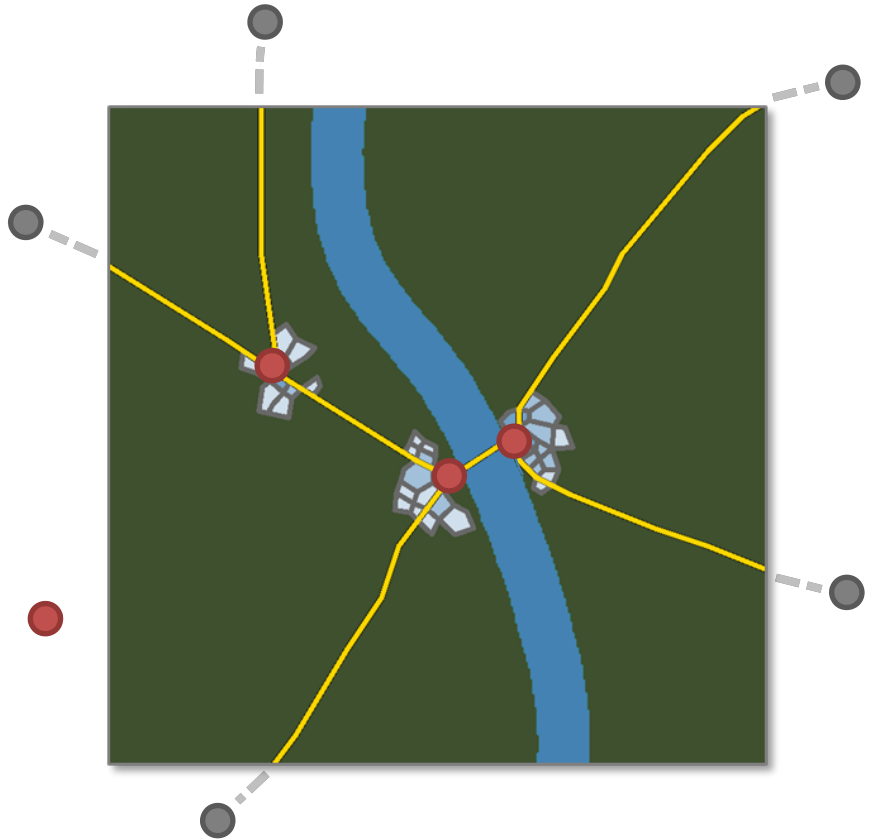
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  3. Increase Trade



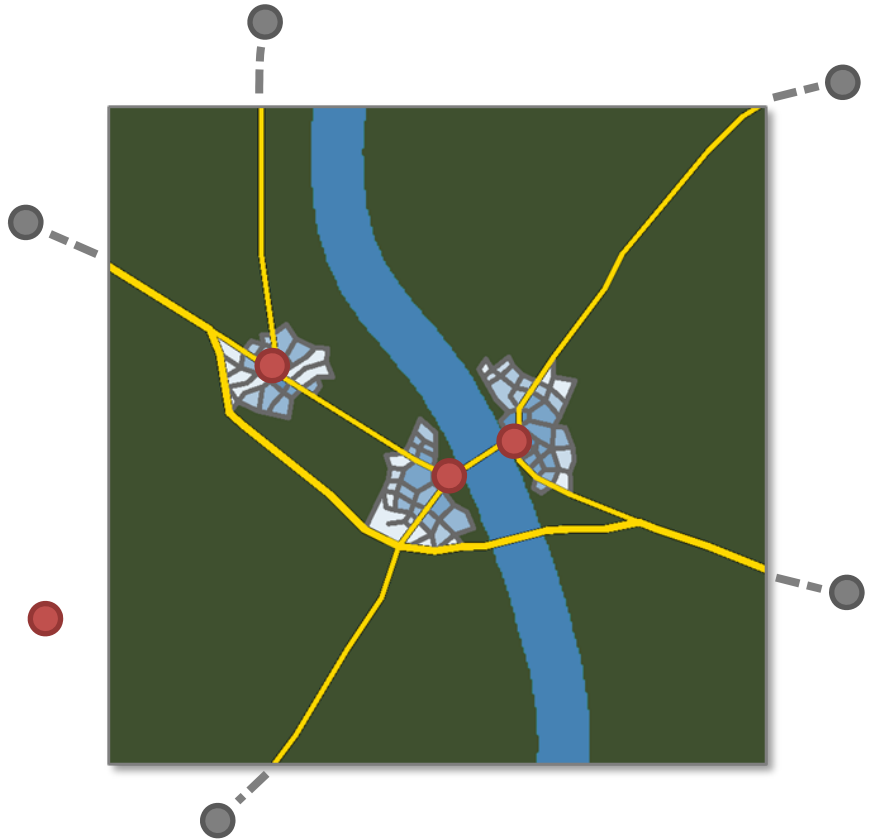
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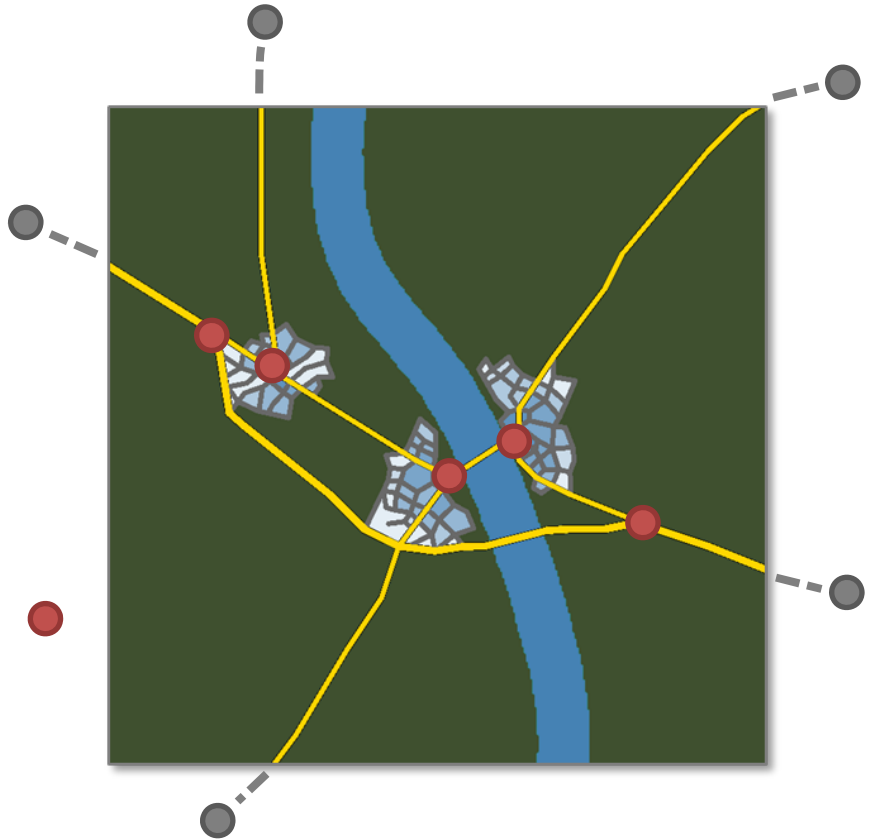
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  4. Grow Major Roads



# Method Overview – Major Roads

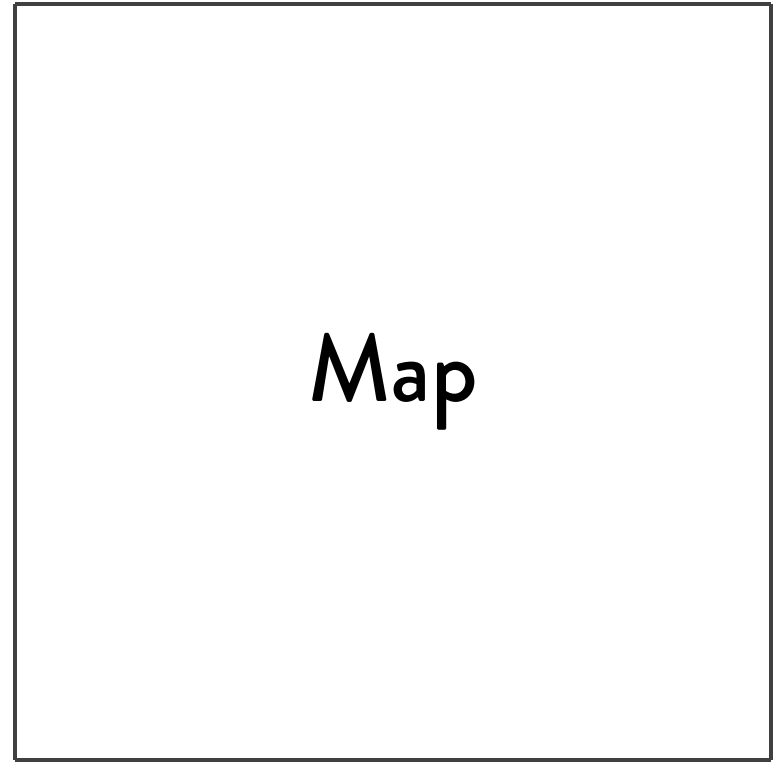
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# The Method

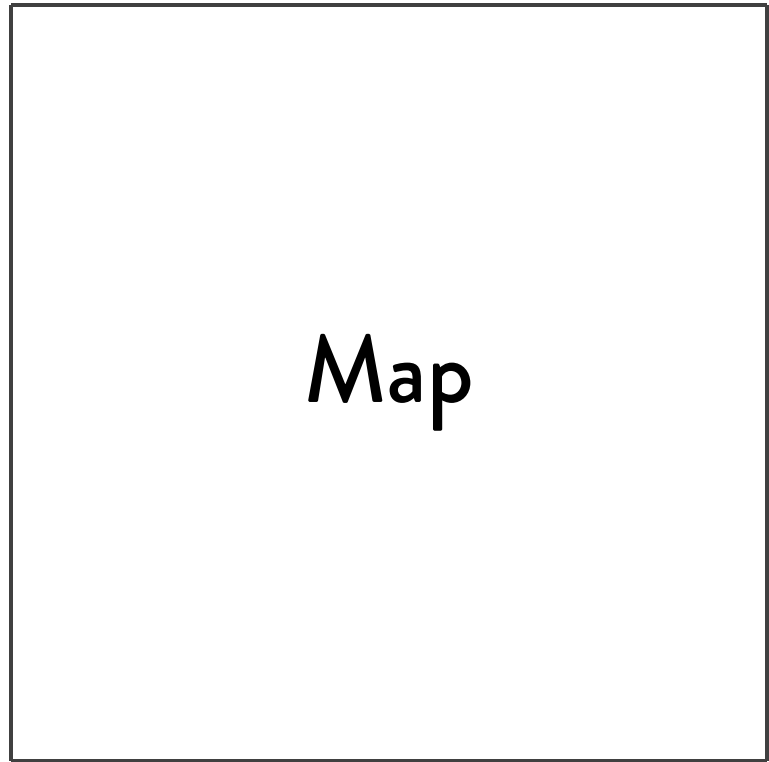
The above, more formally.

# Neighbouring cities



# Neighbouring cities

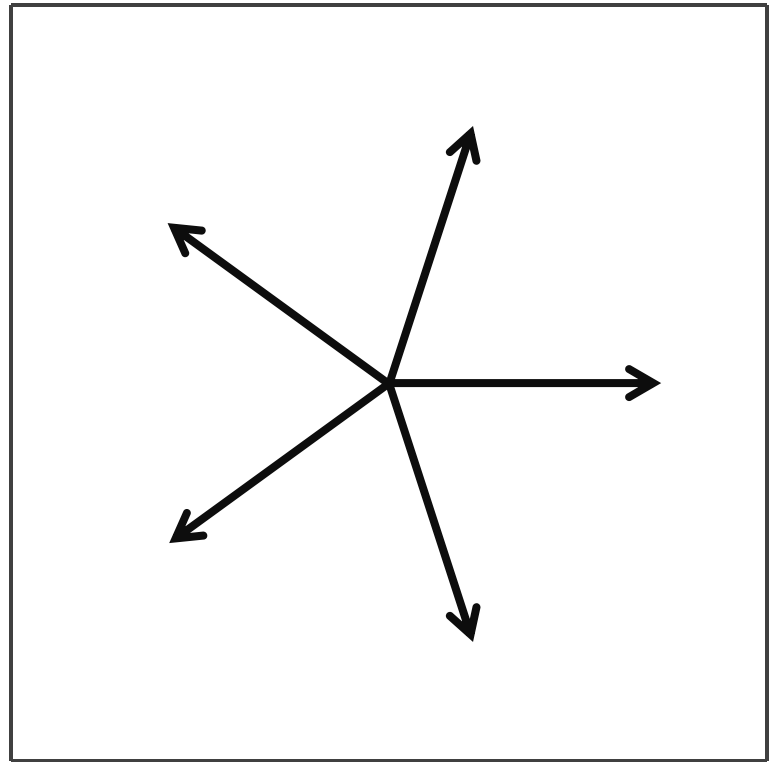
- $N = \#$  Neighboring Cities





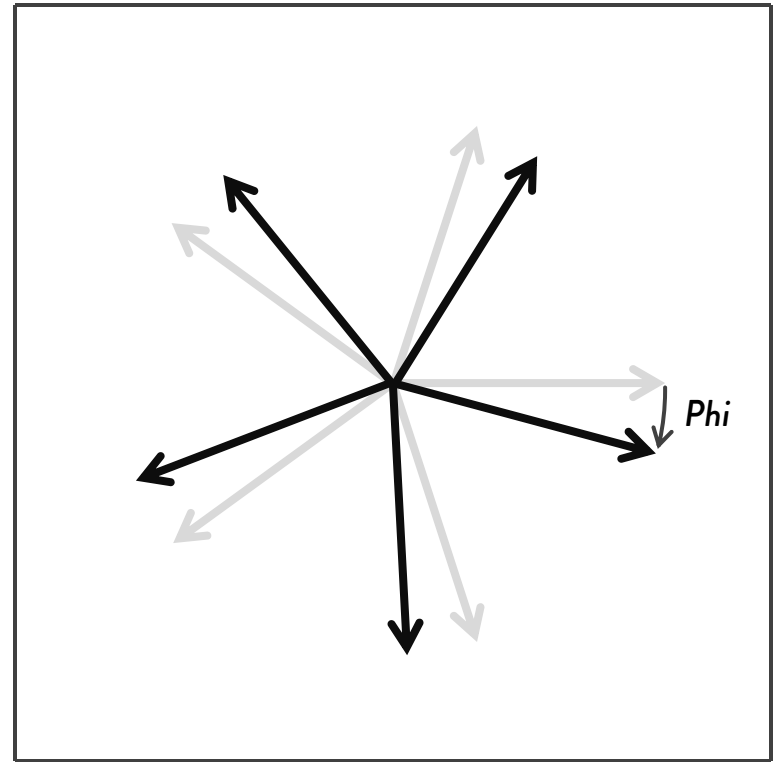
# Neighbouring cities

- $N = \#$  Neighboring Cities
- $N$  equally spaced rays



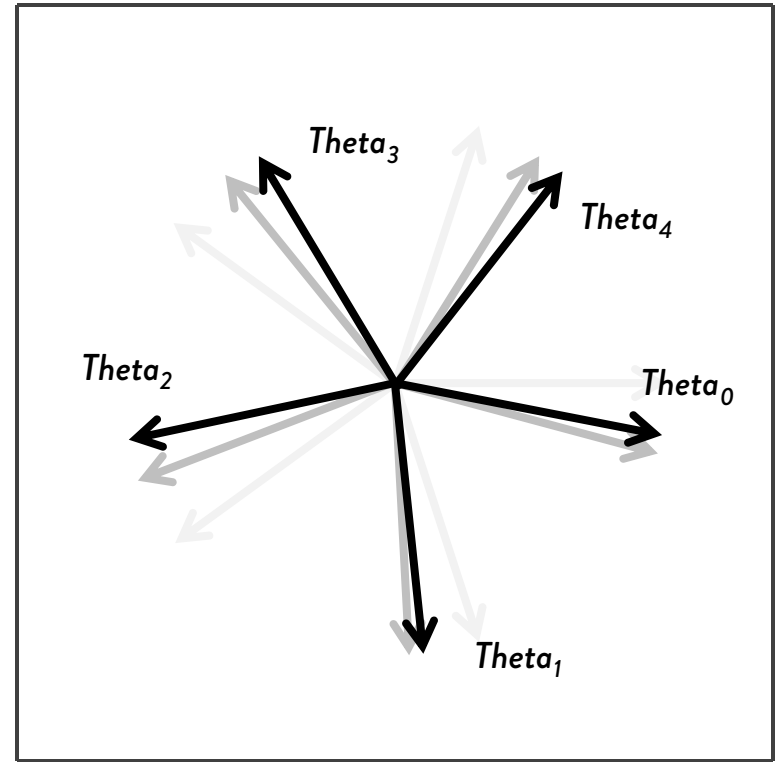
# Neighbouring cities

- $N = \#$  Neighboring Cities
- $N$  equally spaced rays
- Rotate all by  $\Phi$



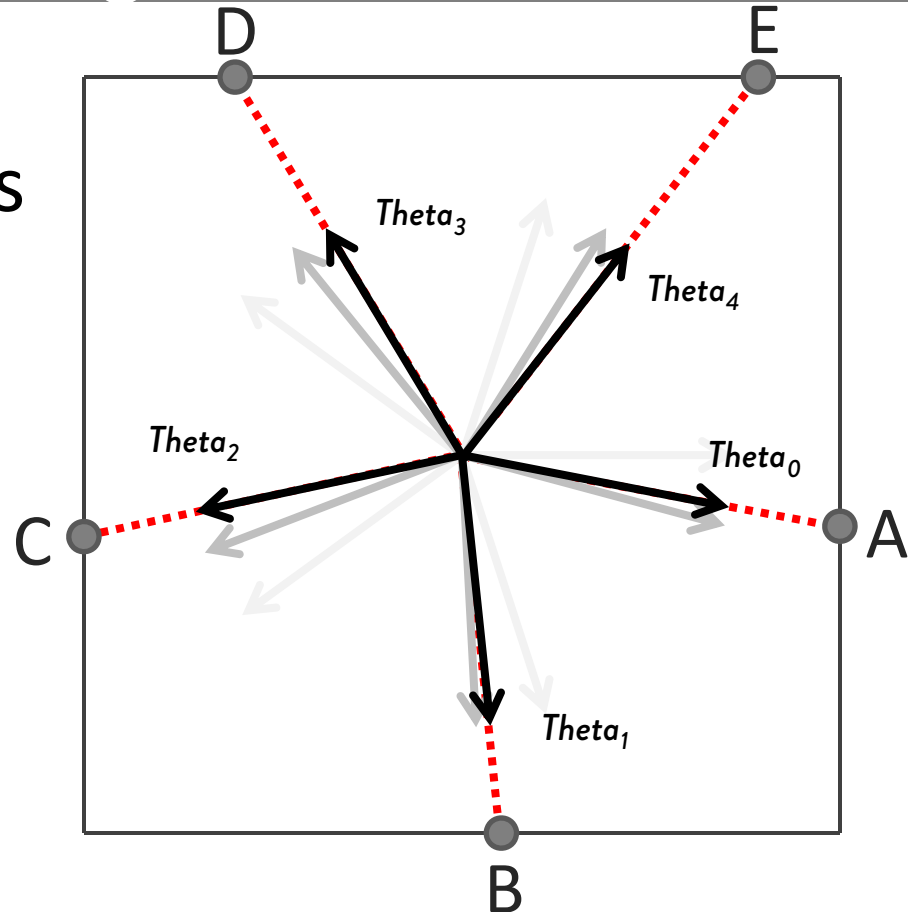
# Neighbouring cities

- $N = \#$  Neighboring Cities
- $N$  equally spaced rays
- Rotate all by  $\Phi$
- Perturb each by  $\Theta_i$

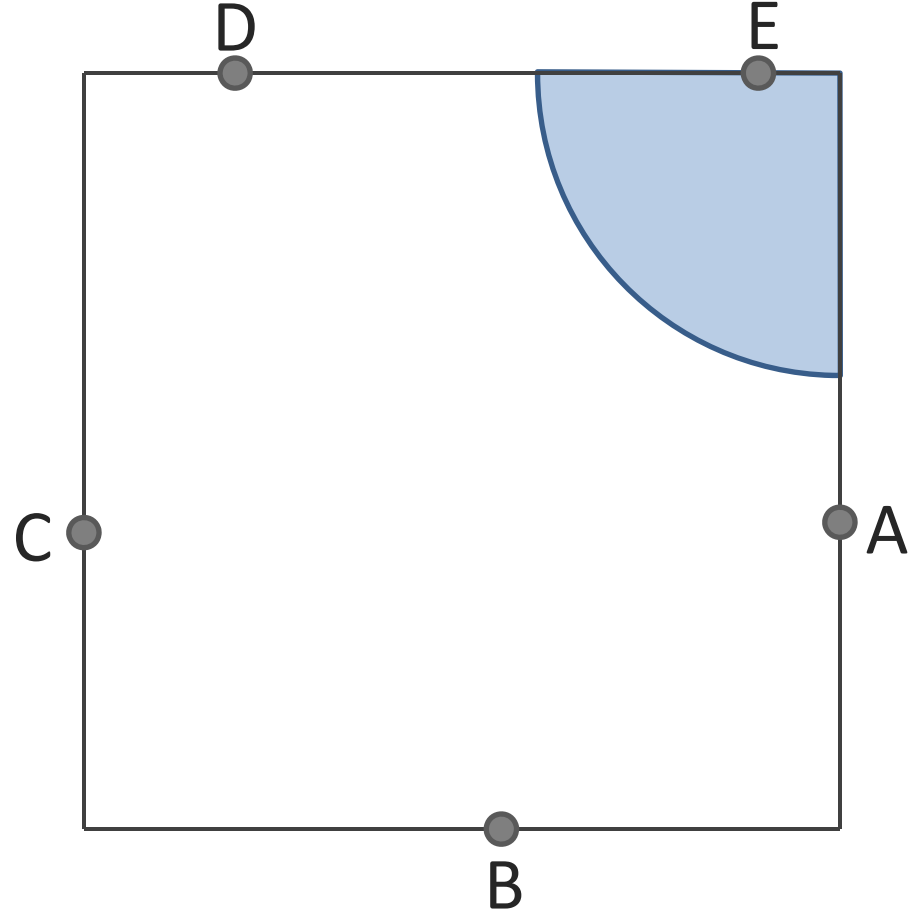


# Neighbouring cities

- $N = \#$  Neighboring Cities
- $N$  equally spaced rays
- Rotate all by  $\Phi$
- Perturb each by  $\Theta_i$
- Intersect the border

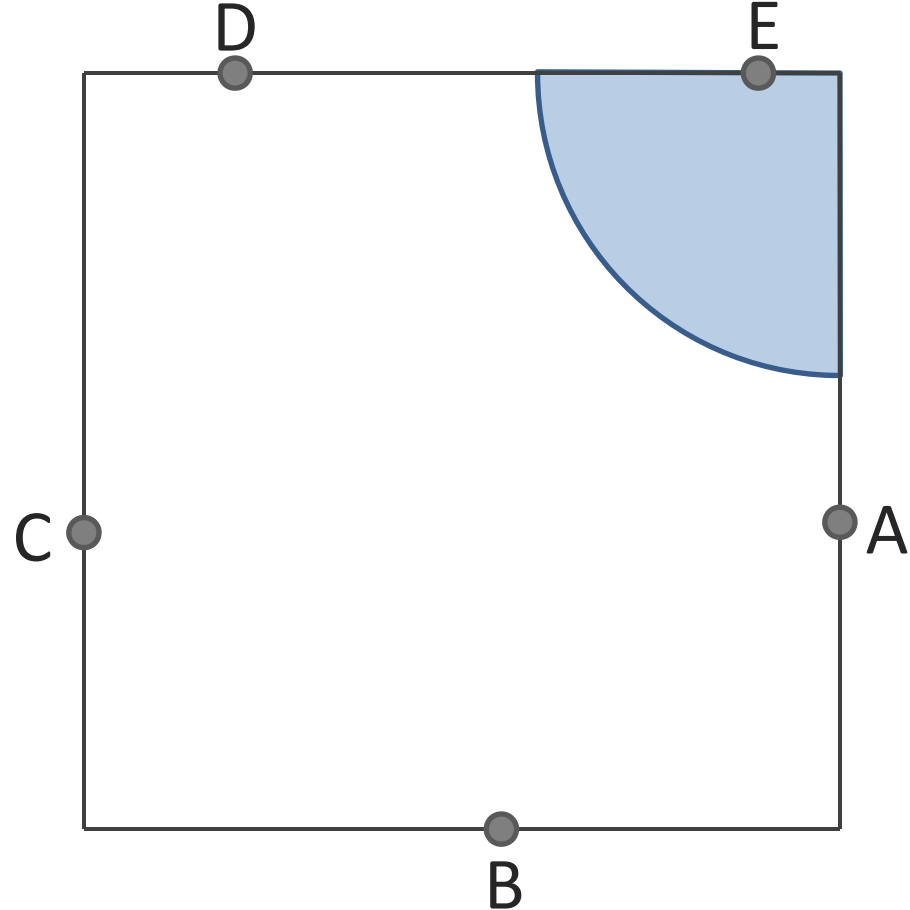


# Initial Road Network



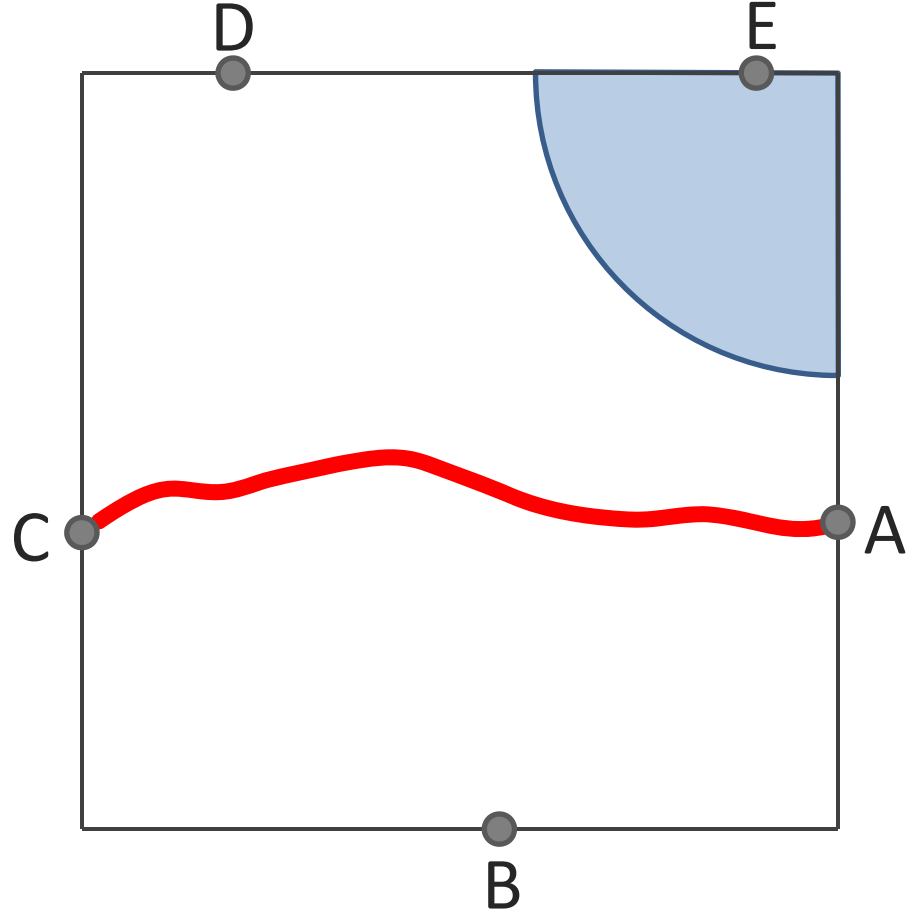
# Initial Road Network

- Connect opposite cities



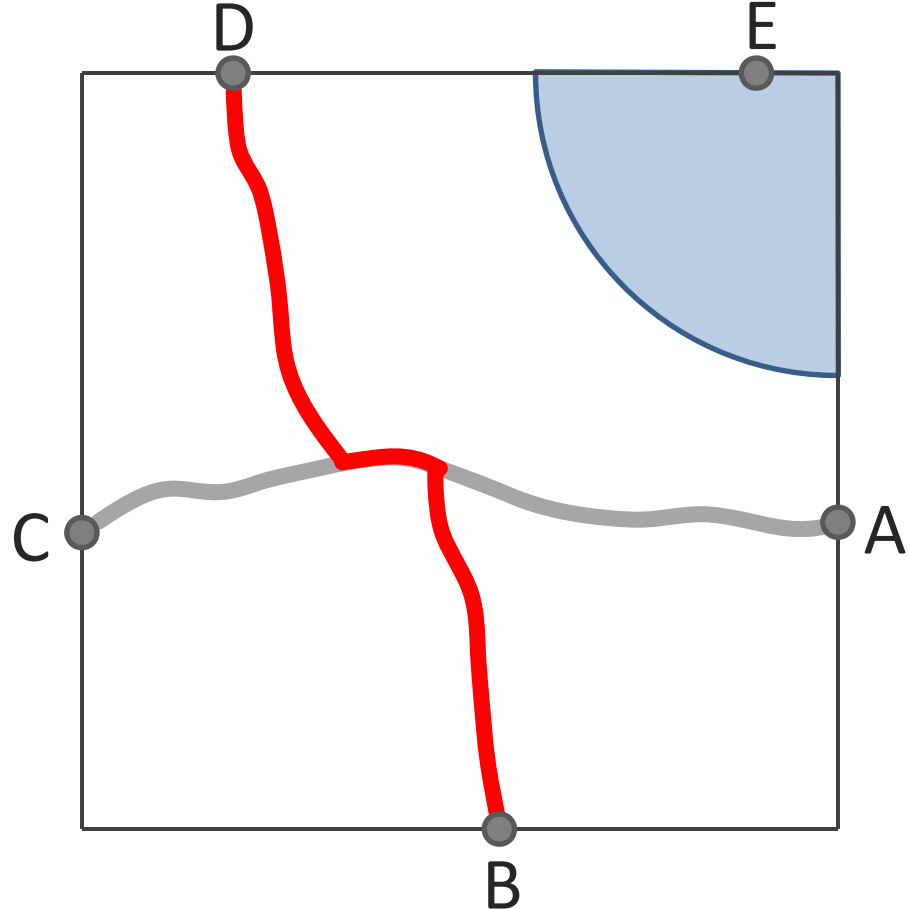
# Initial Road Network

- Connect opposite cities
  1. AC



# Initial Road Network

- Connect opposite cities
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  2. BD

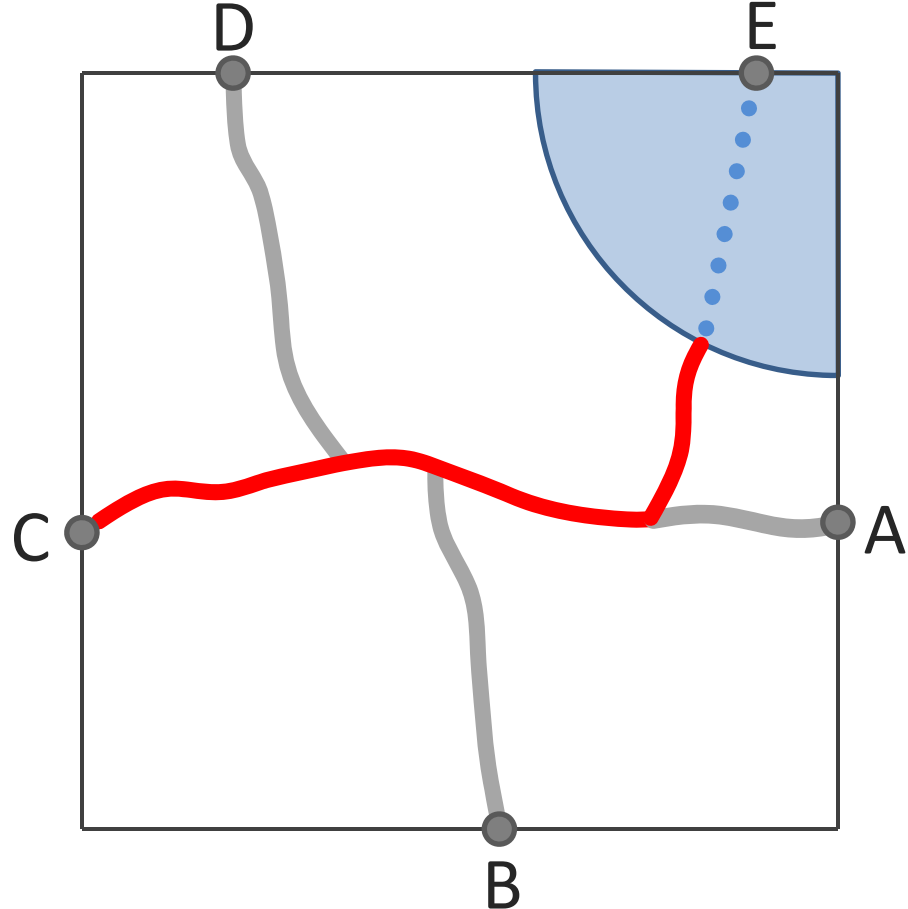




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- Connect opposite cities

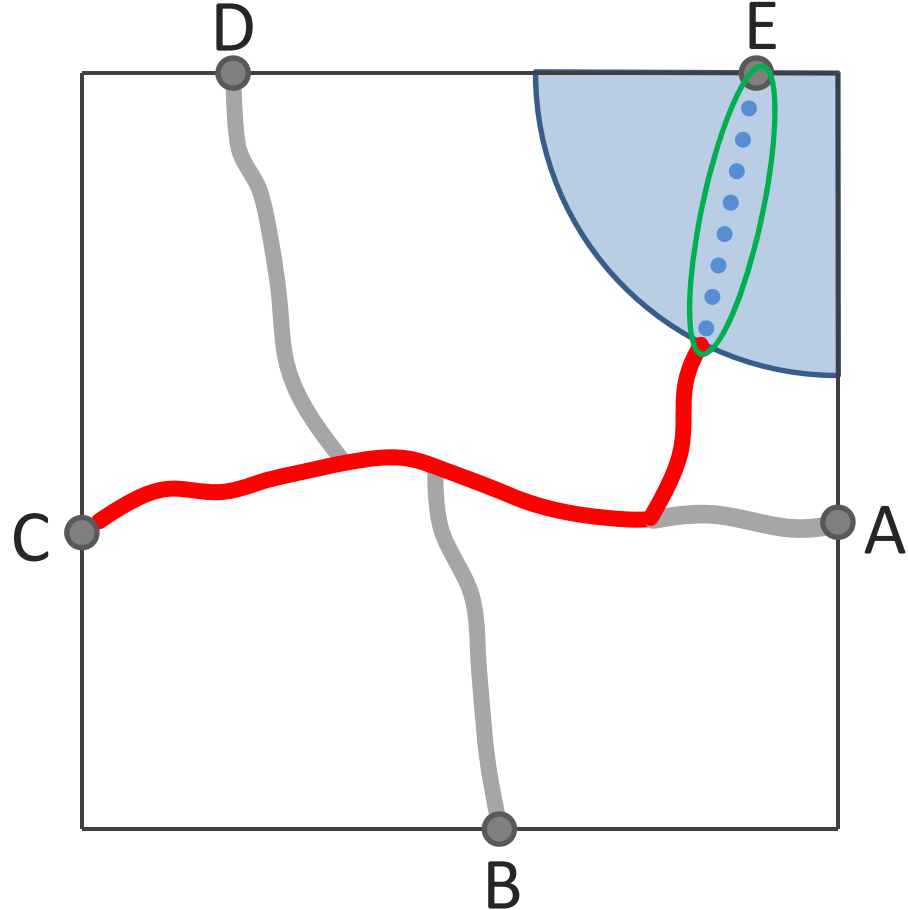
1. AC
2. BD
3. CE



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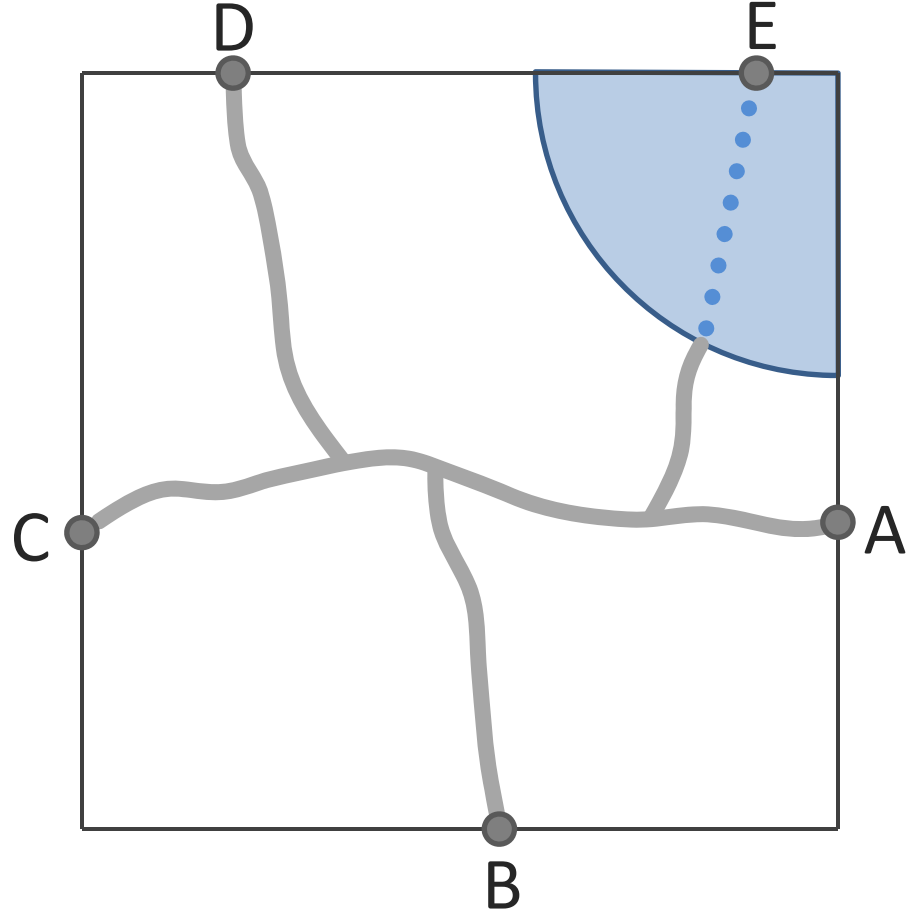
- Connect opposite cities

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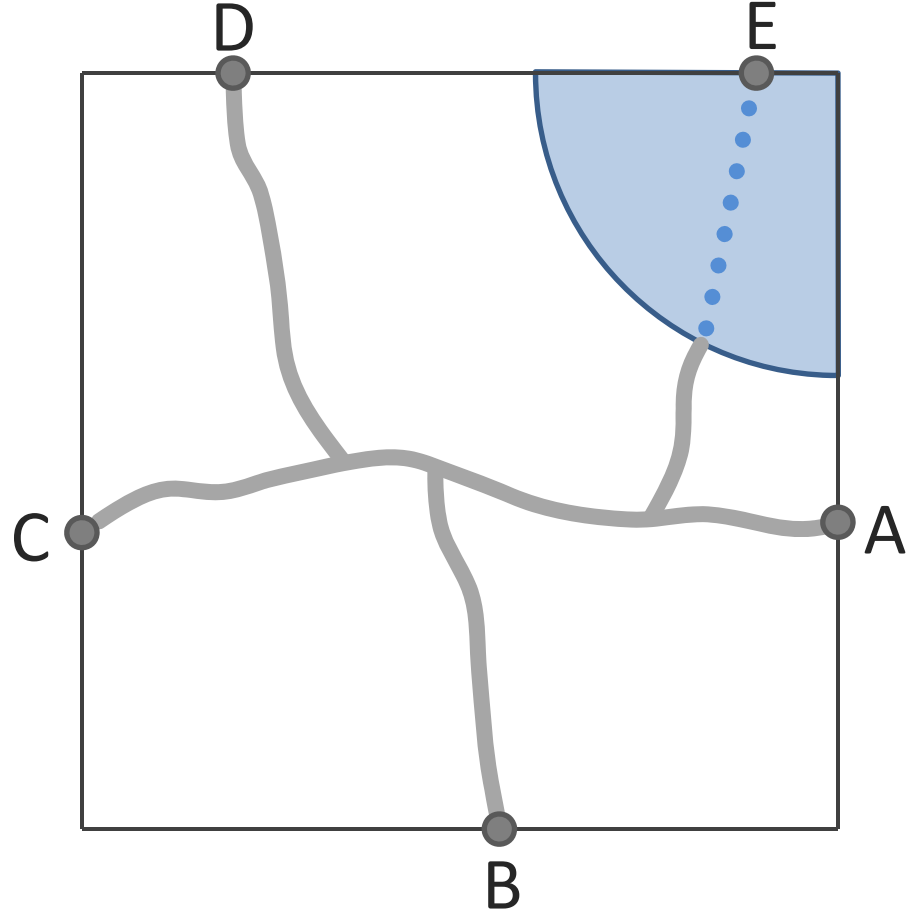
# Initial Road Network

- Connect opposite cities
  1. AC
  2. BD
  3. CE
- Until all are connected



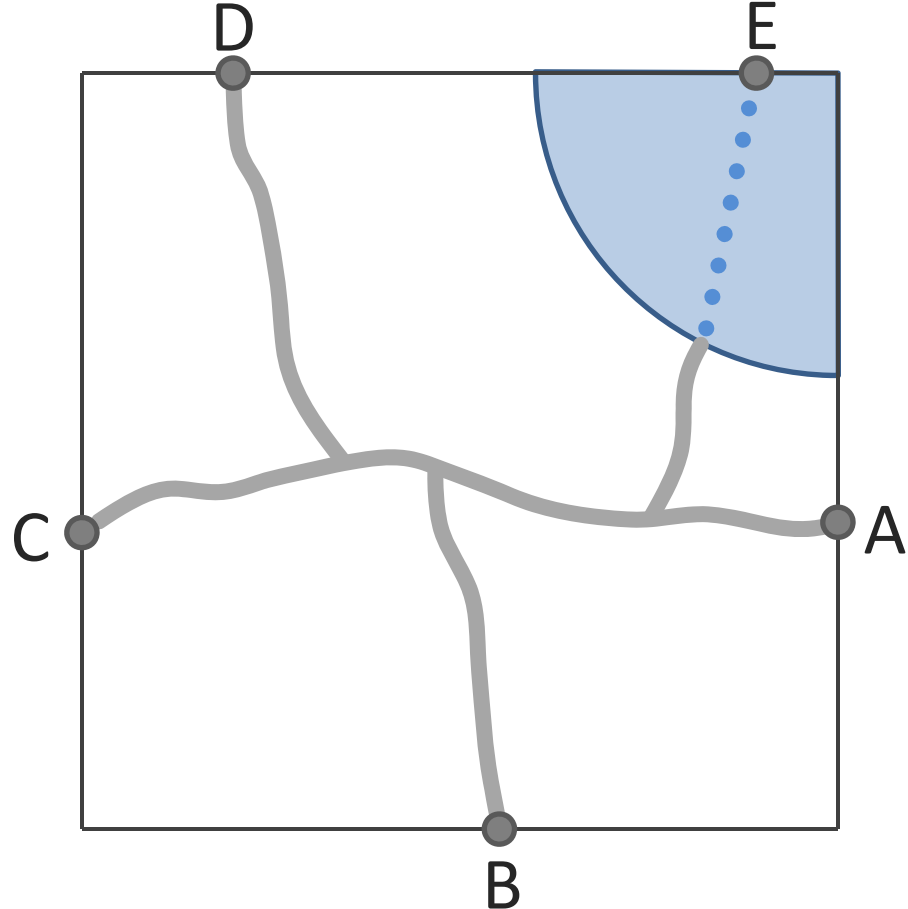
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- Connect opposite cities
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- Until all are connected
- Variations



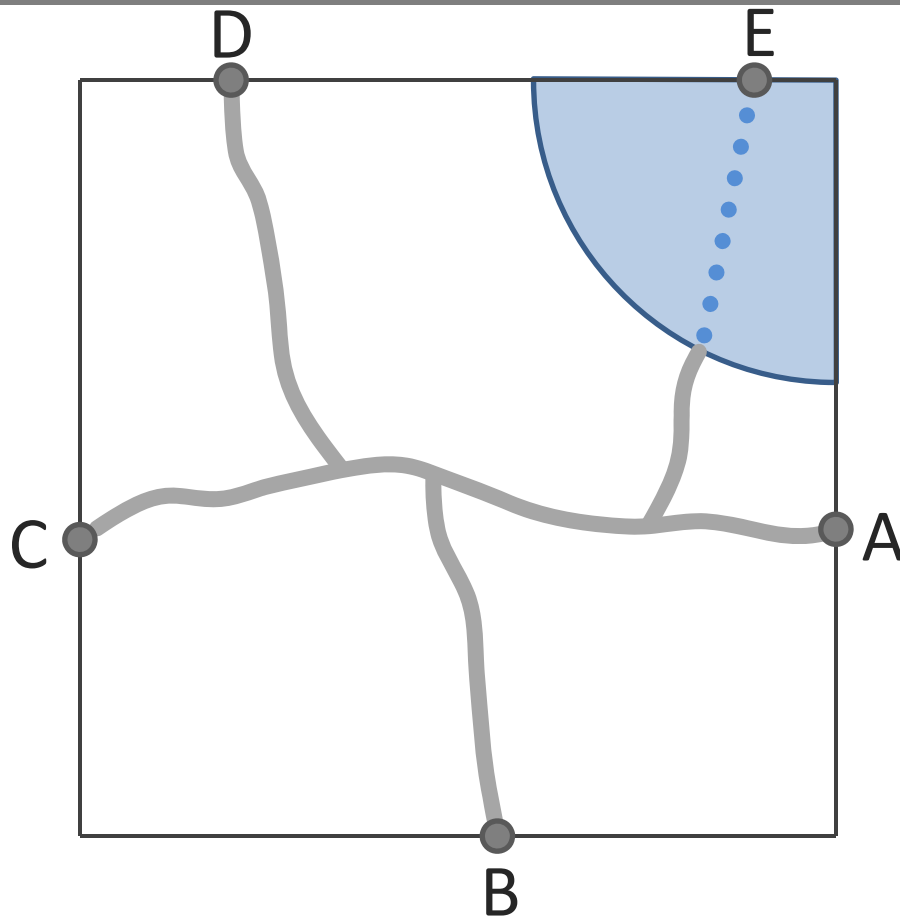
# Initial Road Network

- Connect opposite cities
  1. AC
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- Until all are connected
- Variations
  - Relax the term “opposite”

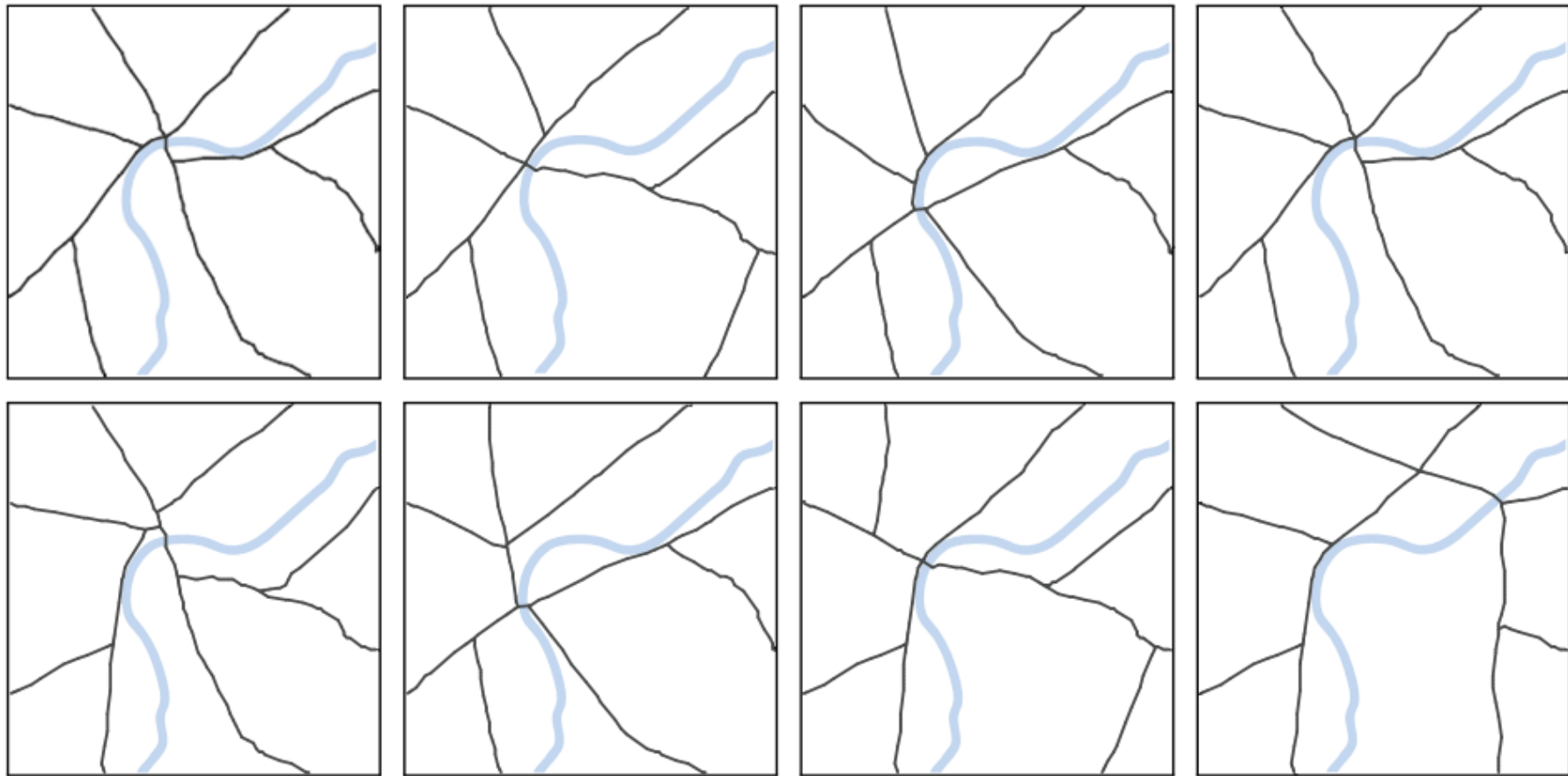


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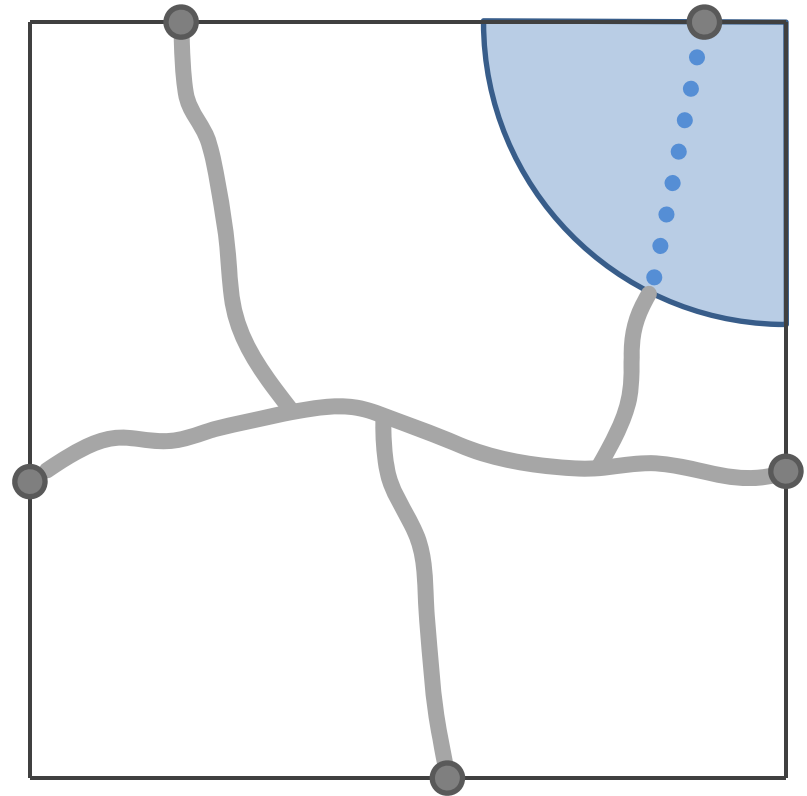
- Connect opposite cities
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  2. BD
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- Until all are connected
- Variations
  - Relax the term “opposite”
  - Shuffle the order



# Initial Road Network



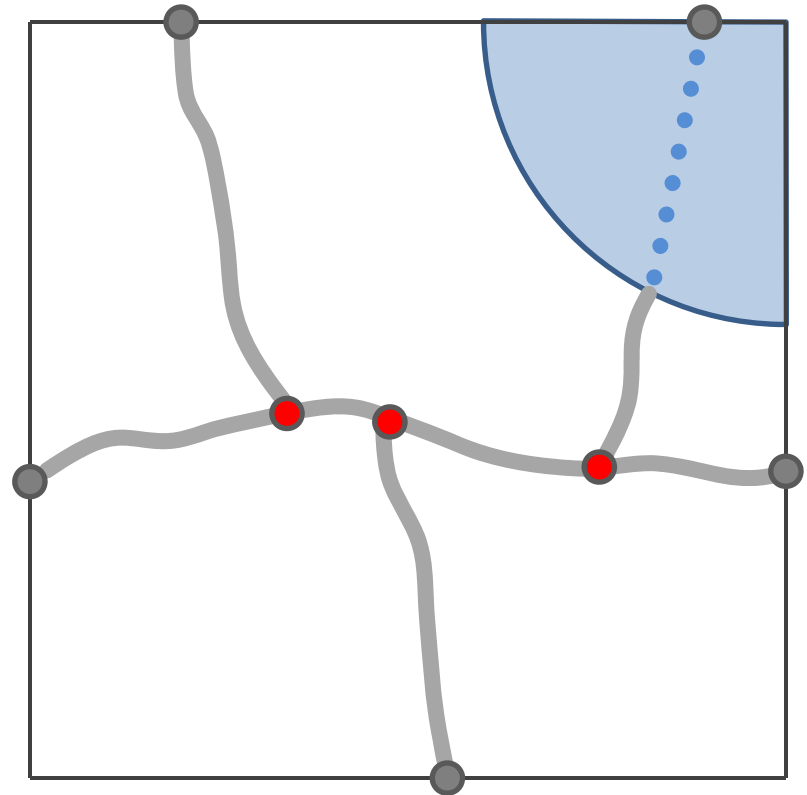
# Nuclei of Growth





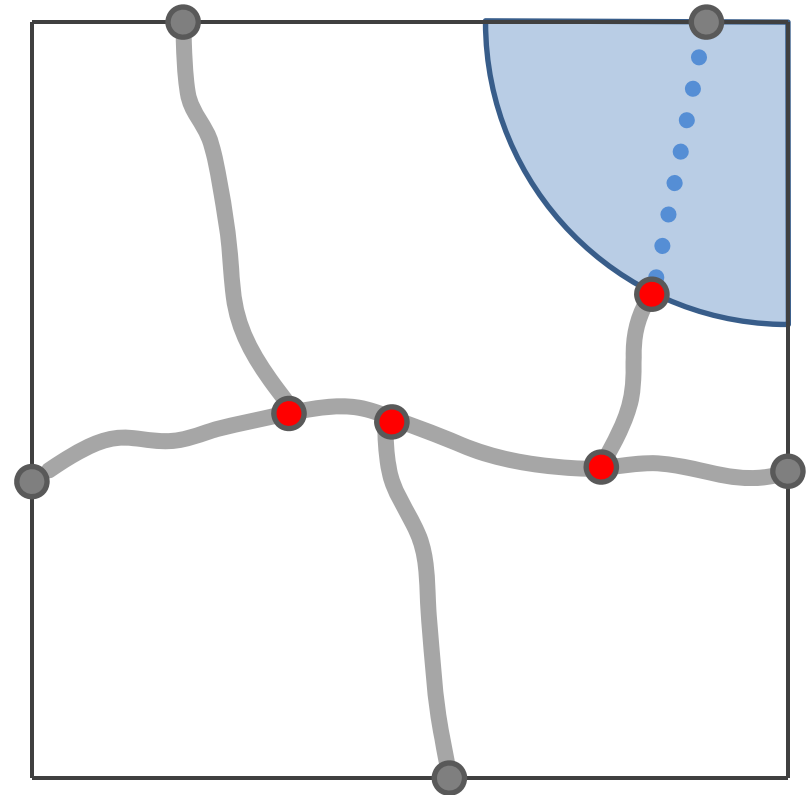
# Nuclei of Growth

- Major road intersections



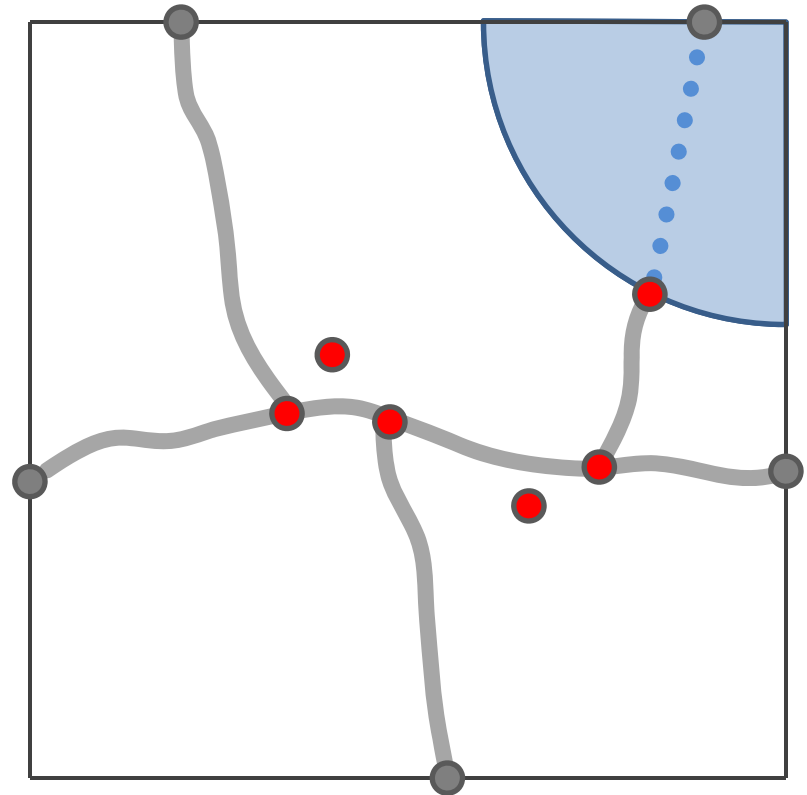
# Nuclei of Growth

- Major road intersections
- Ports



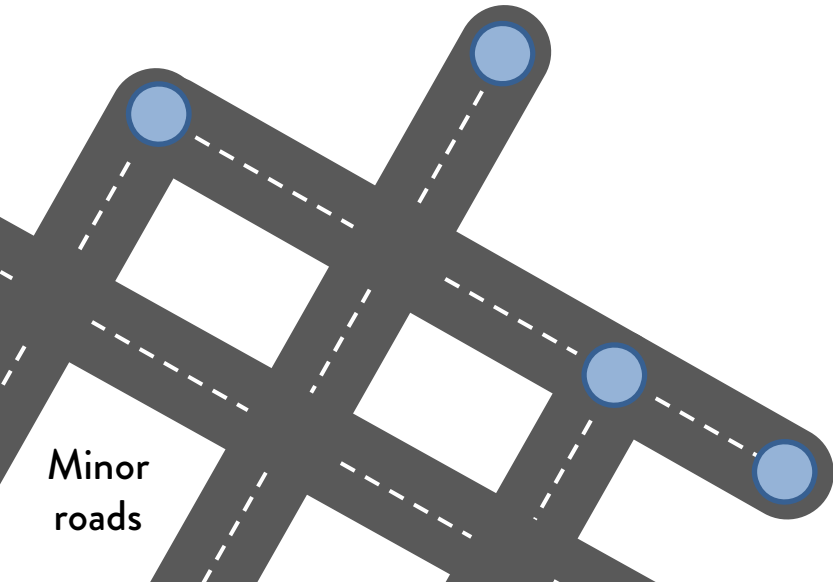
# Nuclei of Growth

- Major road intersections
- Ports
- Near existing nuclei



# Minor Roads

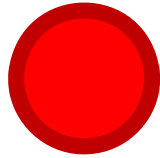
- Intersections 



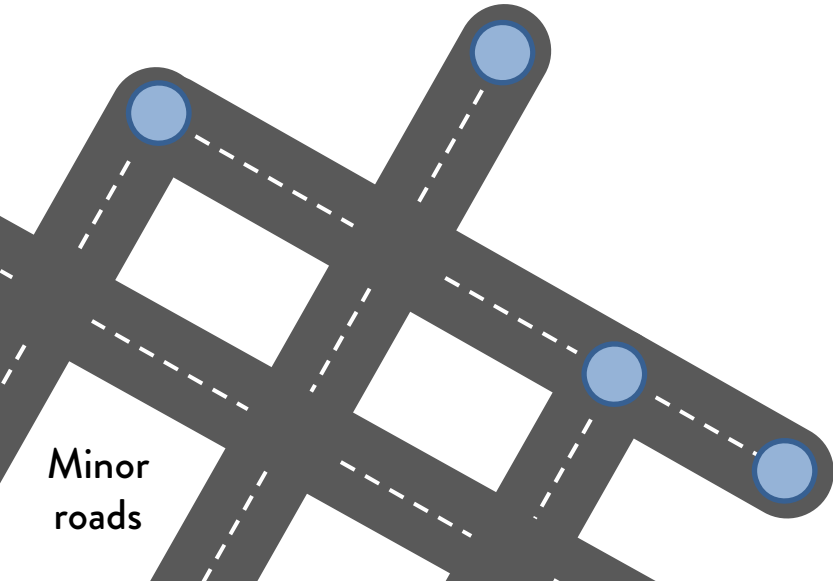
Minor  
roads

# Minor Roads

Nucleus of growth



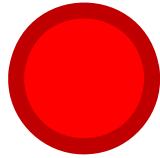
- Intersections 
- Nuclei of growth




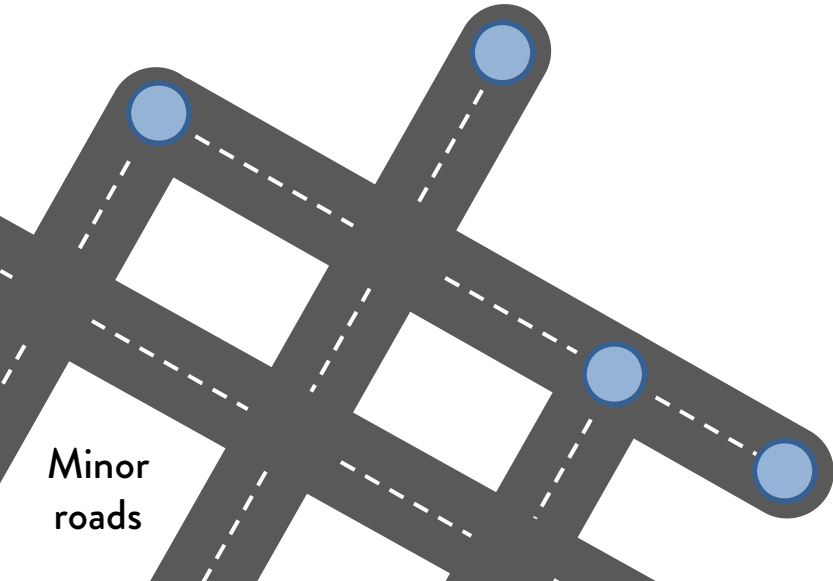
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# Minor Roads

Nucleus of growth

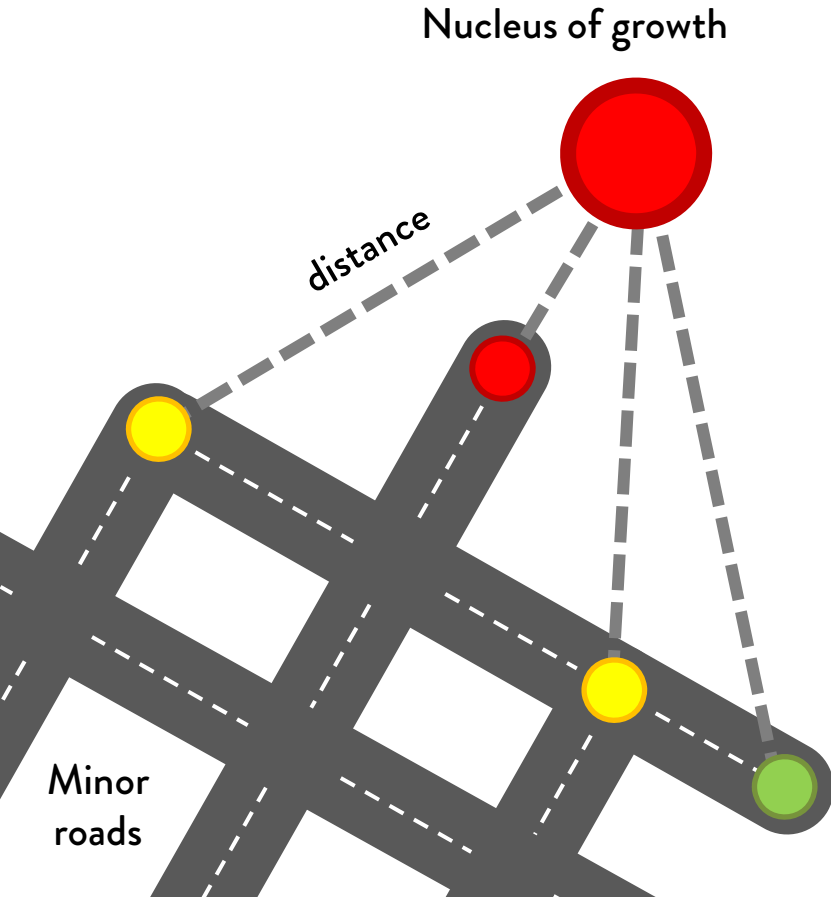


- Intersections 
- Nuclei of growth
- Choose  $N$  intersections?
  - $N \in$  “*Historical context*”



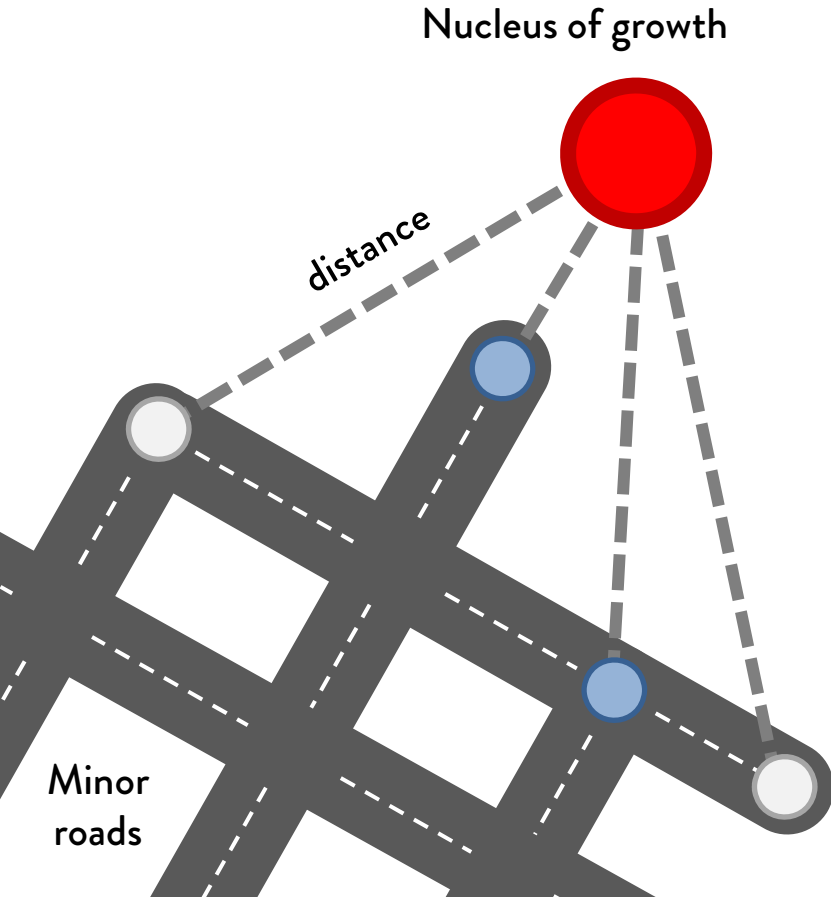
Minor  
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# Minor Roads



- Intersections ●
- Nuclei of growth
- Choose  $N$  intersections?
  - $N \in$  “*Historical context*”
- Closer = more probable

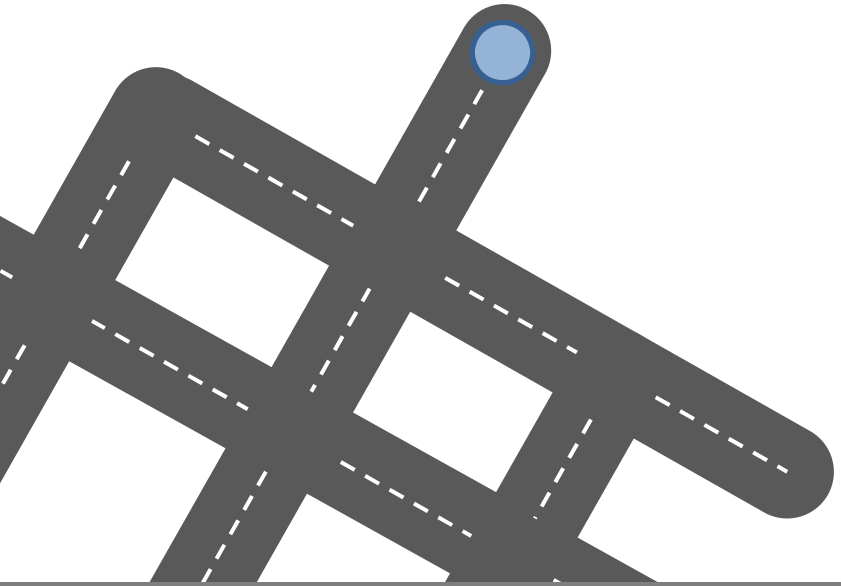
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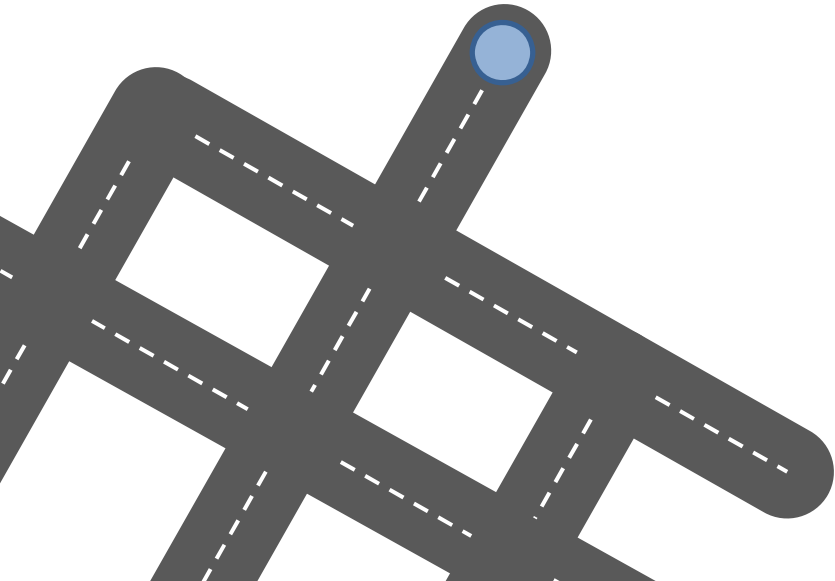


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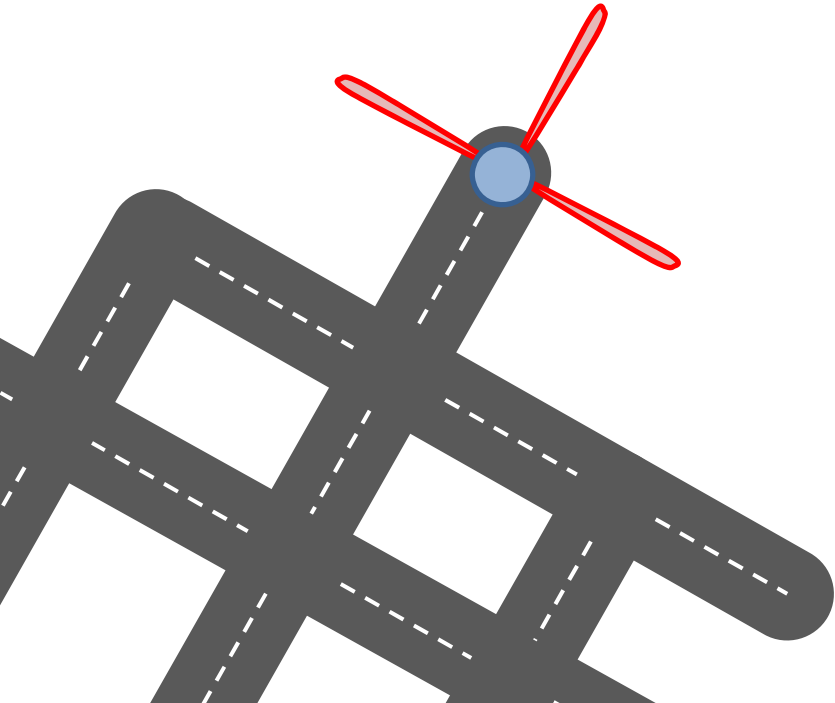
# Minor Roads

- Similar to [Muller01] and [Weber09]



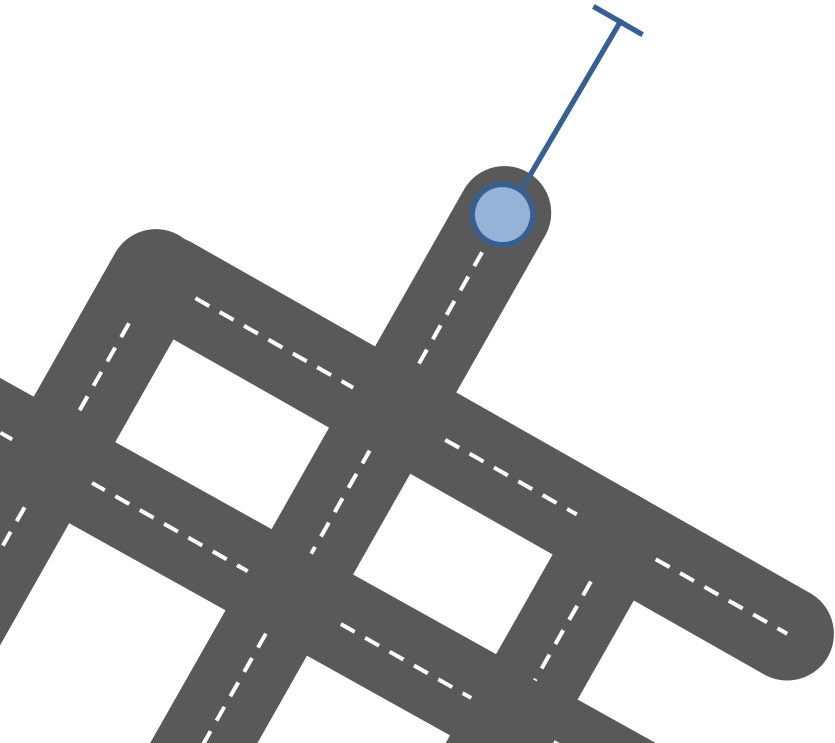
# Minor Roads

- Similar to [Muller01] and [Weber09]



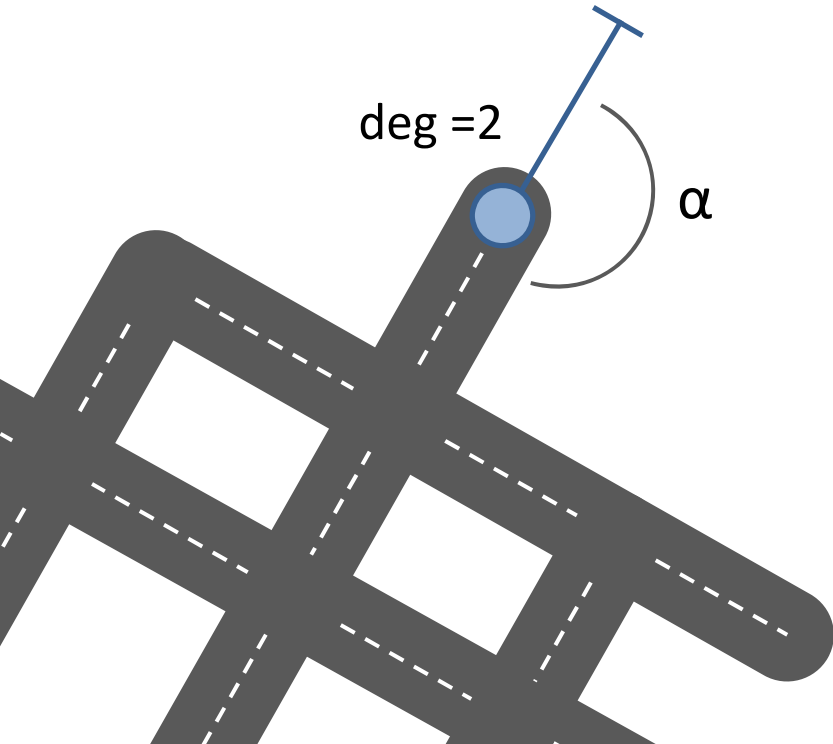
# Minor Roads

- Similar to [Muller01] and [Weber09]



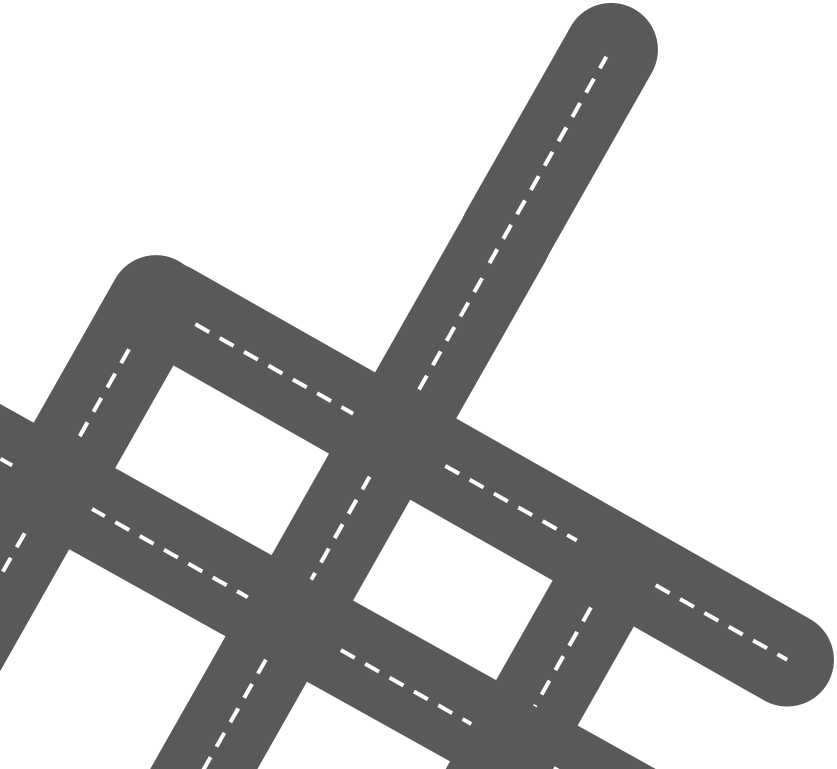
# Minor Roads

- Similar to [Muller01] and [Weber09]
- Constraints



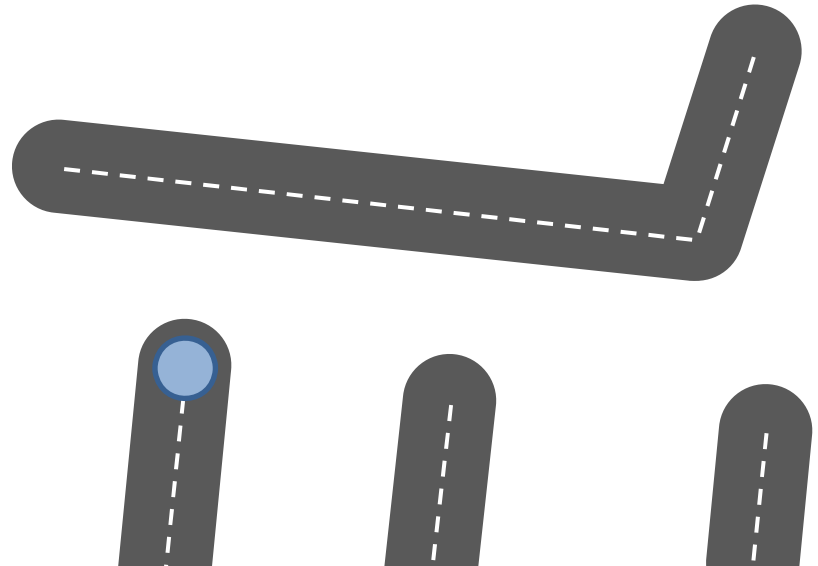
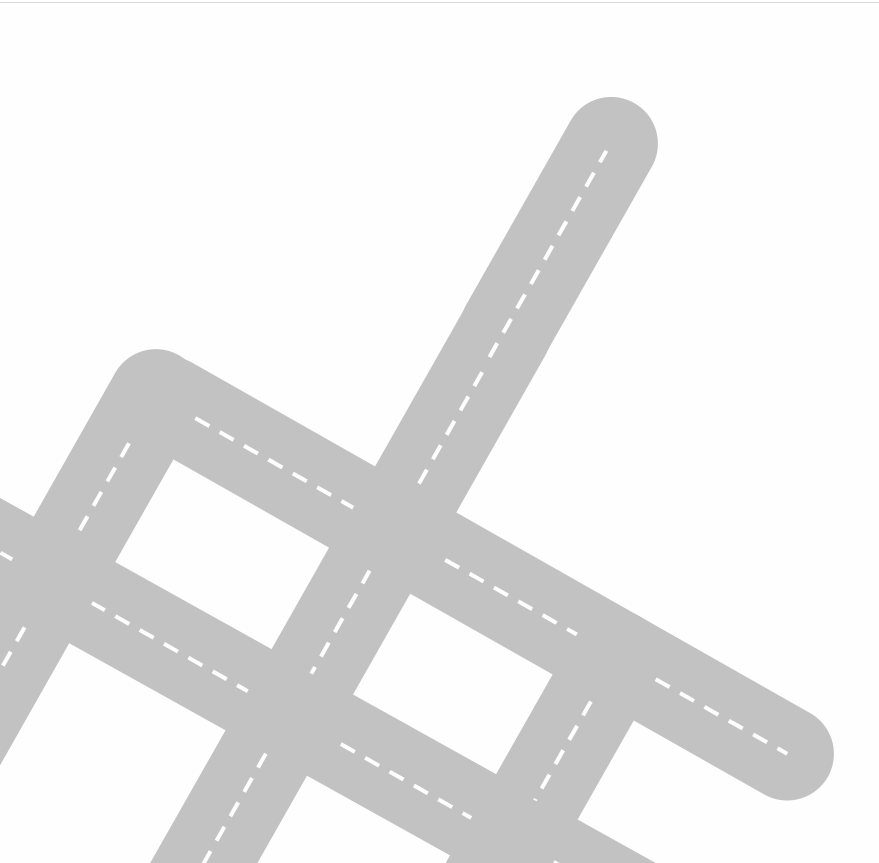
# Minor Roads

- Similar to [Muller01] and [Weber09]
- Constraints



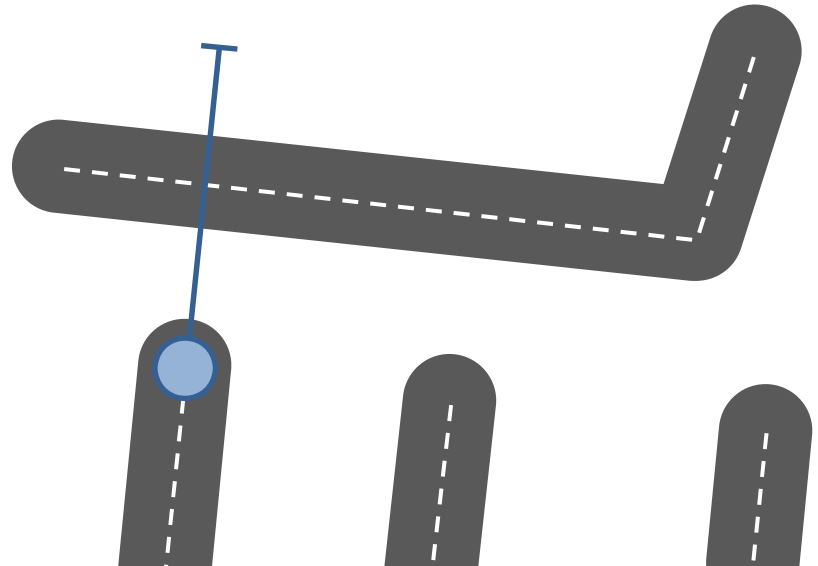
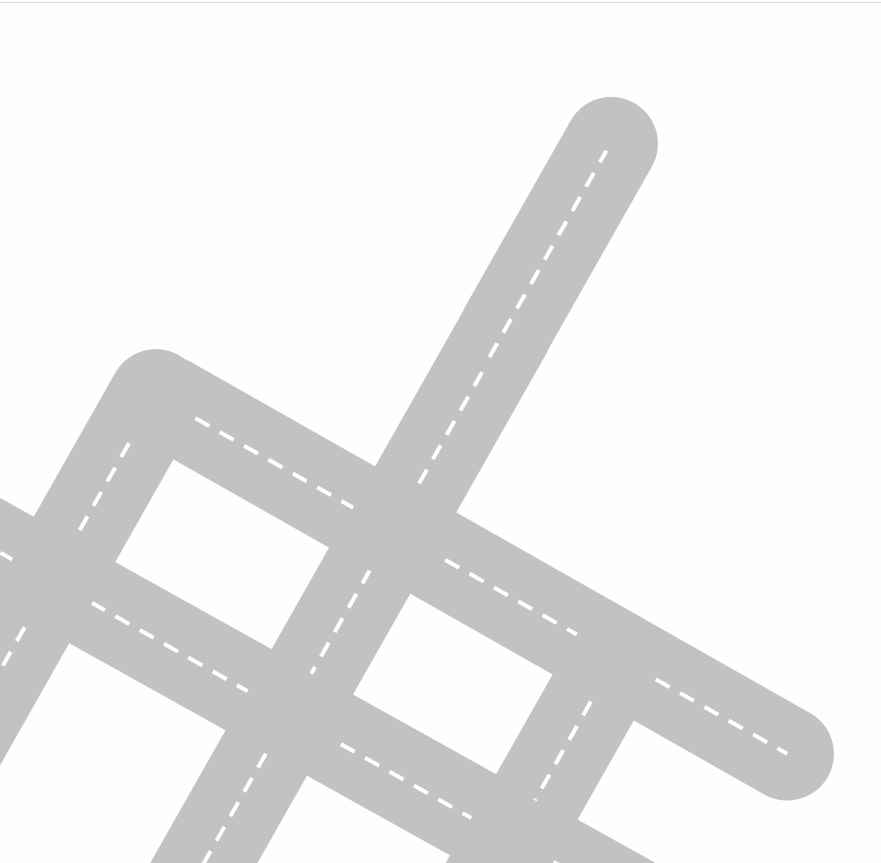
# Minor Roads

- Similar to [Muller01] and [Weber09]
- Constraints
- Good fit



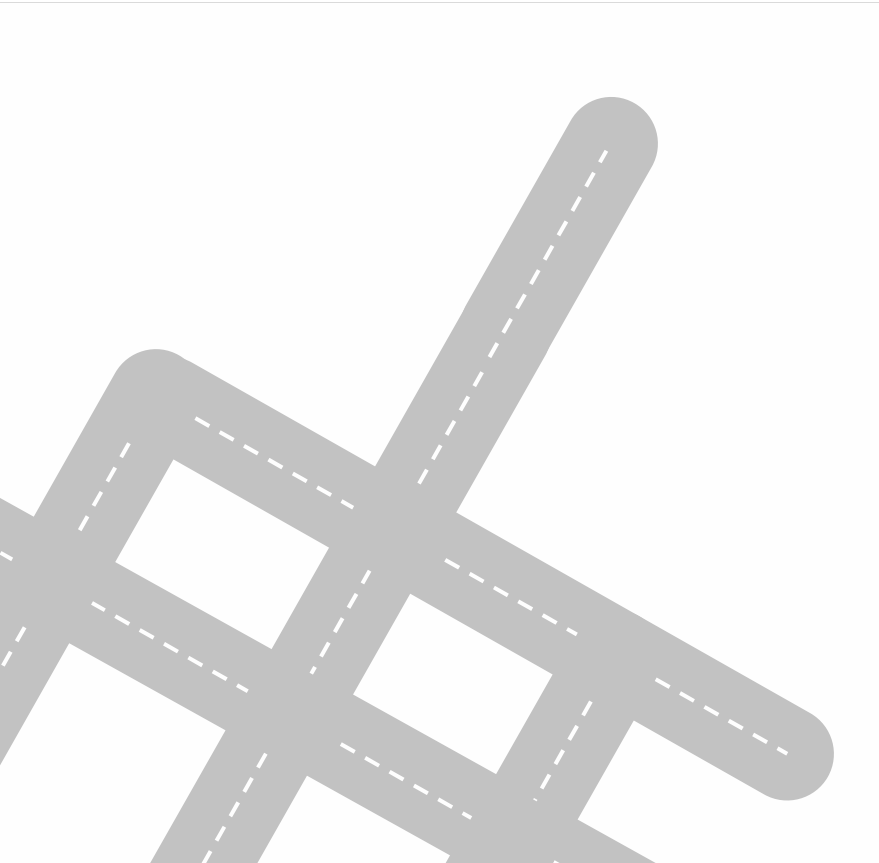
# Minor Roads

- Similar to [Muller01] and [Weber09]
- Constraints
- Good fit

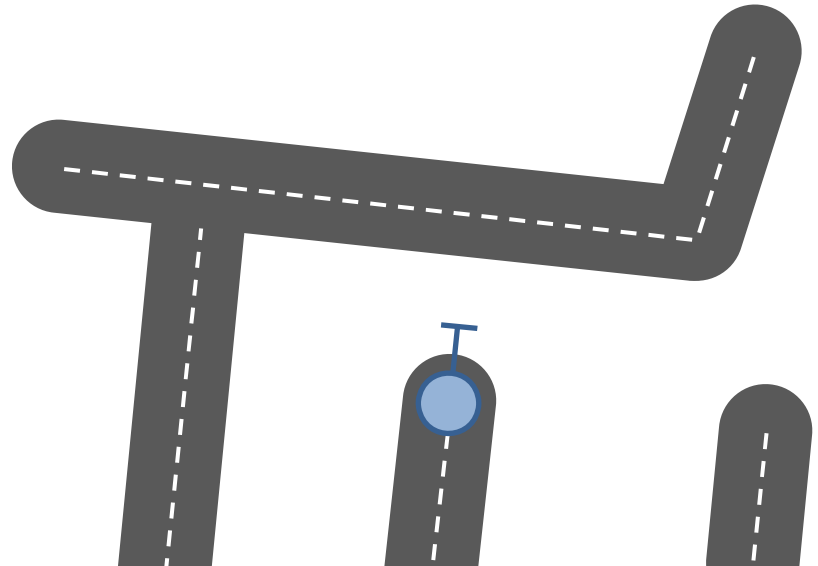




# Minor Roads

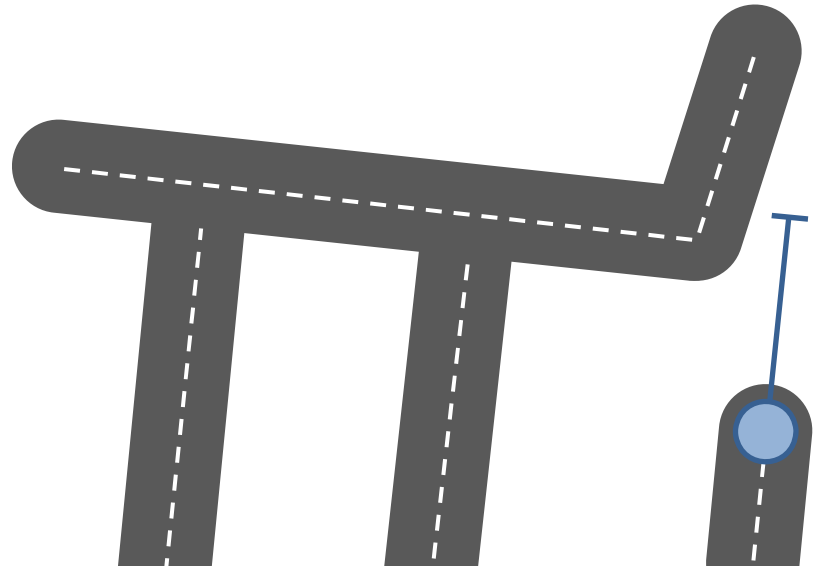
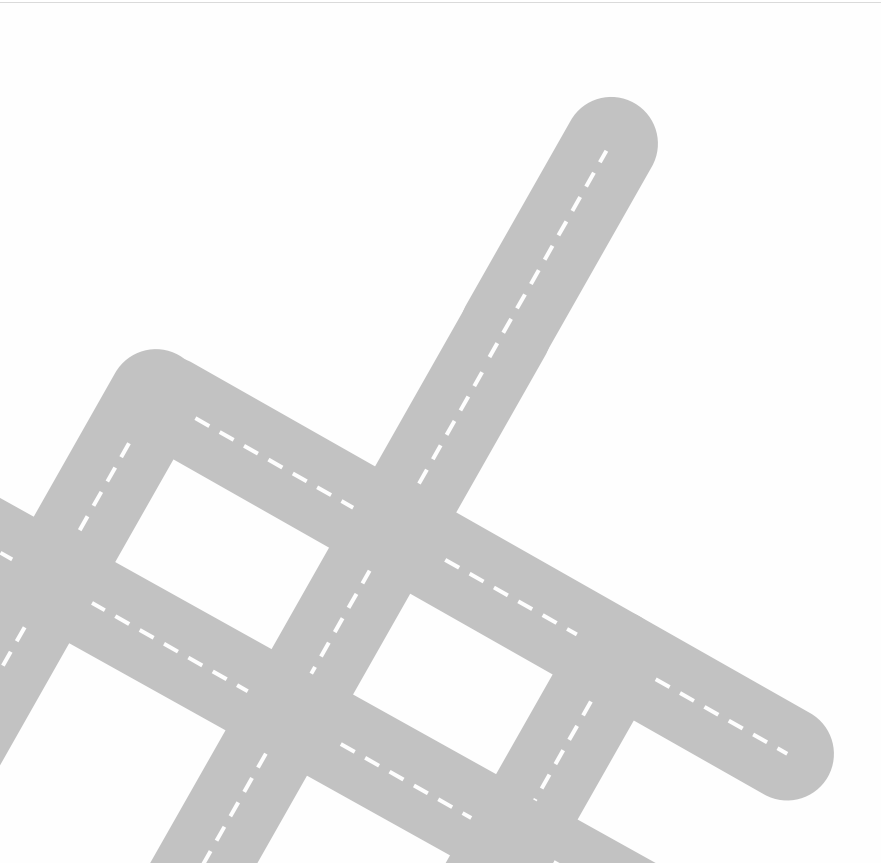


- Similar to [Muller01] and [Weber09]
- Constraints
- Good fit

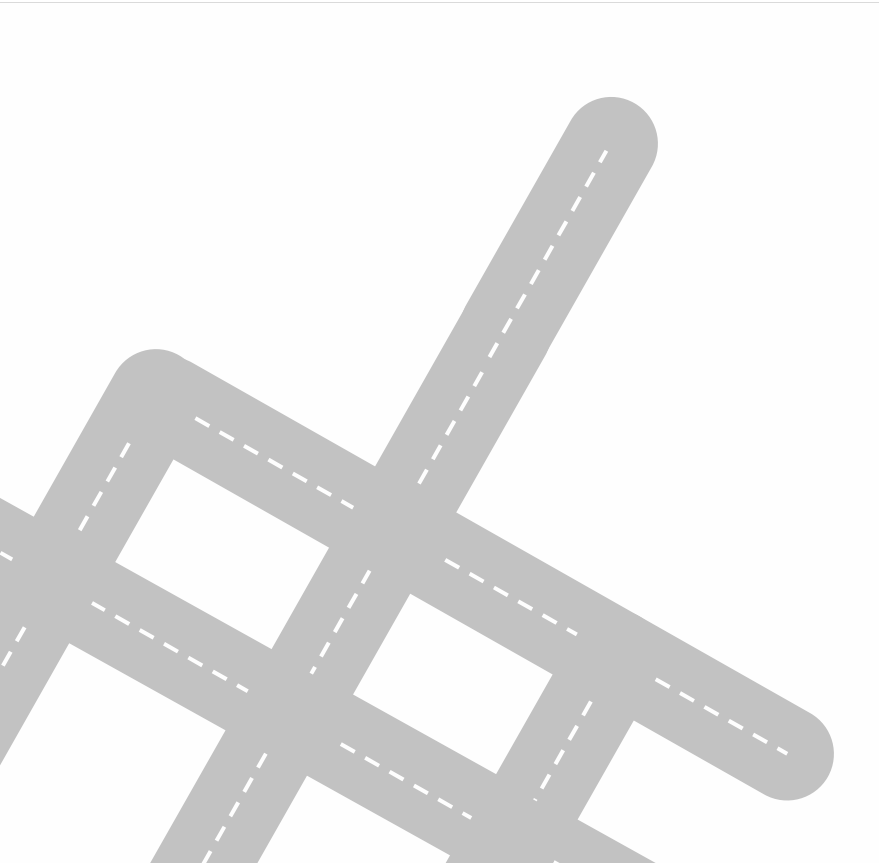


# Minor Roads

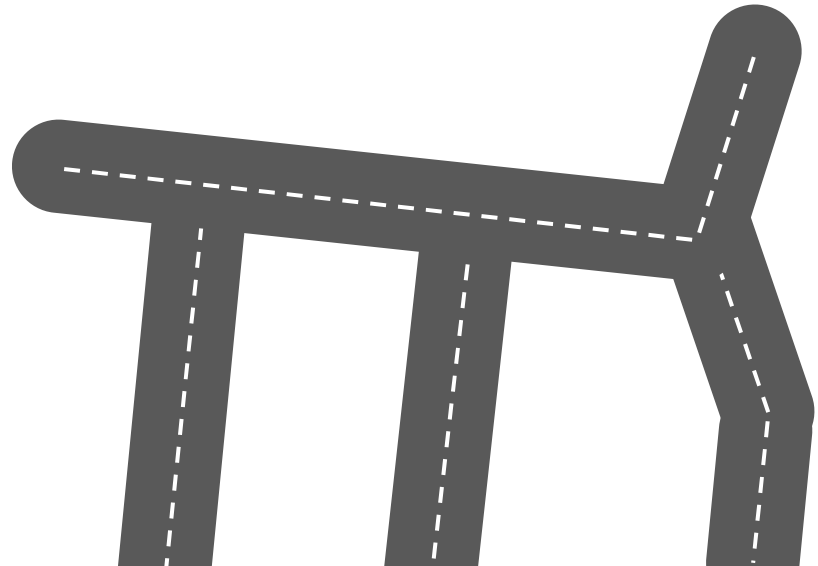
- Similar to [Muller01] and [Weber09]
- Constraints
- Good fit



# Minor Roads

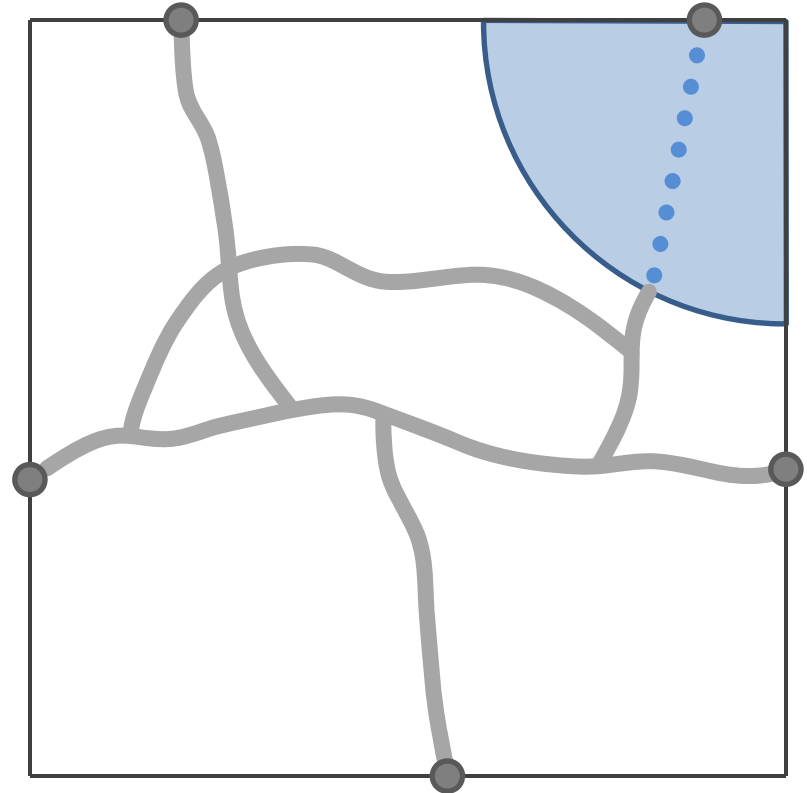


- Similar to [Muller01] and [Weber09]
- Constraints
- Good fit



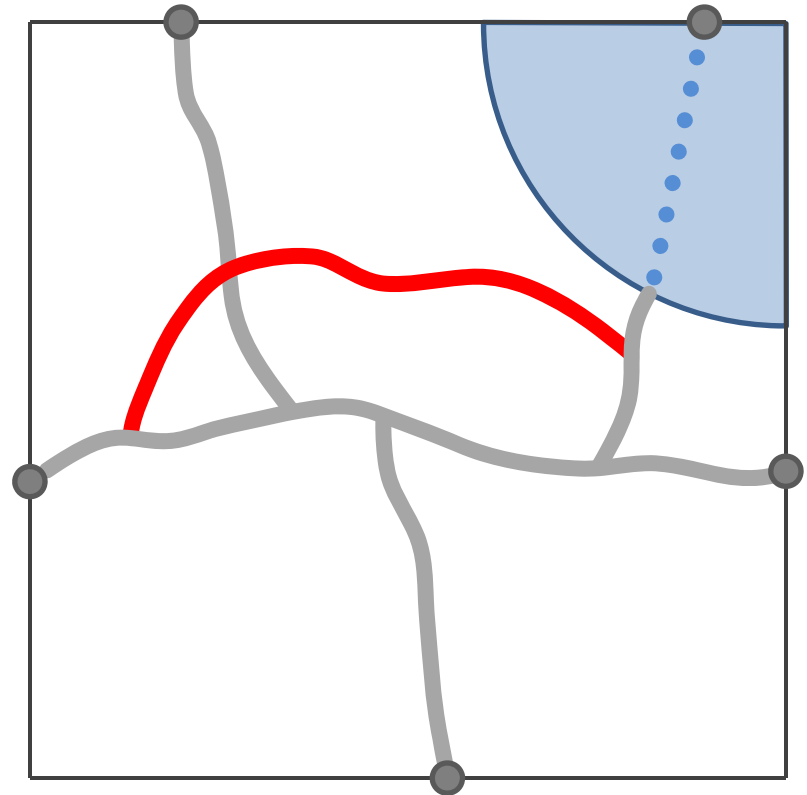
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities



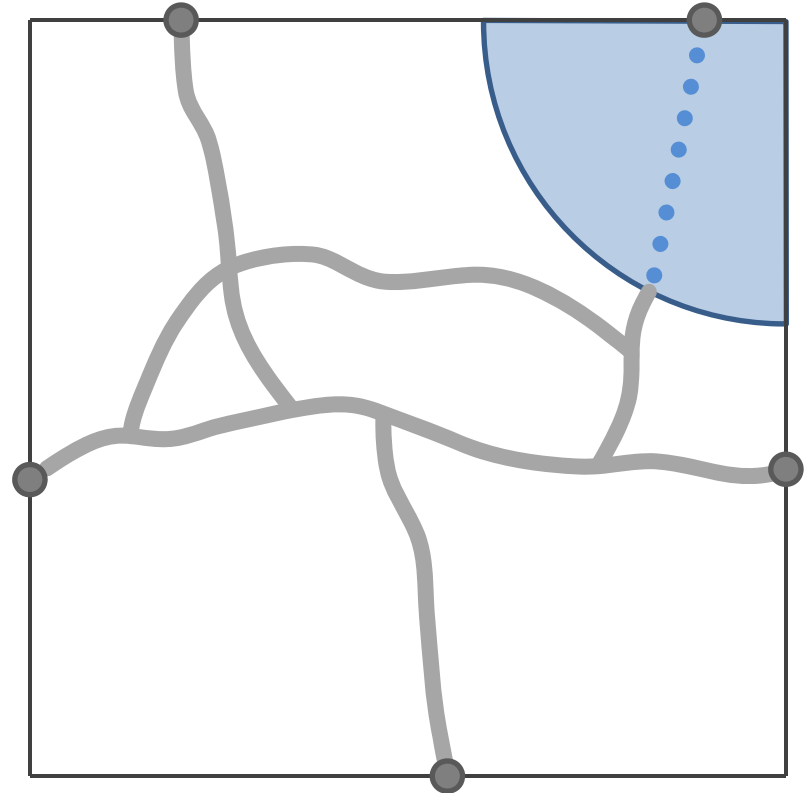
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities



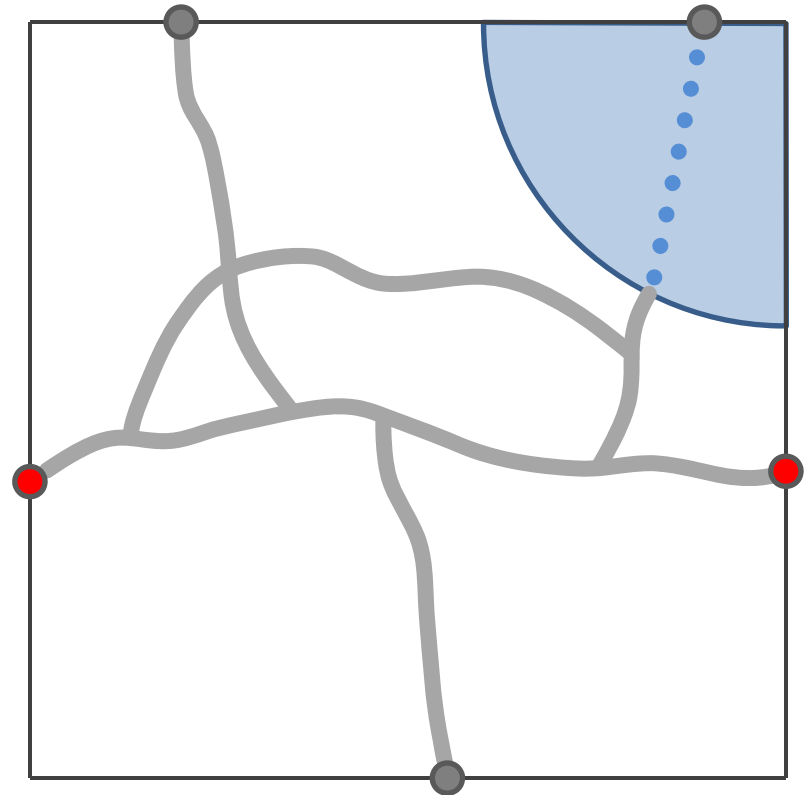
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities



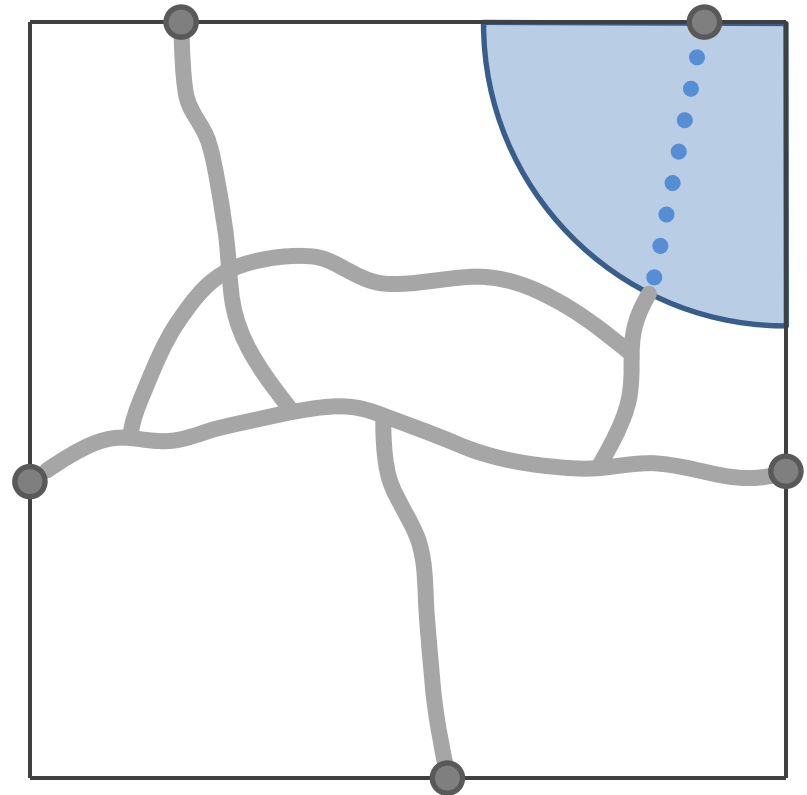
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities



# Trade Simulation

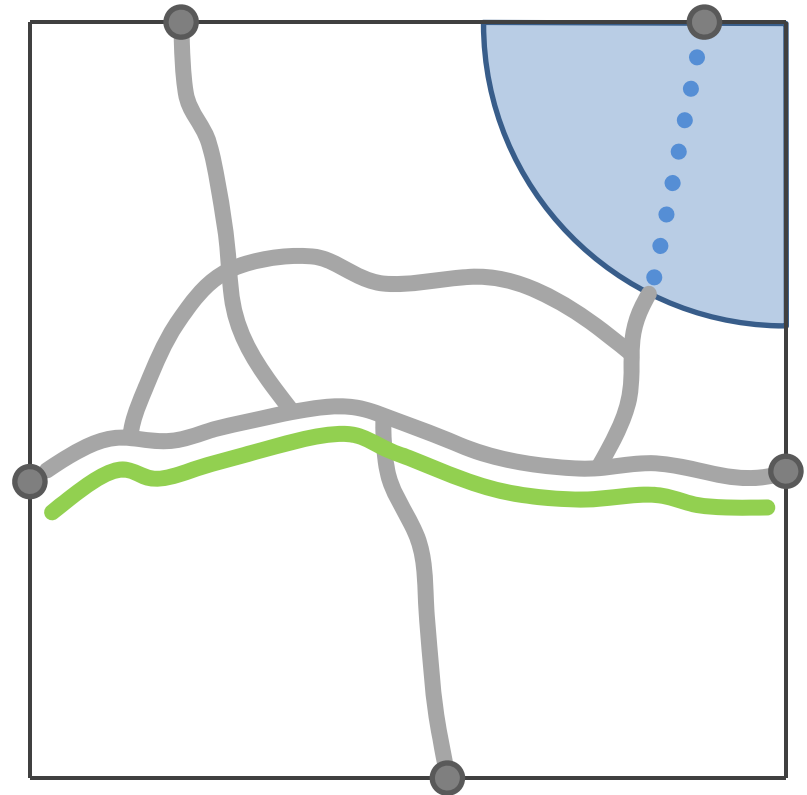
- **Simulate trade**
  - Neighbouring cities
- Trade routes





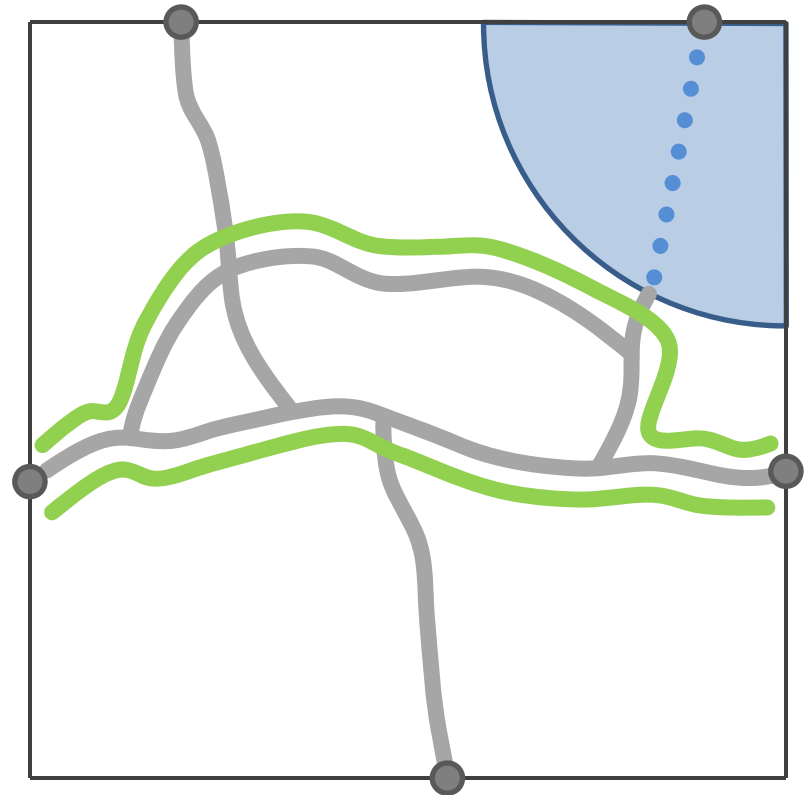
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities
- Trade routes
  - One



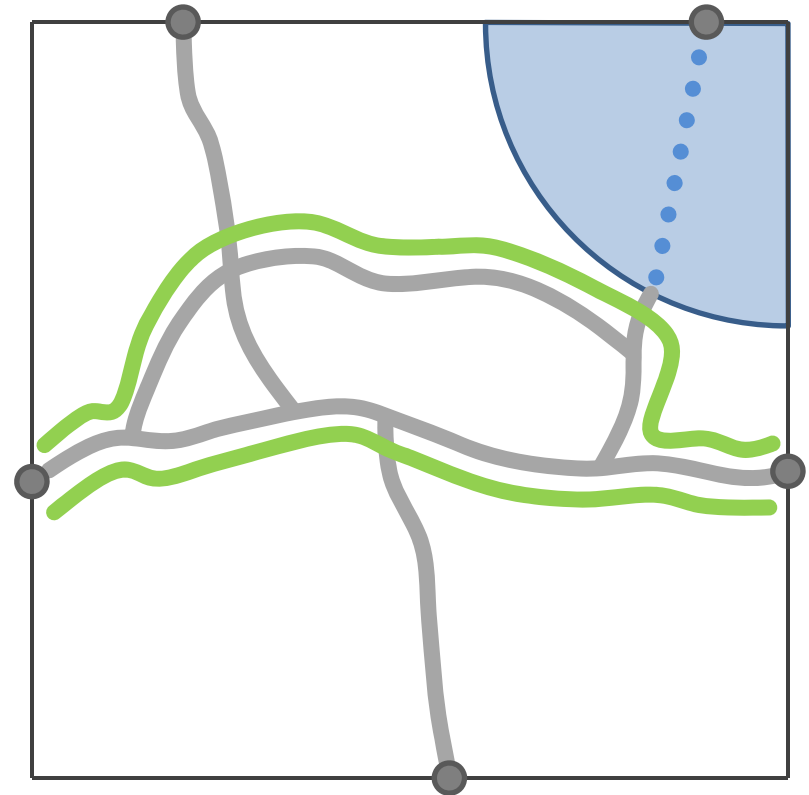
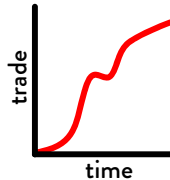
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities
- Trade routes
  - One
  - Or more



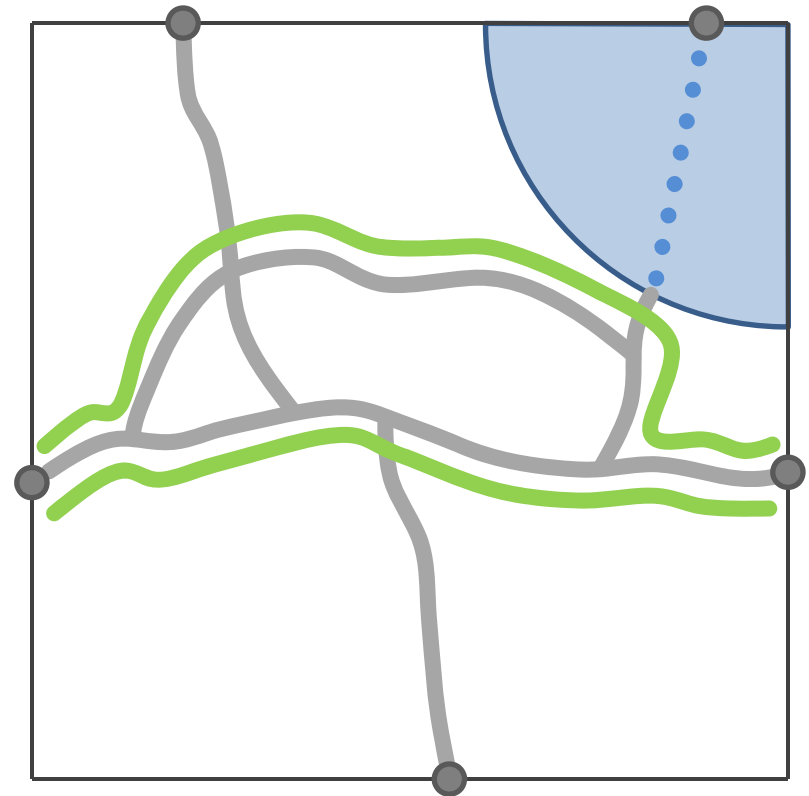
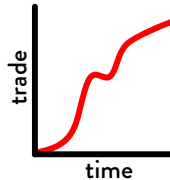
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities
- Trade routes
  - One
  - Or more
- Amount of trade
  - “*Historical context*”



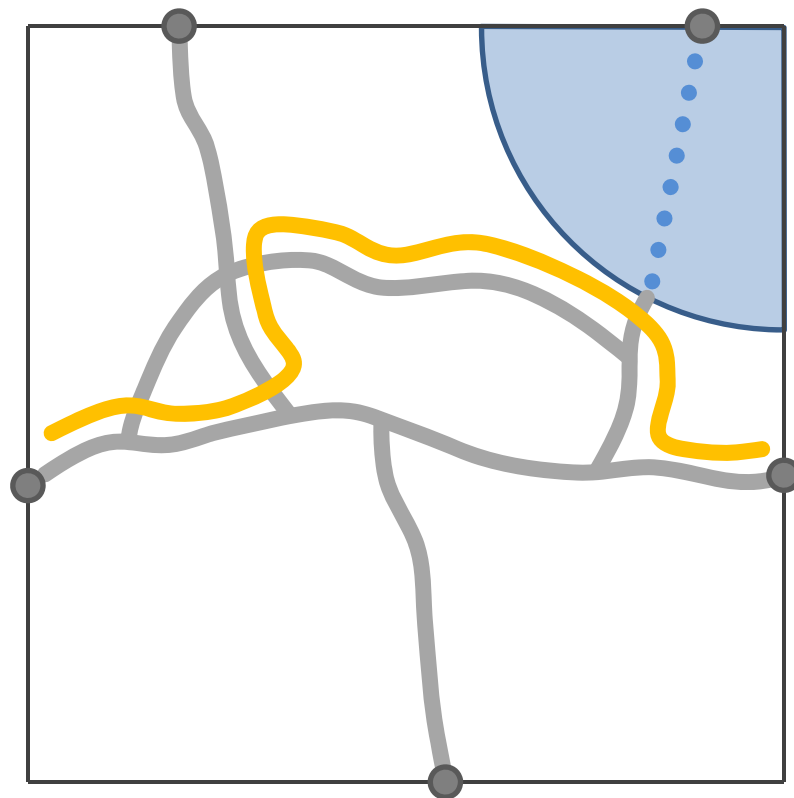
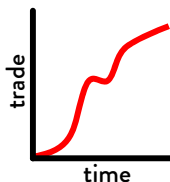
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities
- Trade routes
  - One
  - Or more
- Amount of trade
  - “*Historical context*”
- Trade routes full?



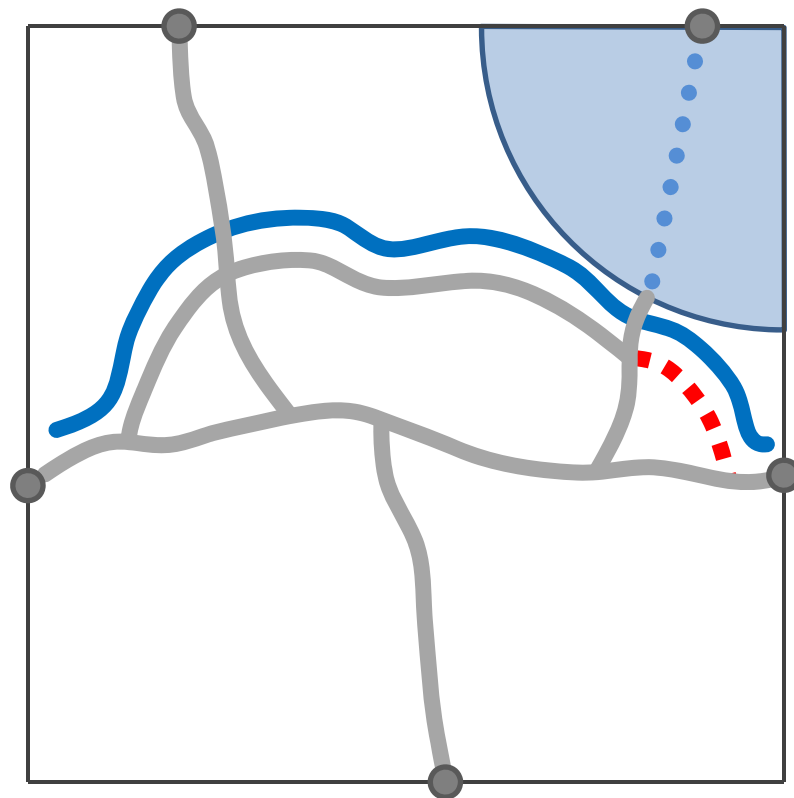
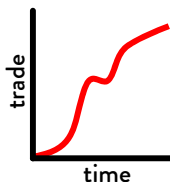
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities
- Trade routes
  - One
  - Or more
- Amount of trade
  - “*Historical context*”
- Trade routes full?
  - New trade route



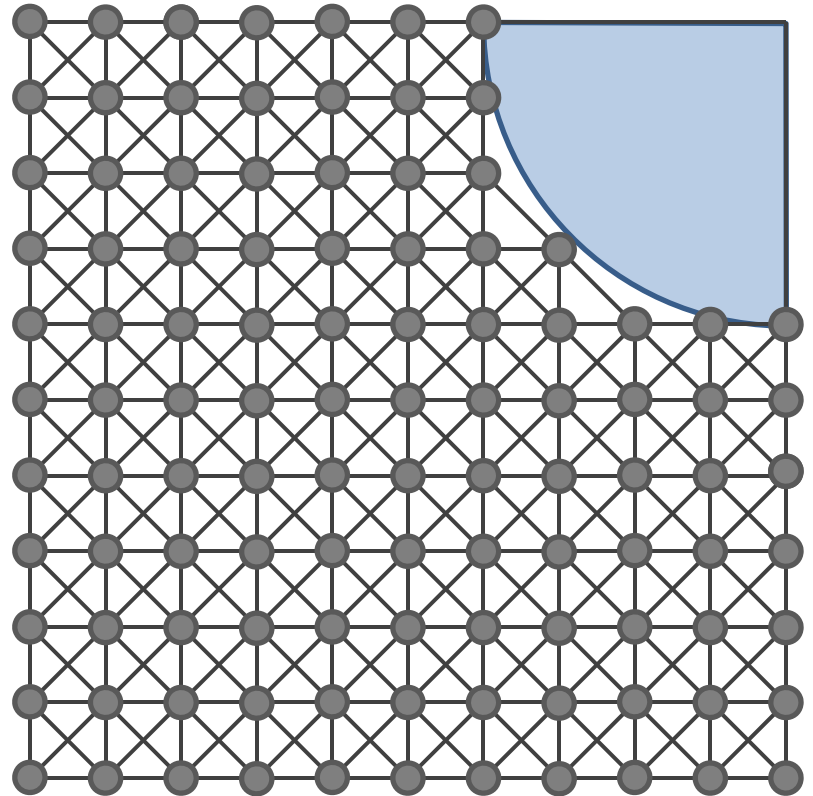
# Trade Simulation

- **Simulate trade**
  - Neighbouring cities
- Trade routes
  - One
  - Or more
- Amount of trade
  - “*Historical context*”
- Trade routes full?
  - New trade route
  - New major road & route



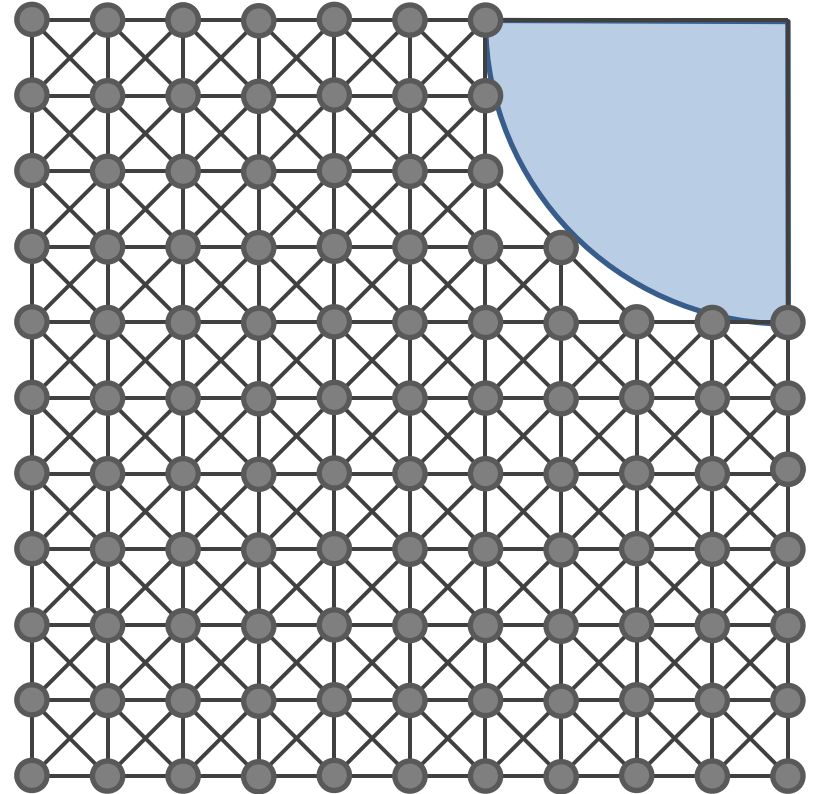
# Major Roads

- [Galín10]
  - Overlay terrain with a graph



# Major Roads

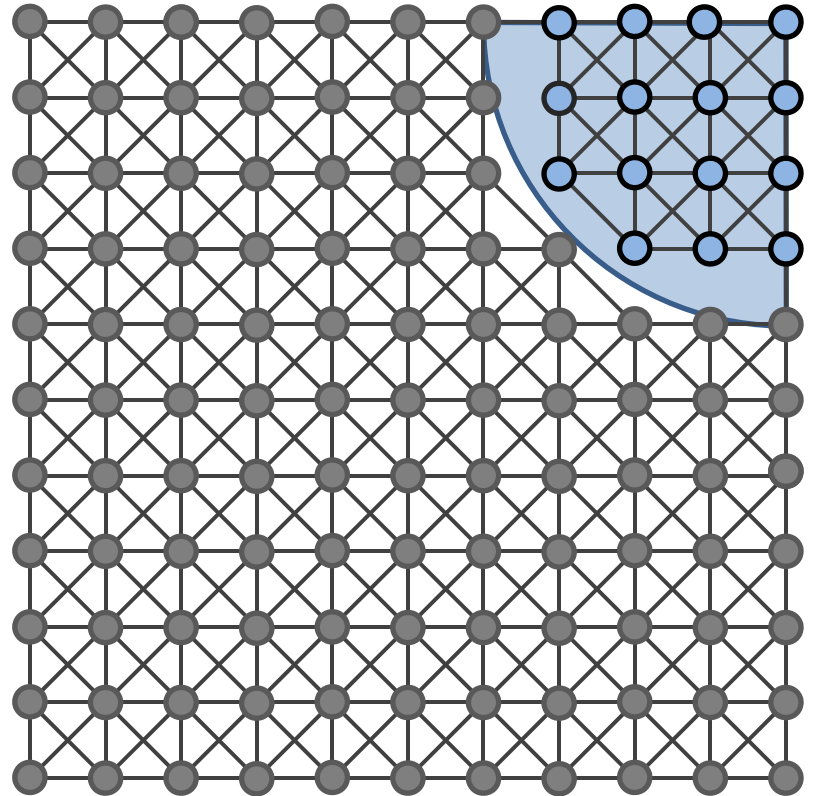
- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path





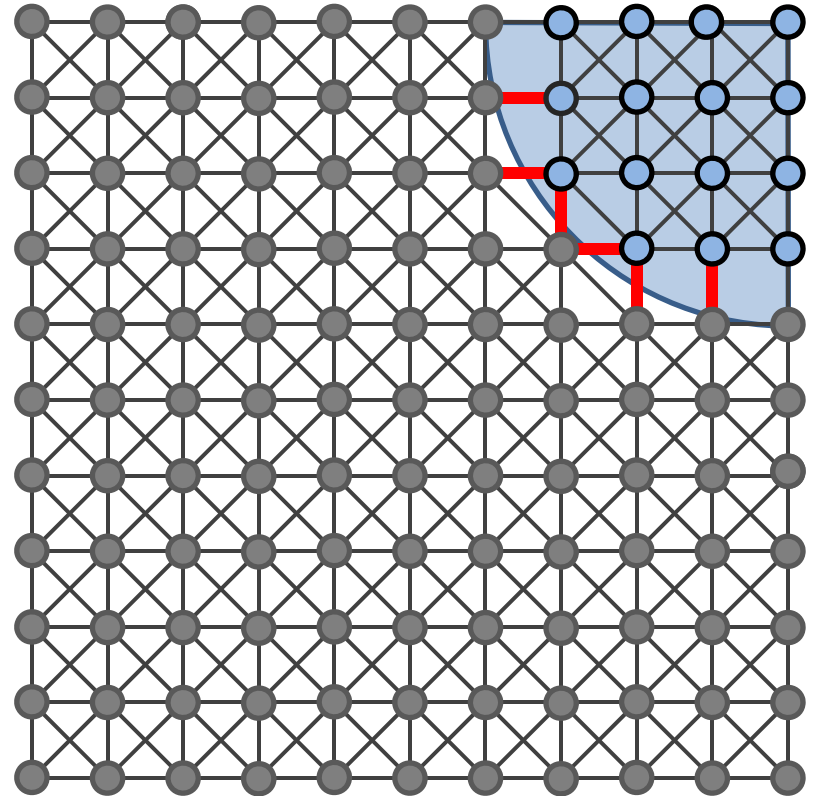
# Major Roads

- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph



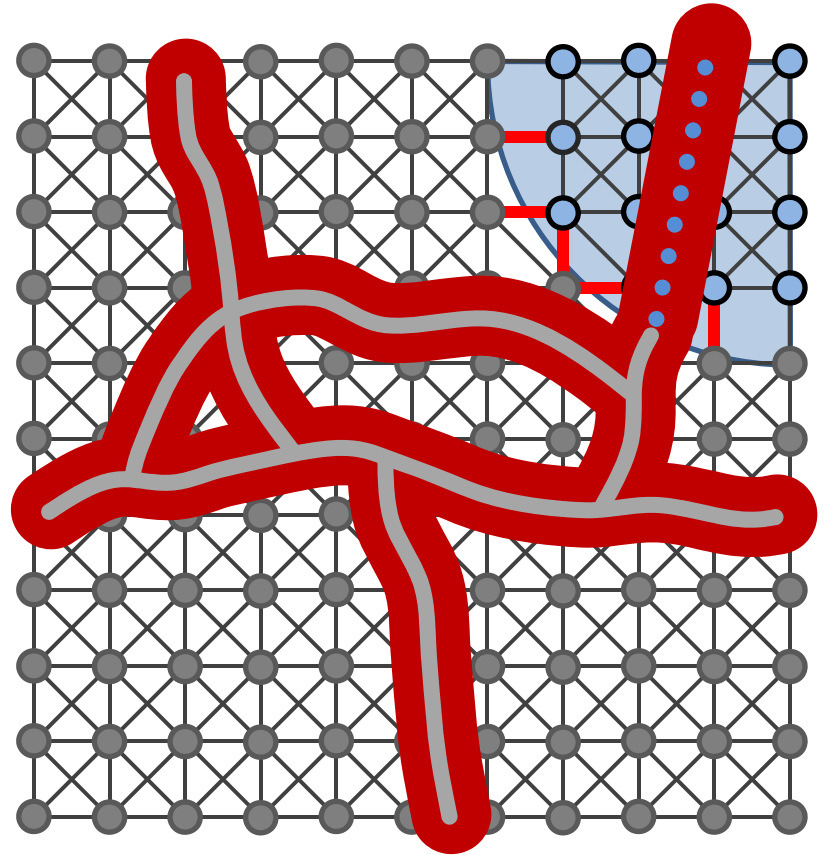
# Major Roads

- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph
  - Harbour edges



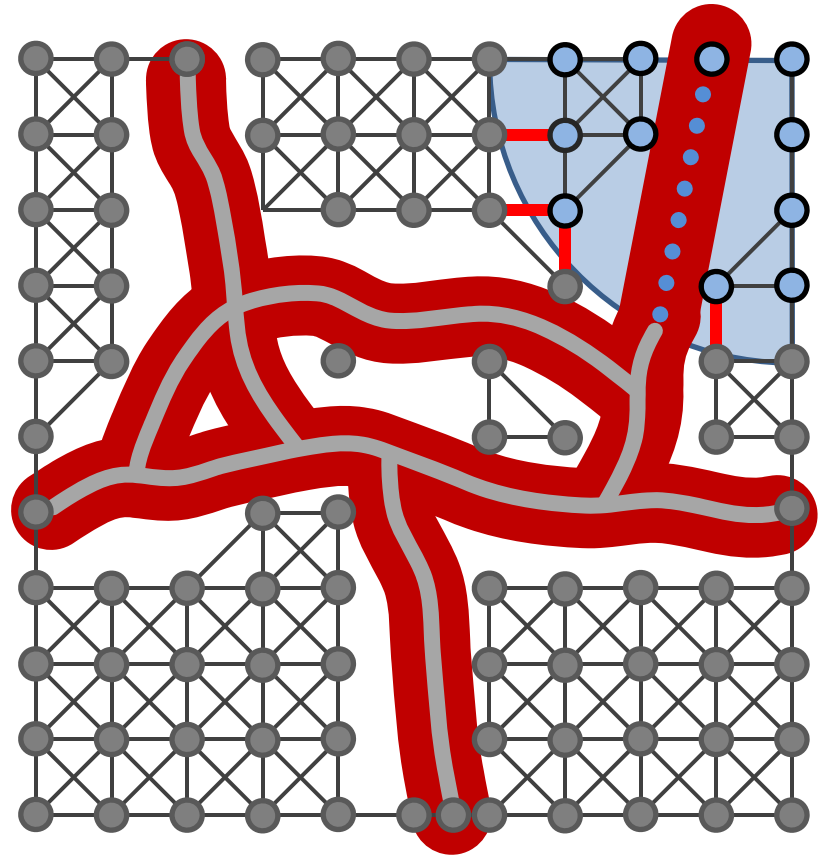
# Major Roads

- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph
  - Harbour edges
- Existing road network



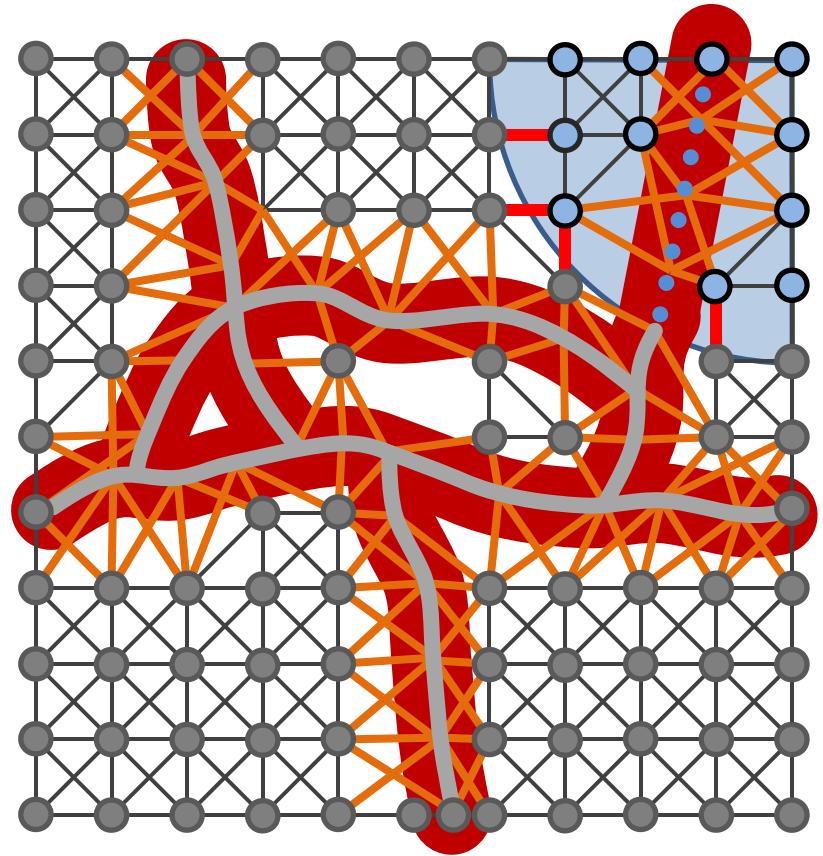
# Major Roads

- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph
  - Harbour edges
- Existing road network
  - Remove collisions



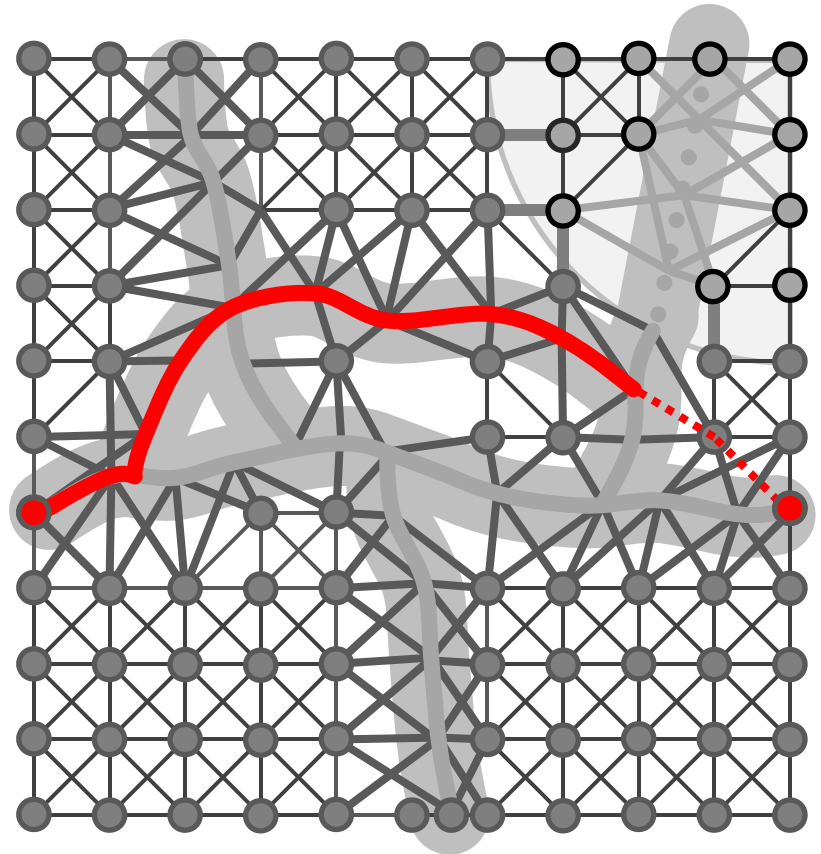
# Major Roads

- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph
  - Harbour edges
- Existing road network
  - Remove collisions
  - Stitch together



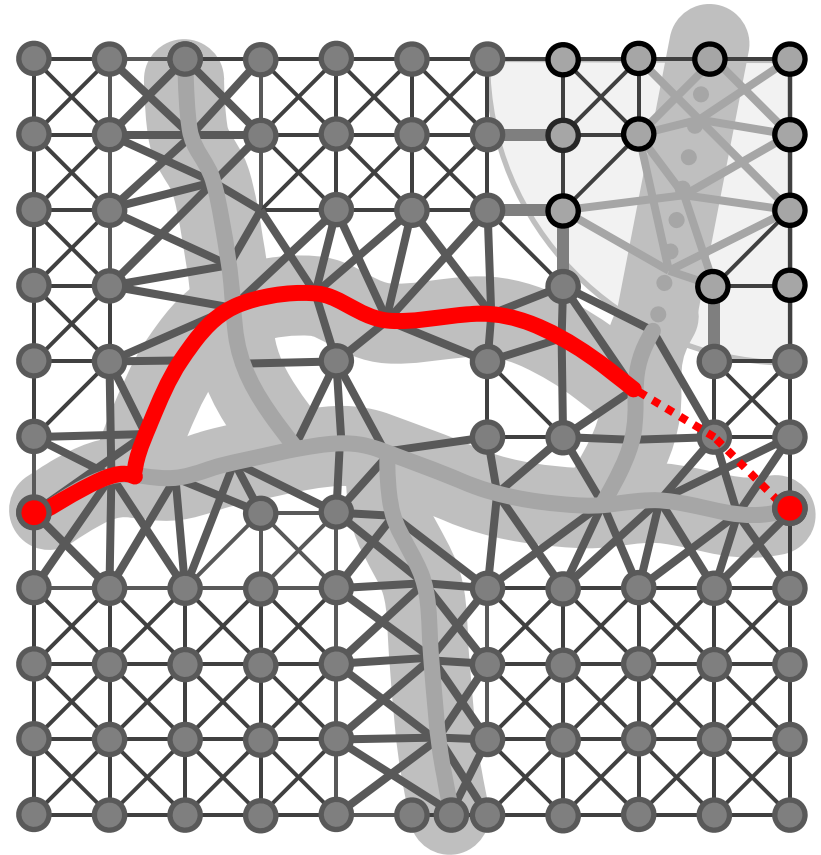
# Major Roads

- [Galín10]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph
  - Harbour edges
- Existing road network
  - Remove collisions
  - Stitch together
  - Use instead

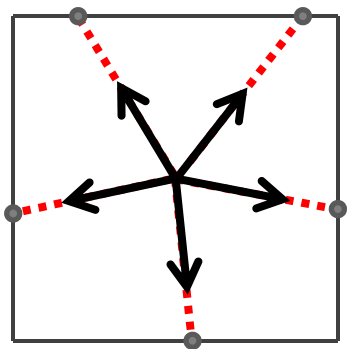


# Major Roads

- [[Galín10](#)]
  - Overlay terrain with a graph
  - Curvature & elevation aware shortest path
- Extend
  - Water graph
  - Harbour edges
- Existing road network
  - Remove collisions
  - Stitch together
  - Use instead

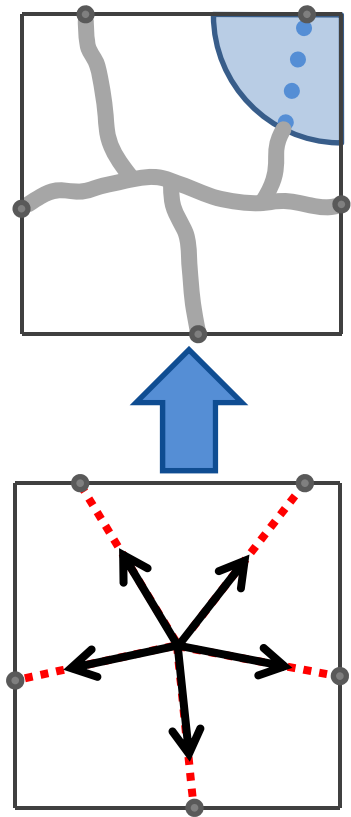


# Recapitulation

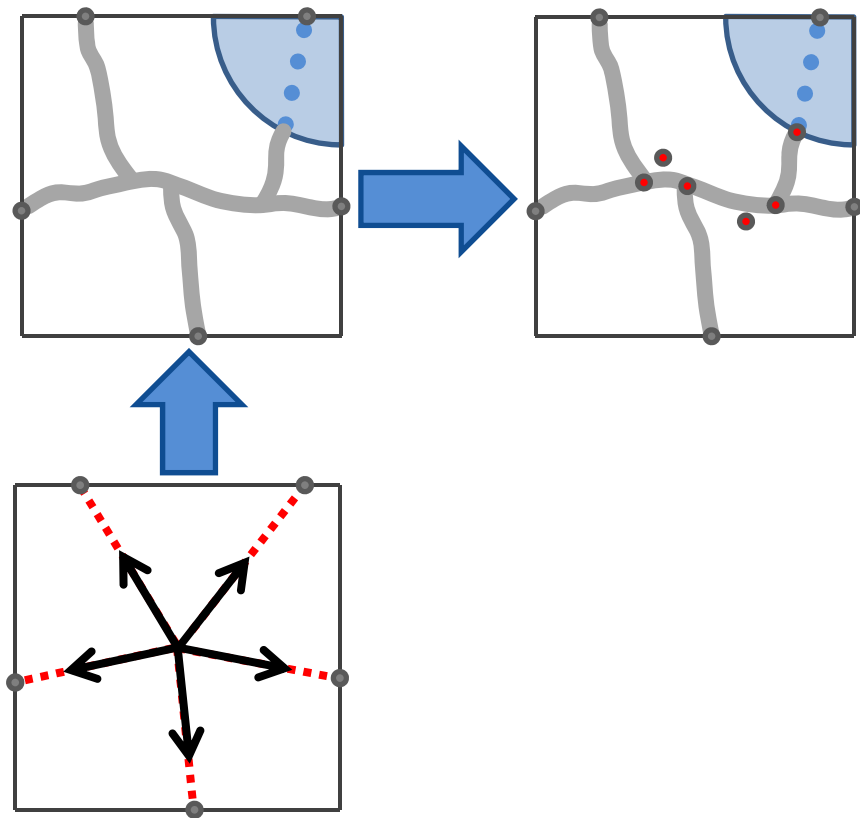




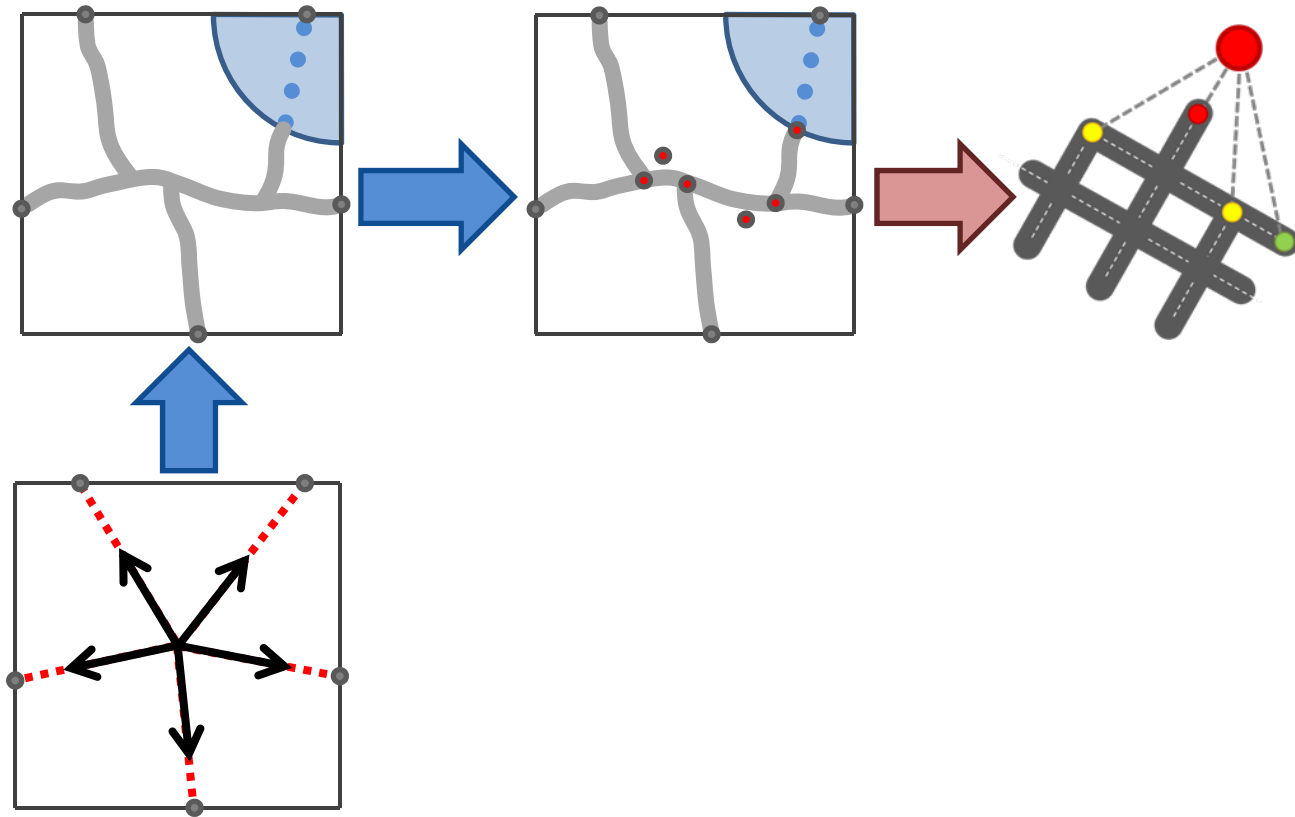
# Recapitulation



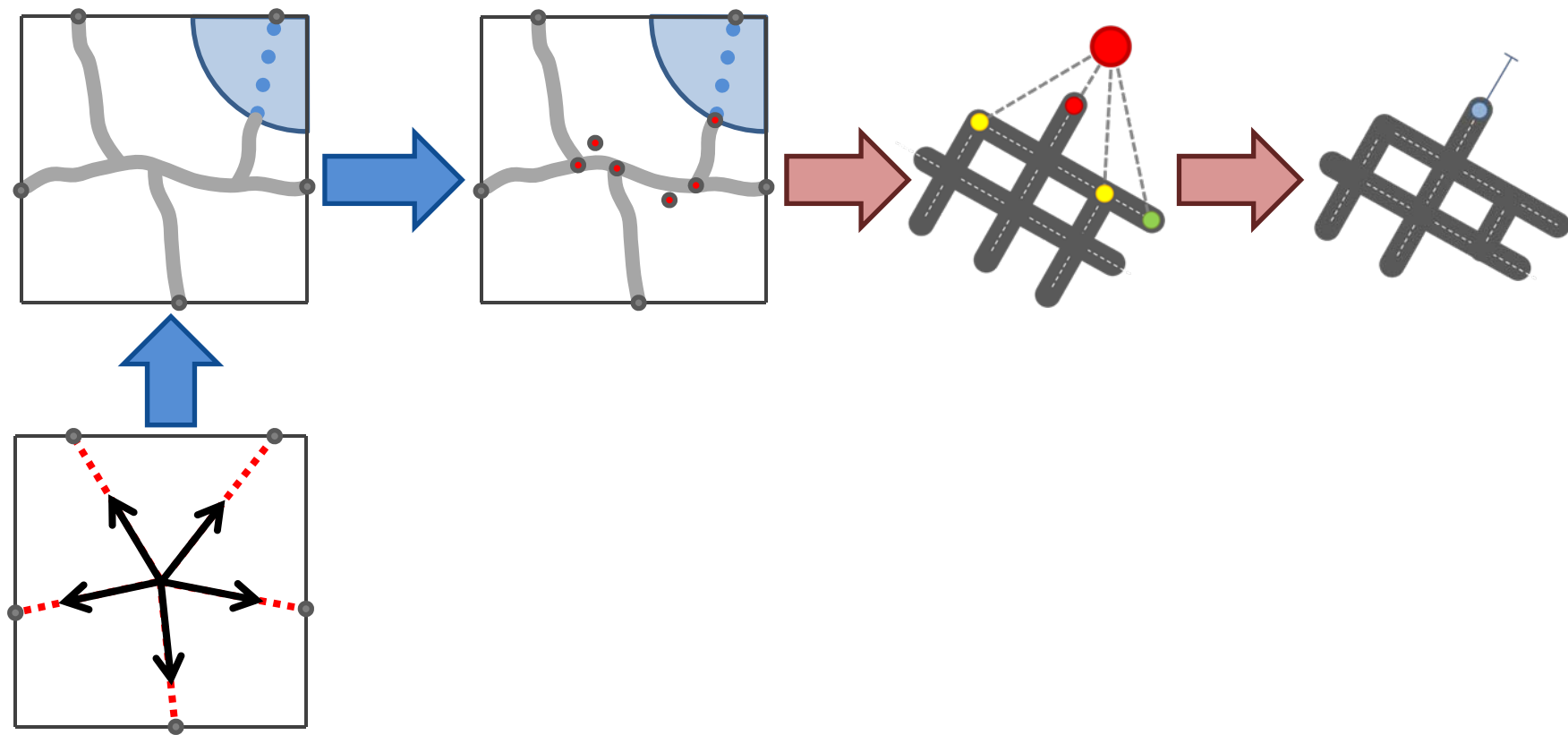
# Recapitulation



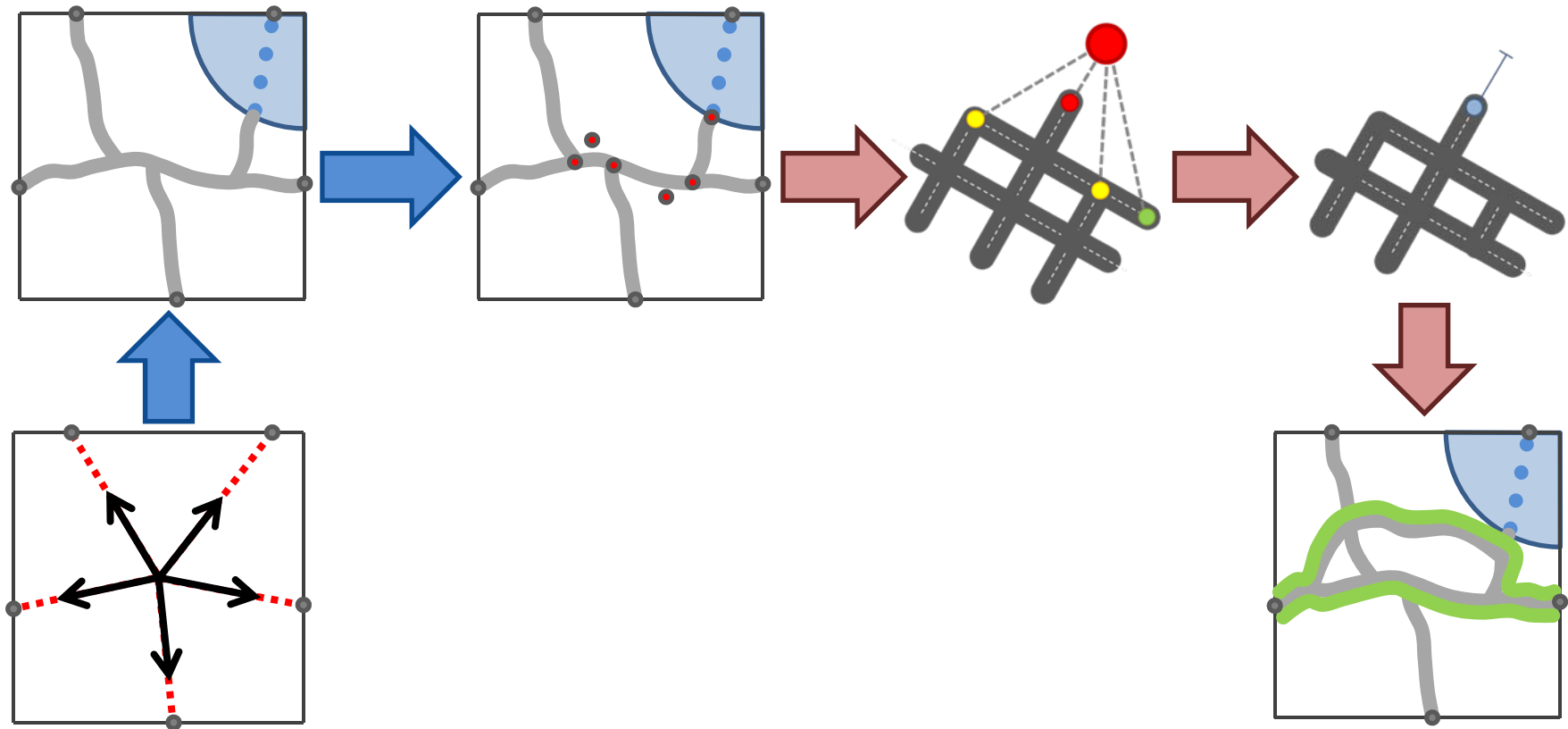
# Recapitulation



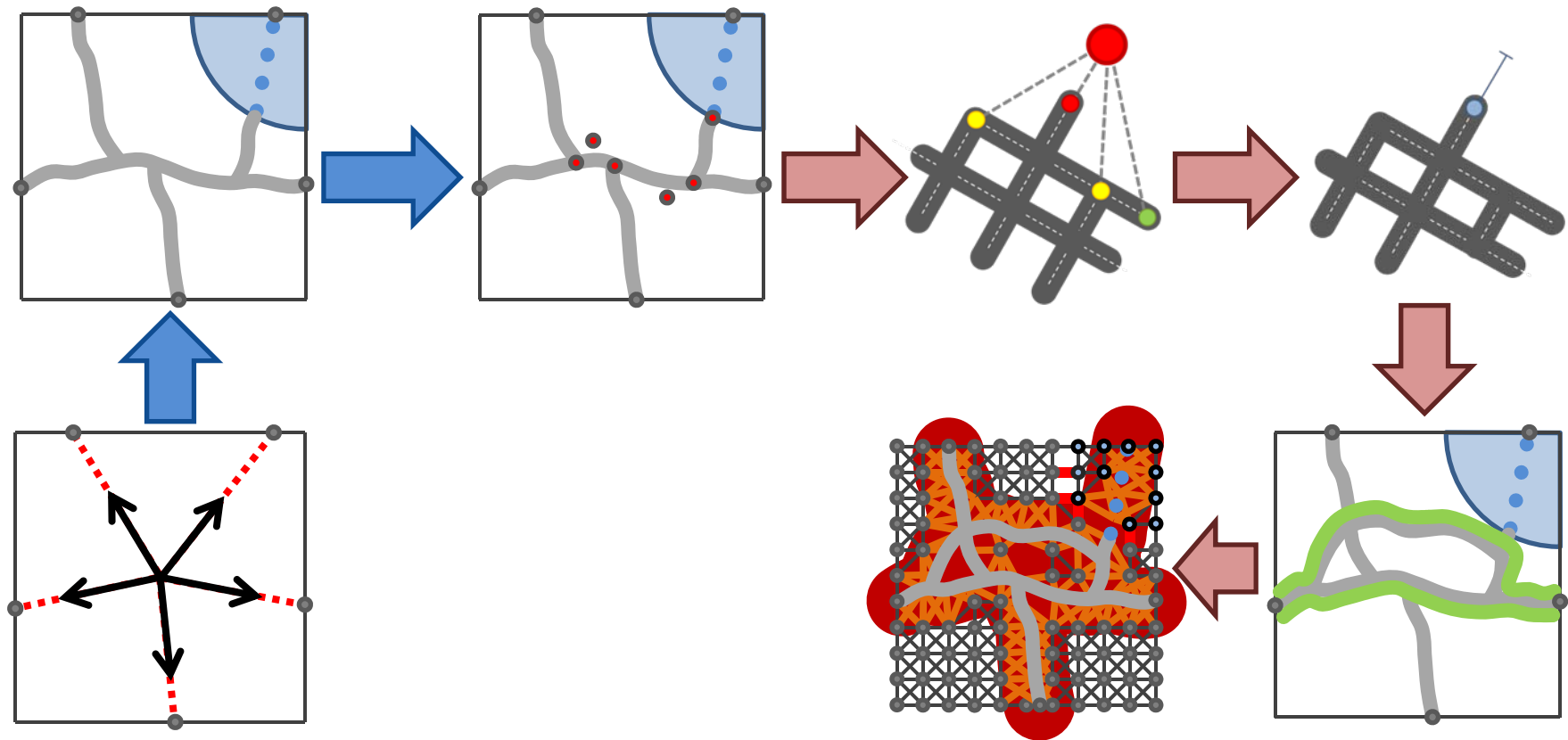
# Recapitulation



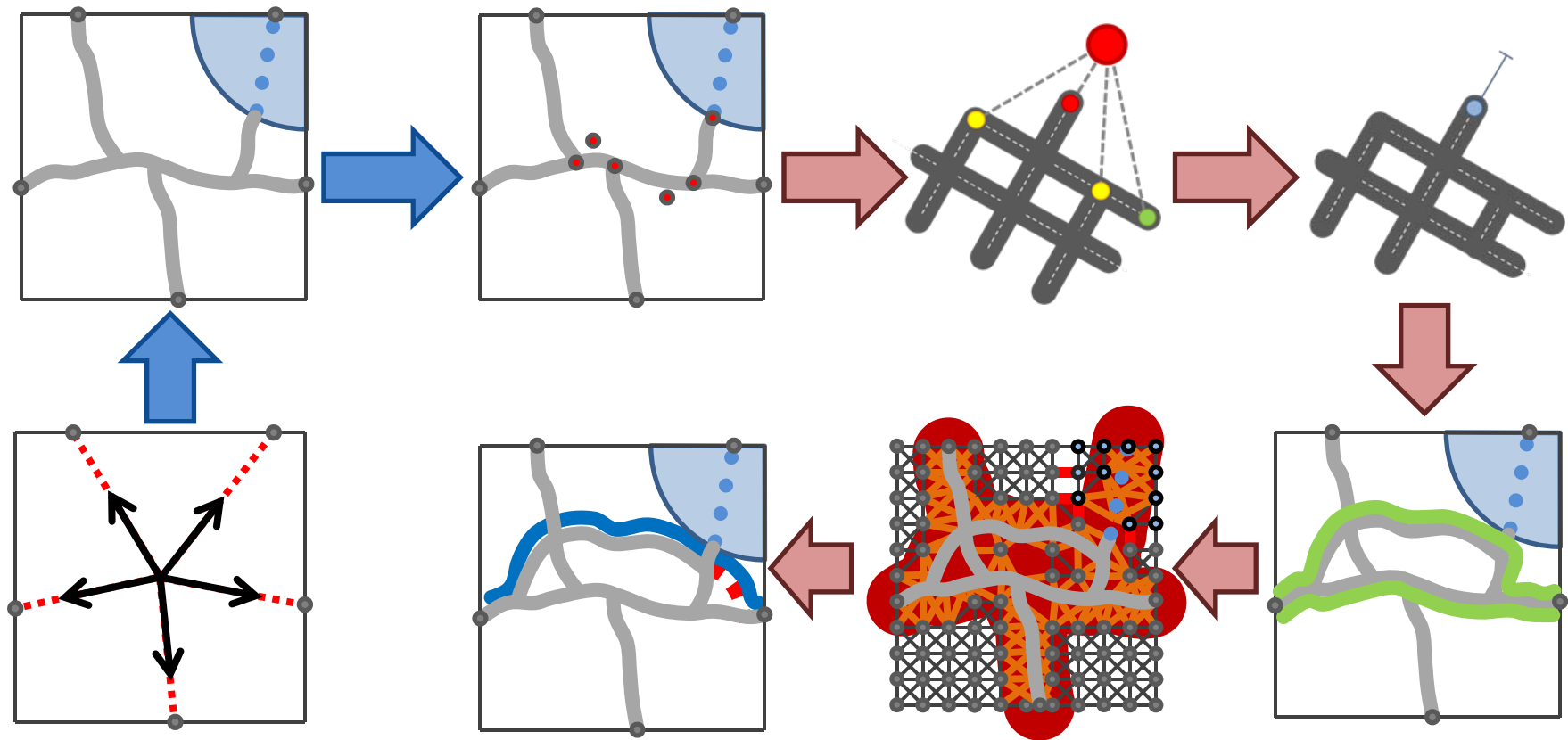
# Recapitulation



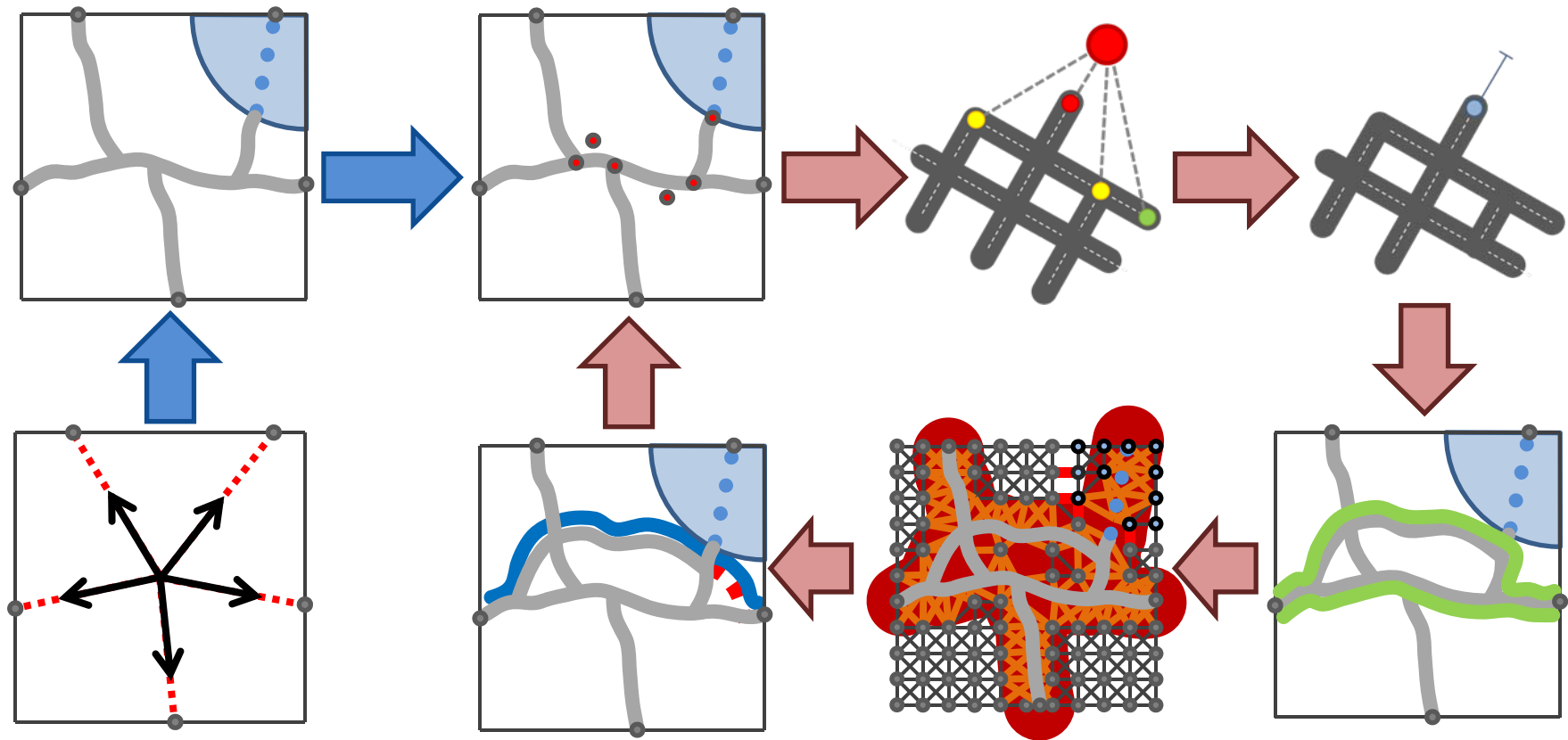
# Recapitulation



# Recapitulation

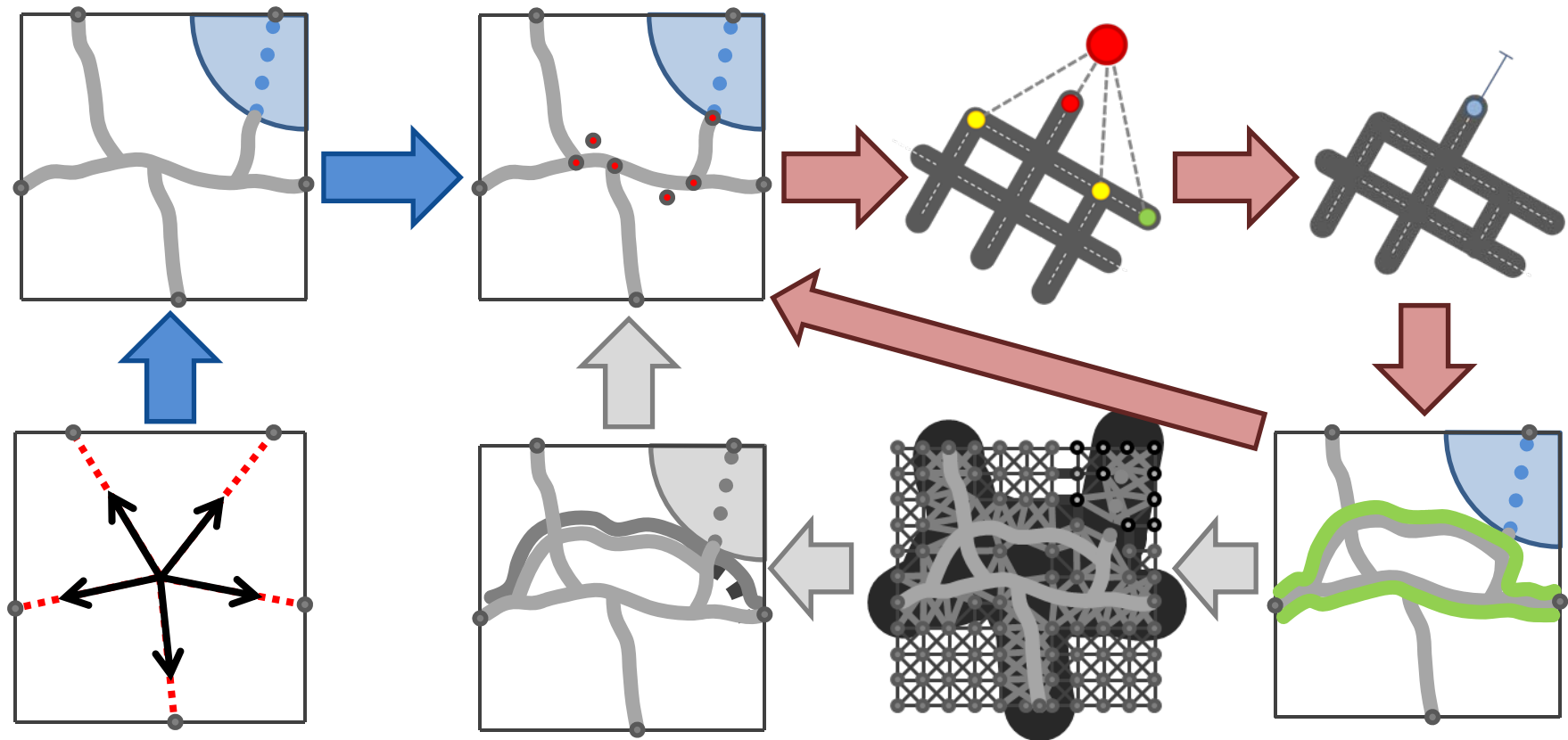


# Recapitulation

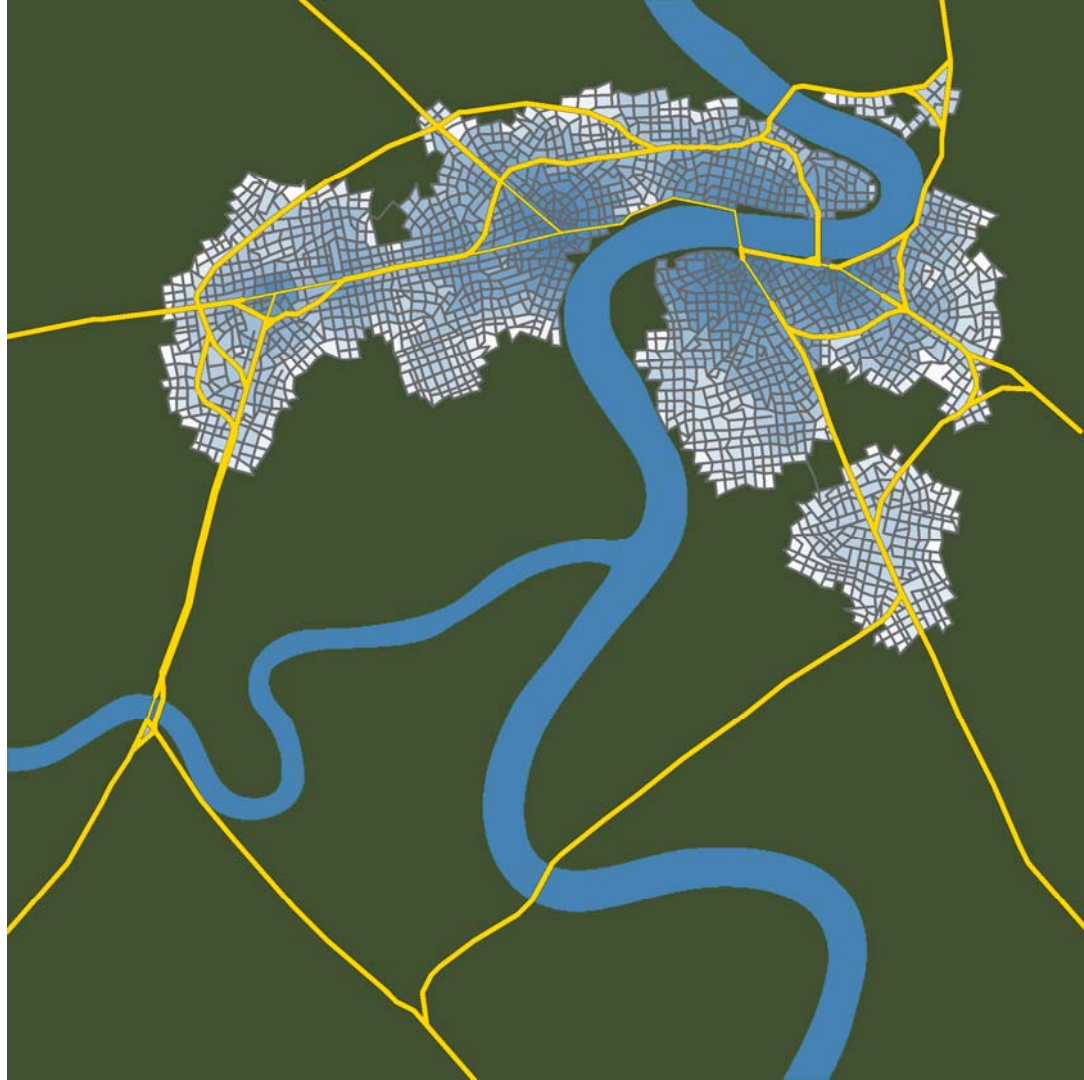


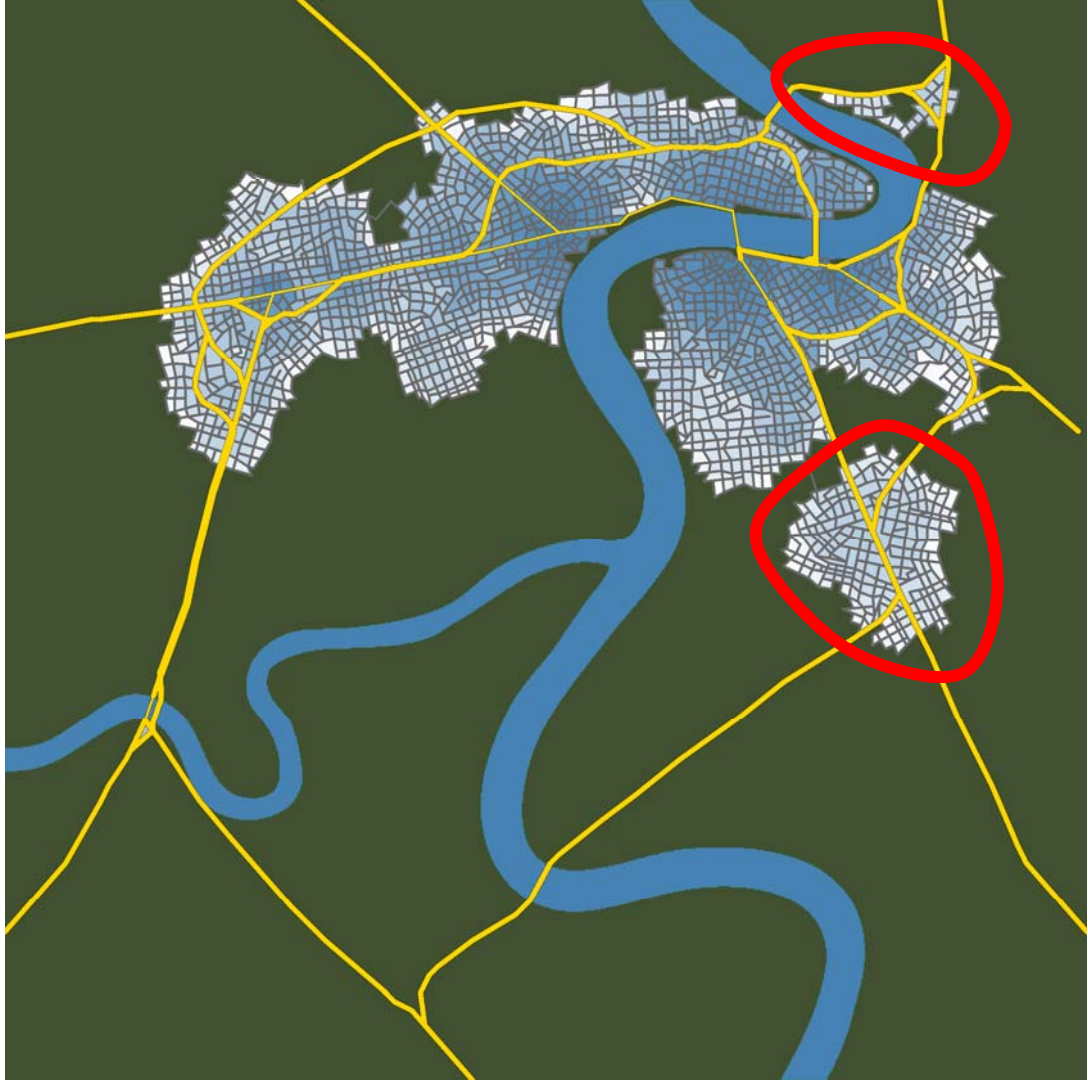


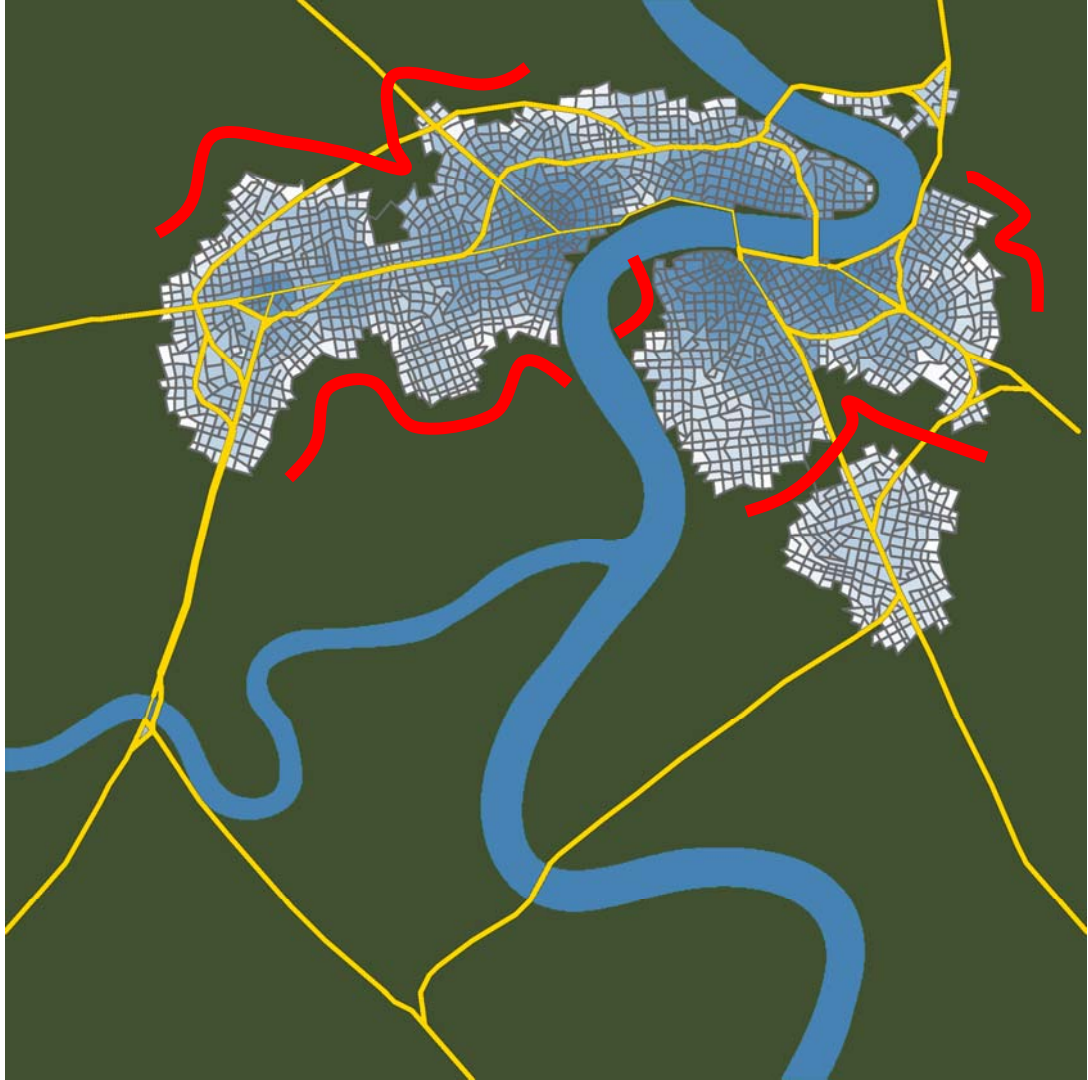
# Recapitulation

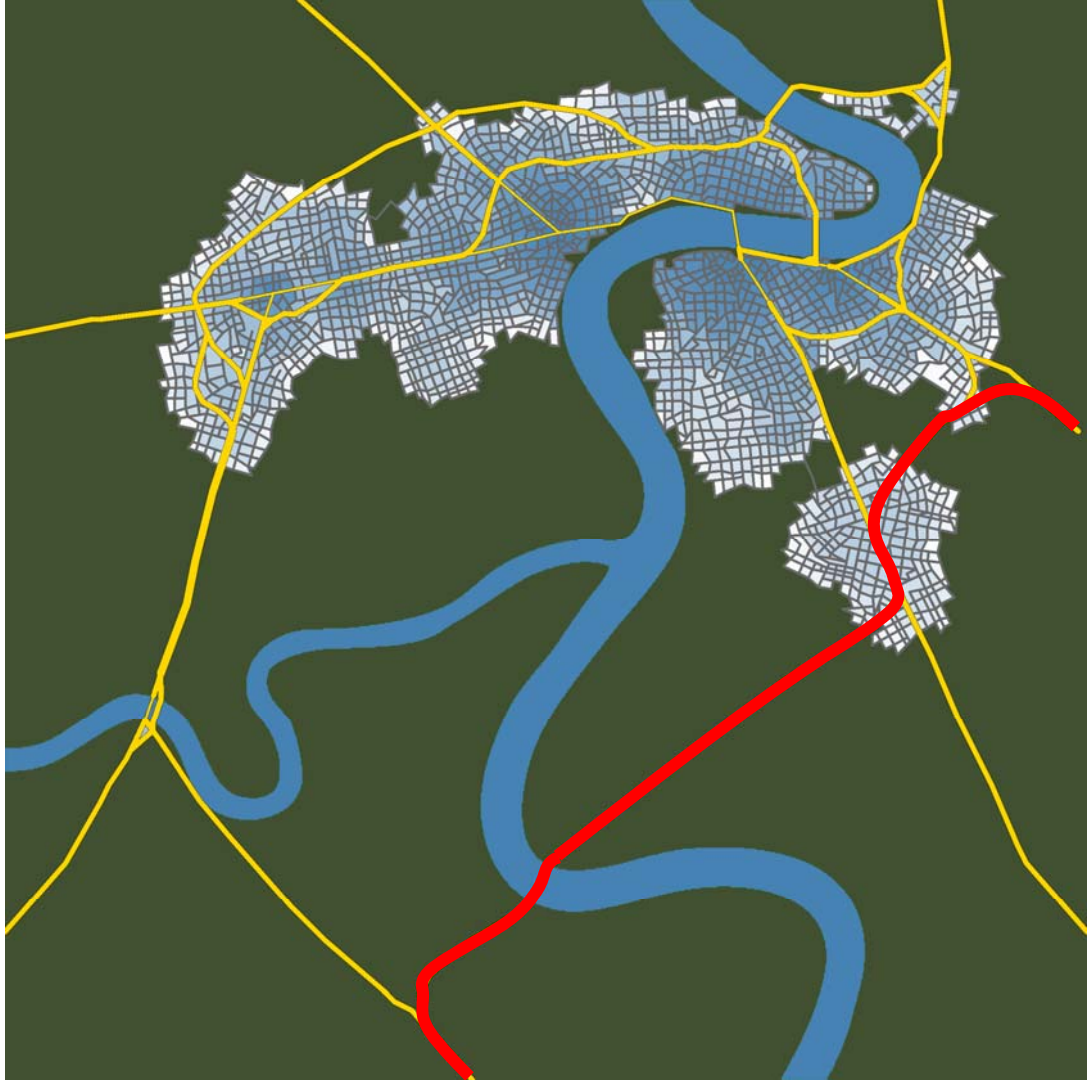


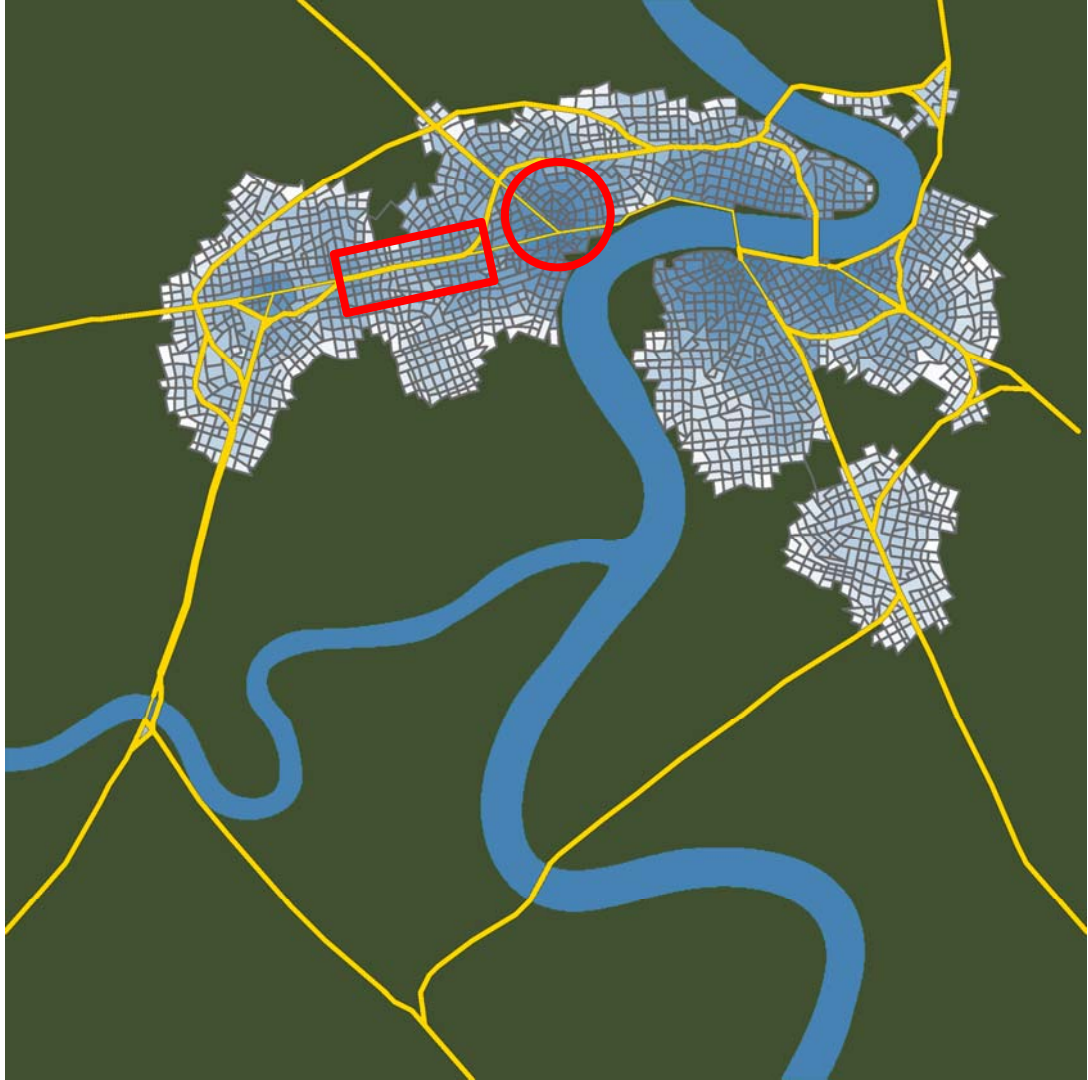
# Results & Conclusions

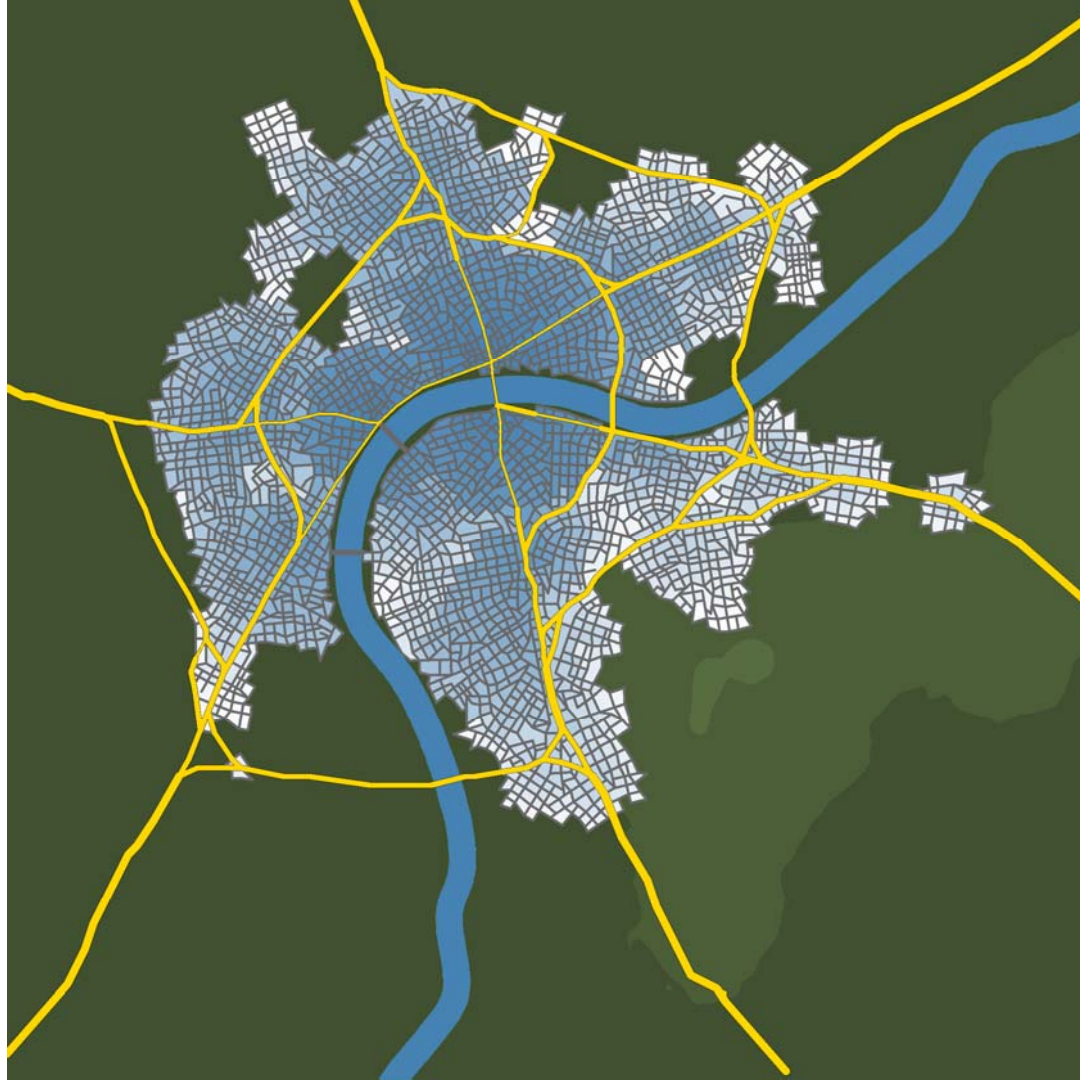




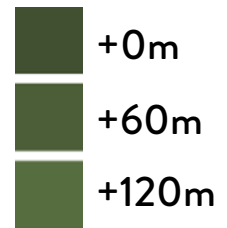




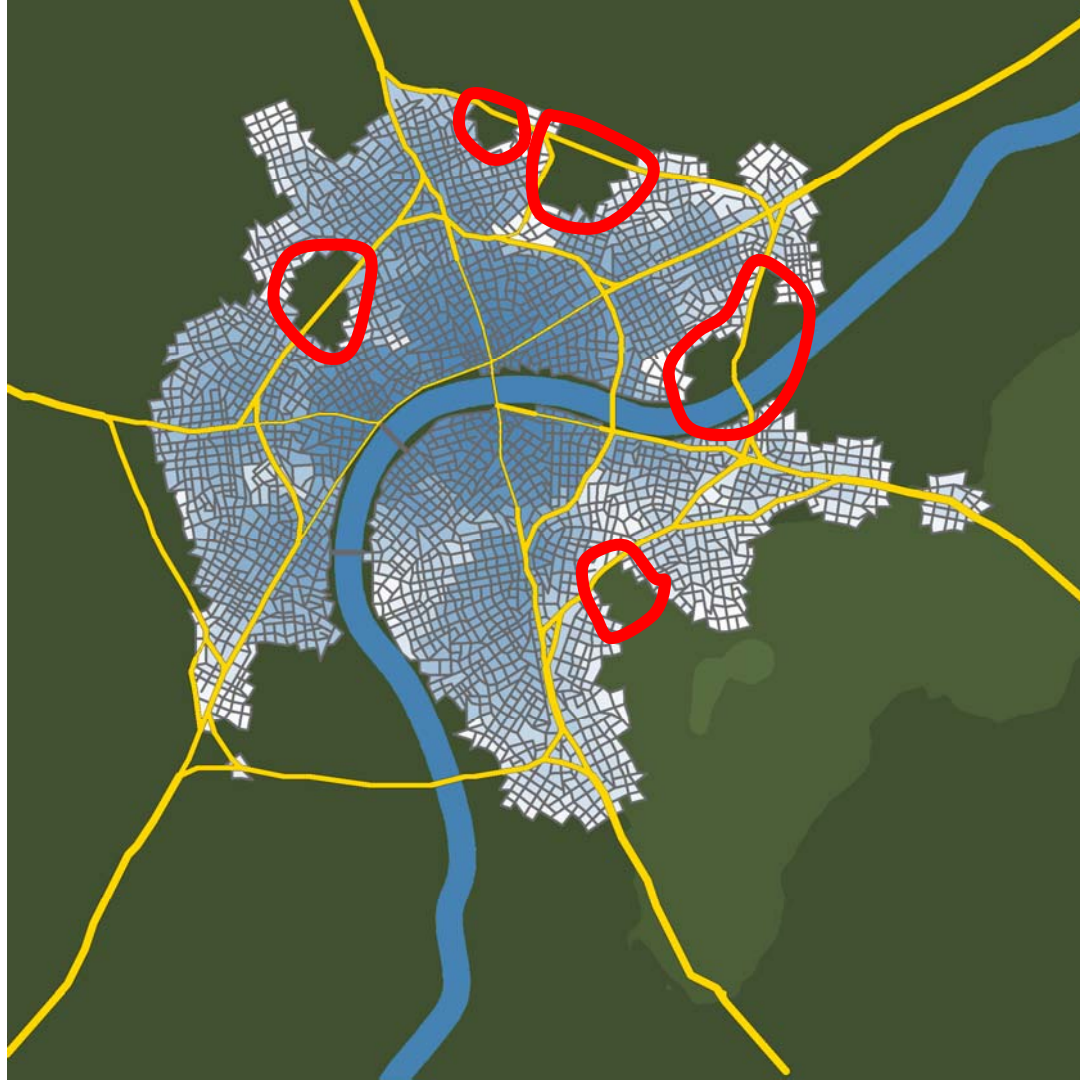




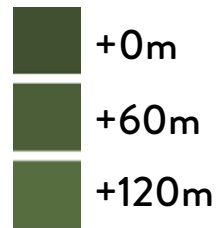
### Elevation

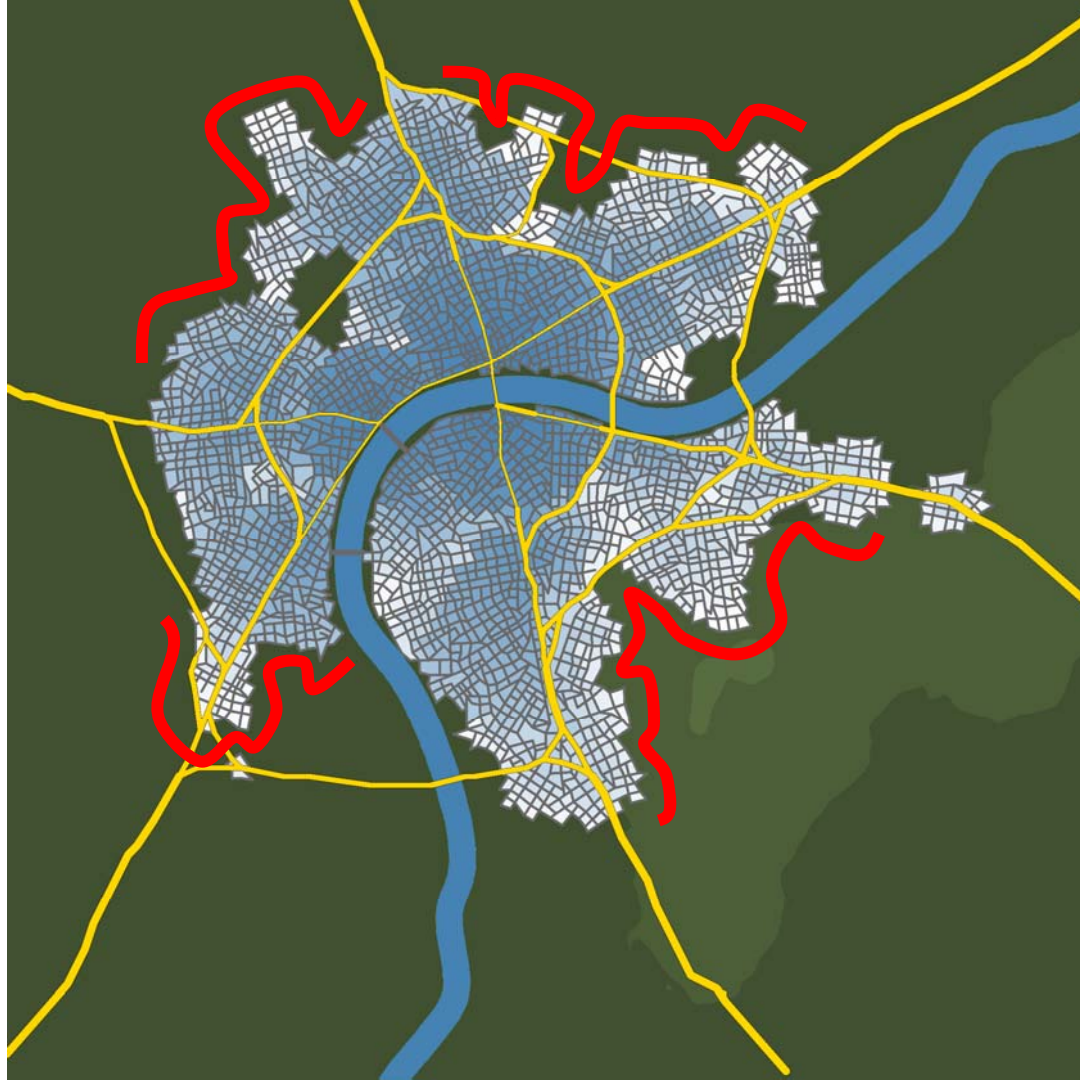




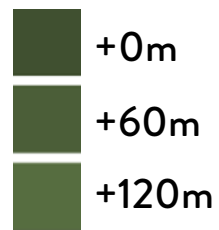


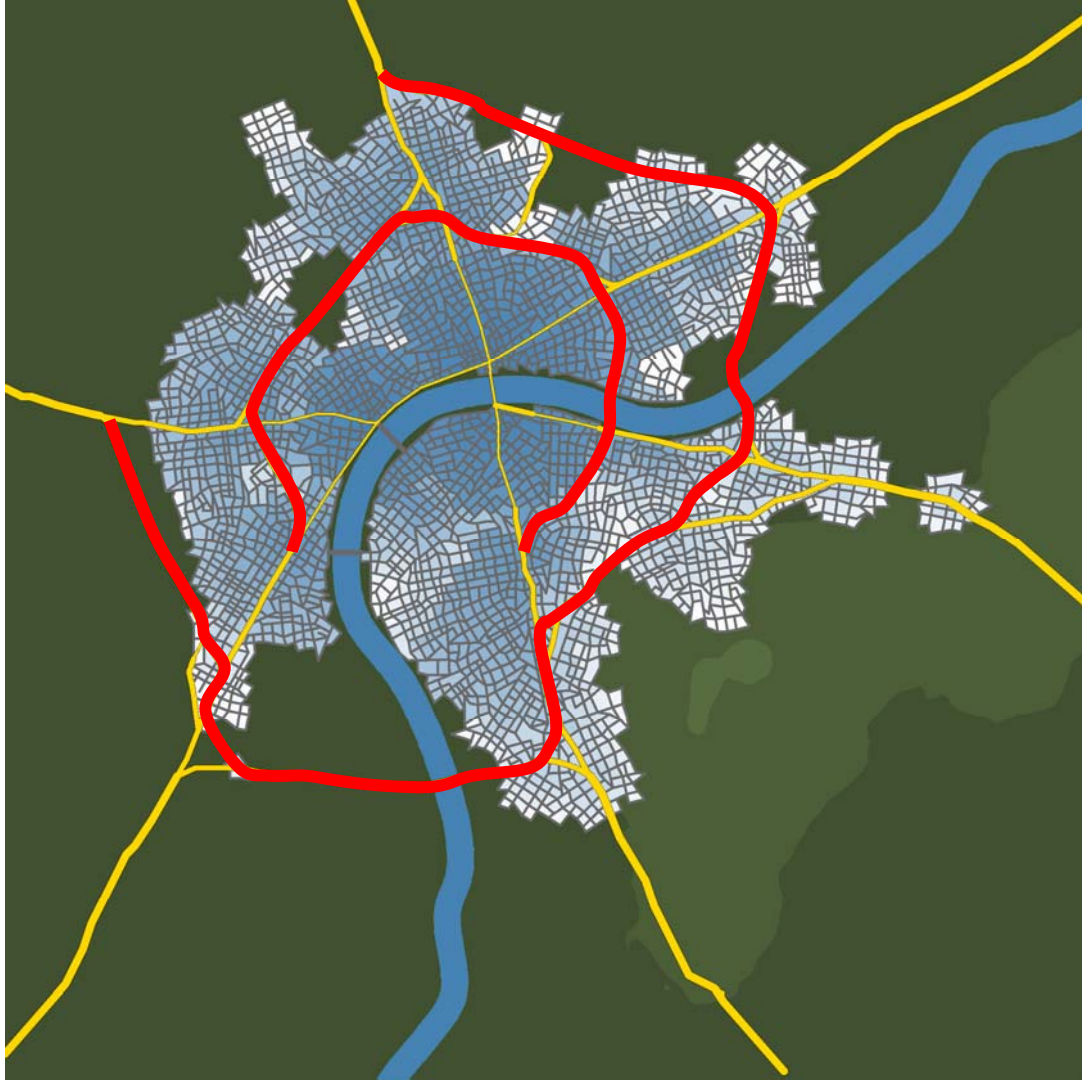
Elevation





Elevation





Elevation

- +0m
- +60m
- +120m



Elevation



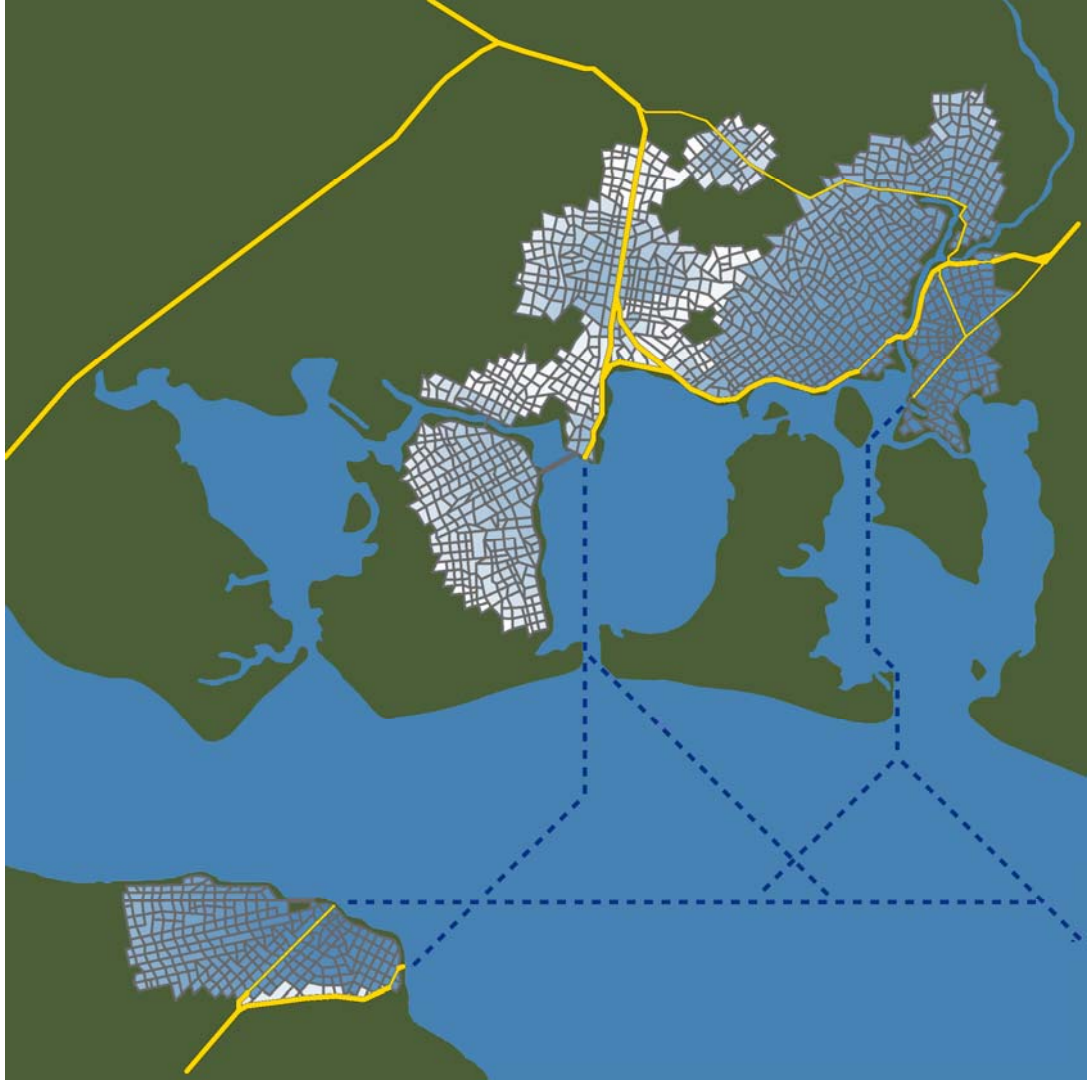
+0m



+60m



+120m







# Conclusions

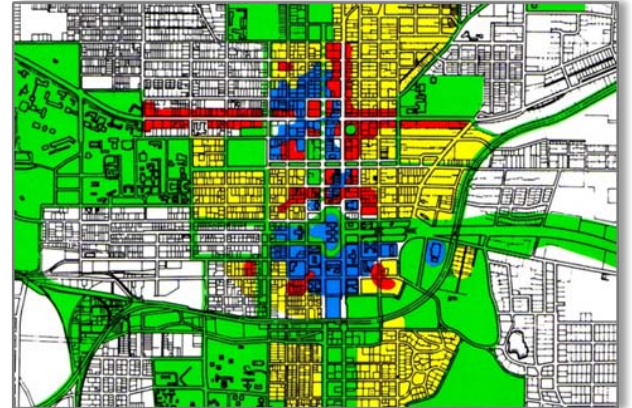
- More realistic cities
  - Assumes trade is key
  - Trade driven major roads
  - Water and terrain
  - Settlement placement
  - City as a set of settlements
- Requires minimal input





# Future Work

- Other modes of transportation
- Incorporate Land Use
- In-city transportation
- Redevelopment



# Thank you!

Paper, video, supplemental materials:

[JanBenes.net](http://JanBenes.net)

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