



CONFERENCE 4 – 7 December 2018  
EXHIBITION 5 – 7 December 2018  
Tokyo International Forum, Japan  
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# Selective guided sampling with complete light transport paths

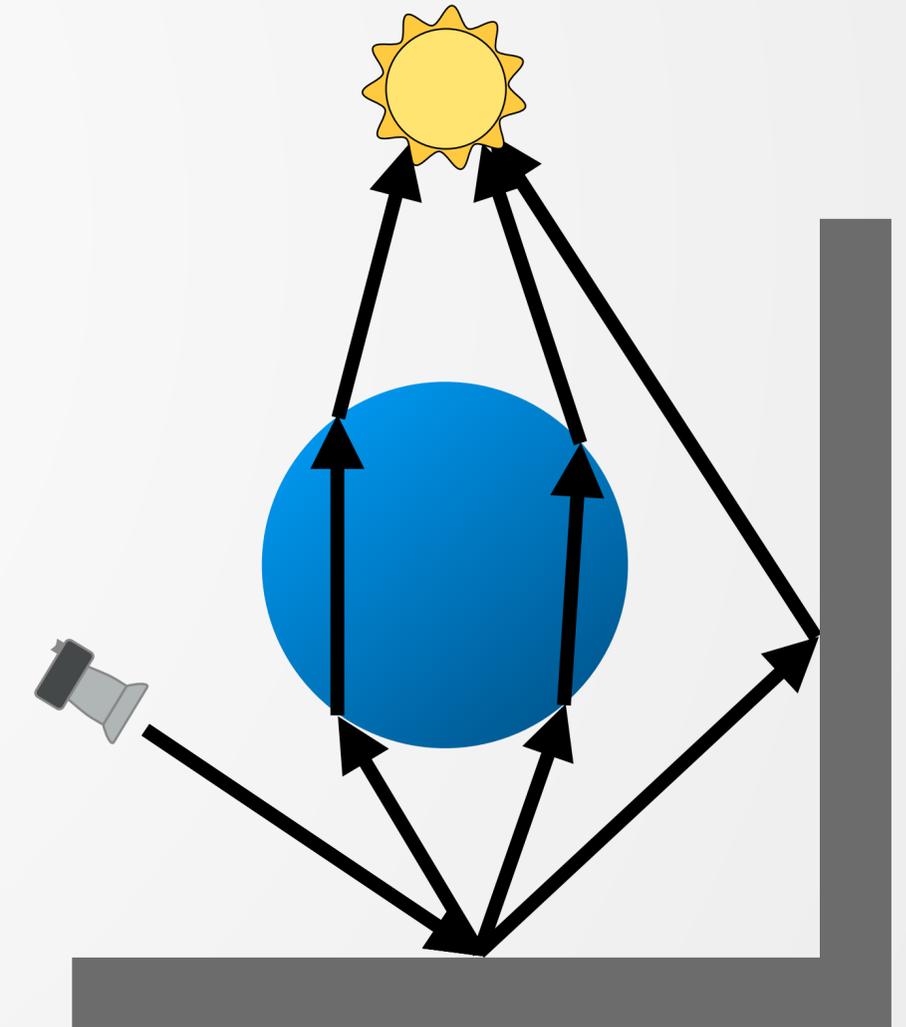
Florian Reibold, Johannes Hanika, Alisa Jung, Carsten Dachsbacher

Karlsruhe Institute of Technology, Germany



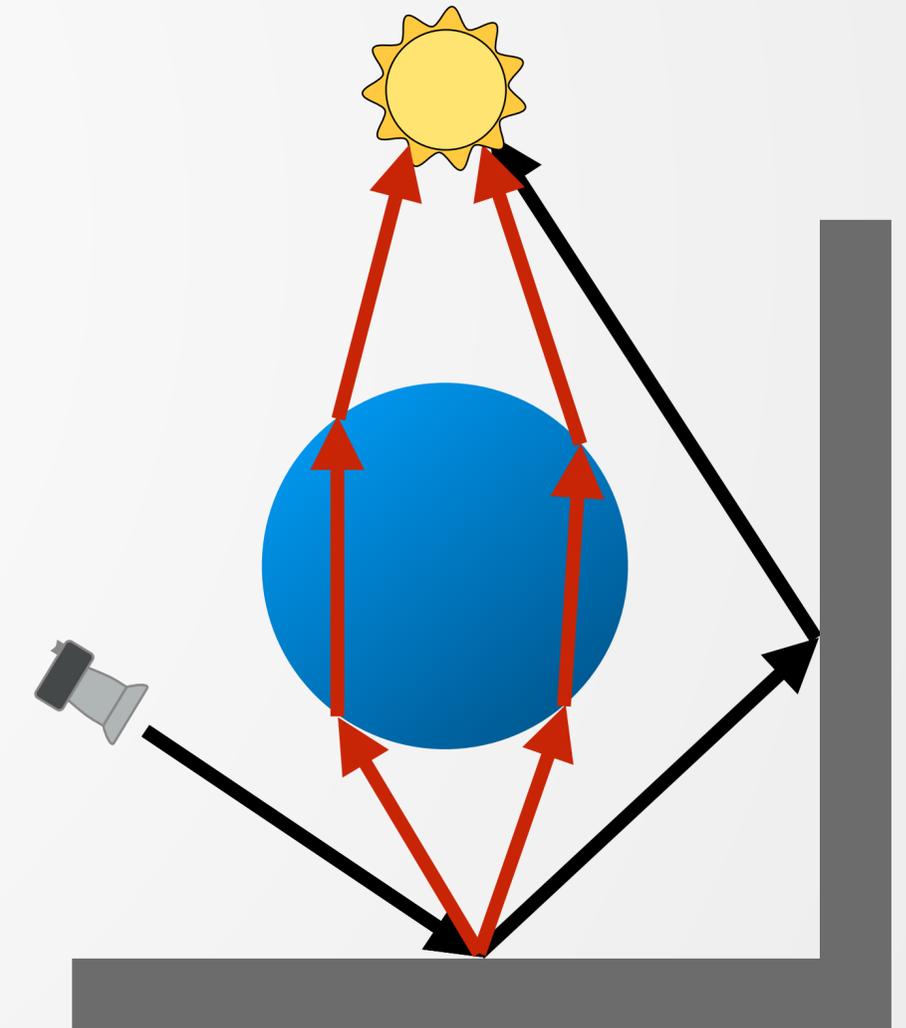
# Motivation

- Path tracing can efficiently handle the majority of rendering problems in practice (Fascione et al. [2017])



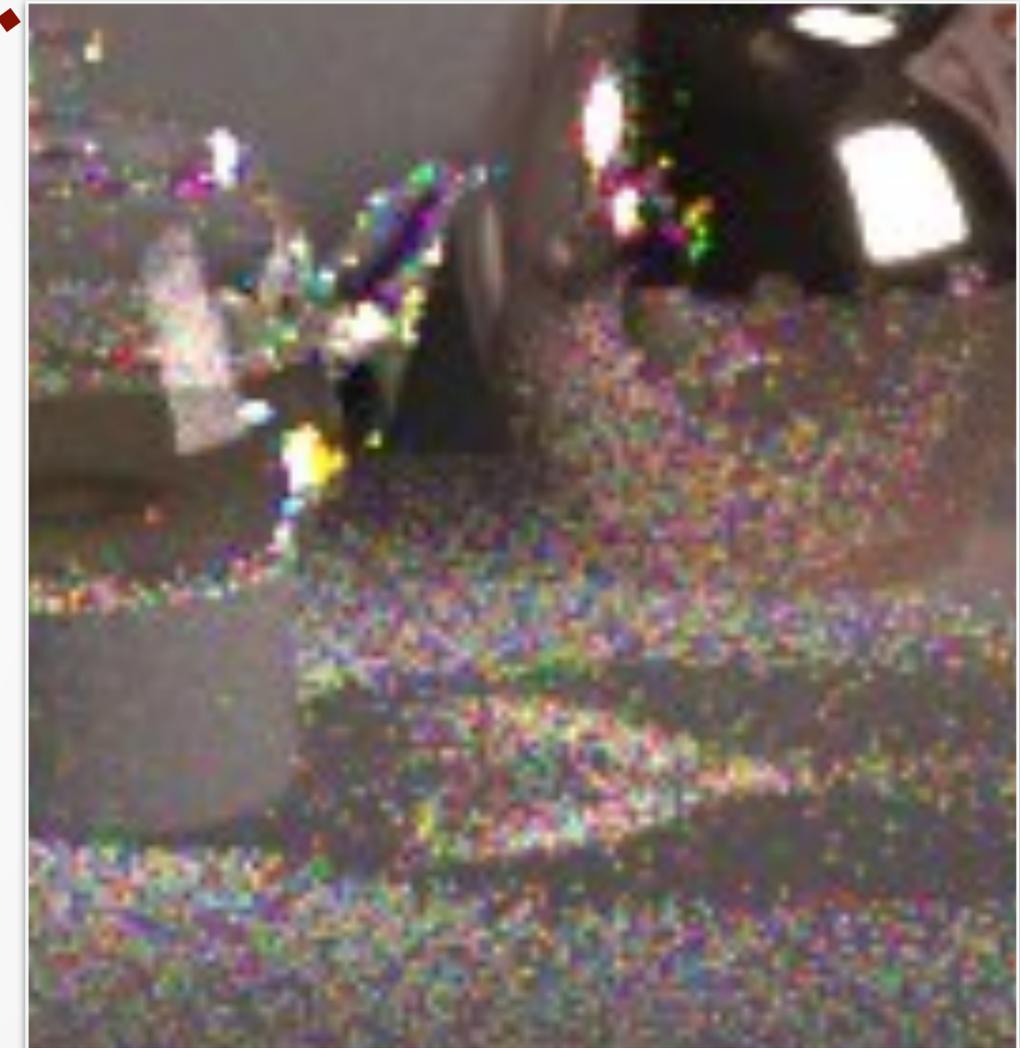
# Motivation

- What about the rest?



# Motivation

- What about the rest?



# Motivation



↑  
Unproblematic  
light transport

Difficult light transport  
outliers



# Motivation



↑  
Unproblematic  
light transport  
(**unguided sampling**)

Difficult light transport  
(**guided sampling**)



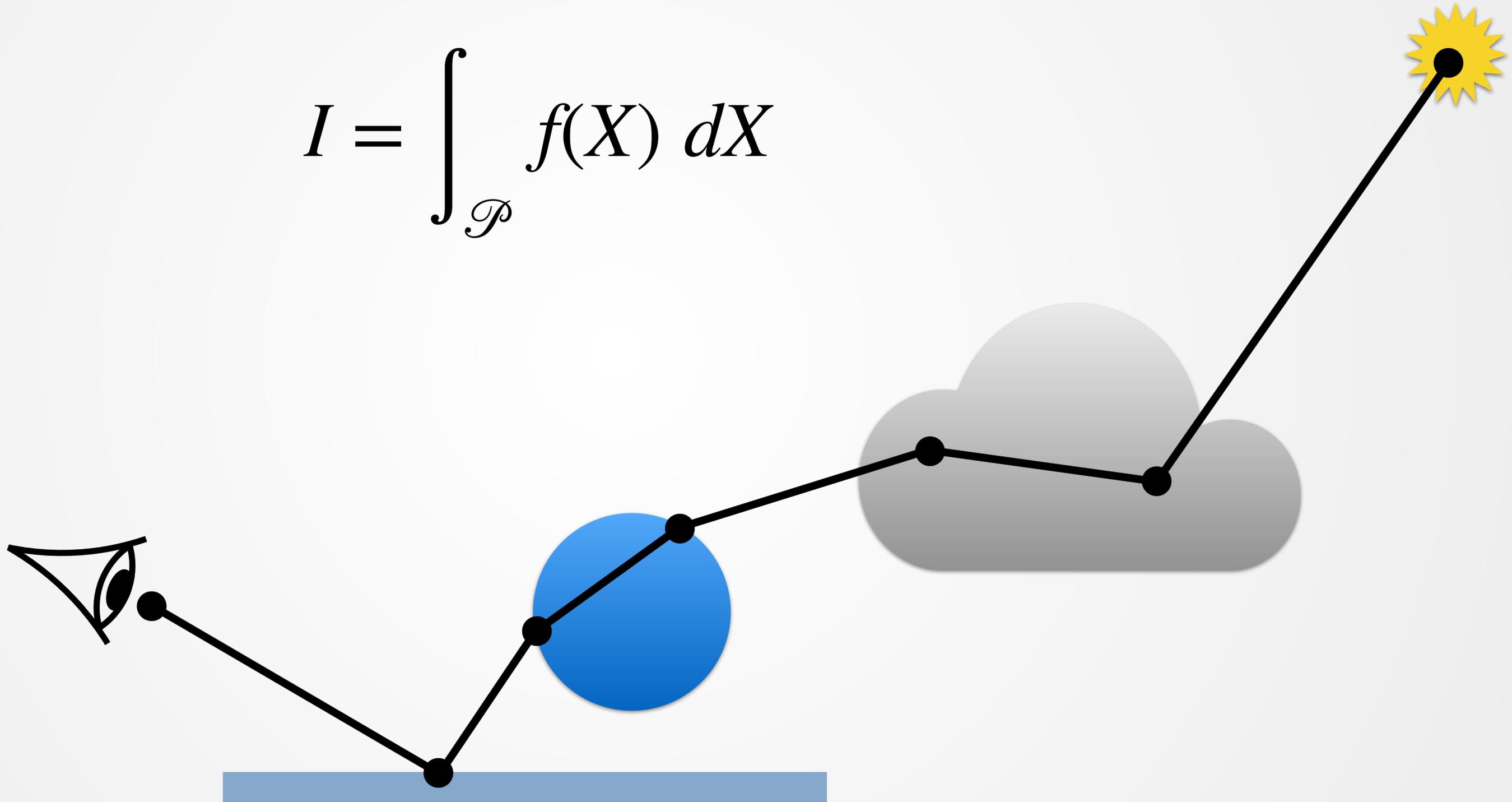
# Recent related guiding methods



- Vorba et al. [2014], Müller et al. [2017], ...
  - path guiding using incident radiance information
- Product sampling (Herholtz et al. [2016]) and application to participating media is not straight forward

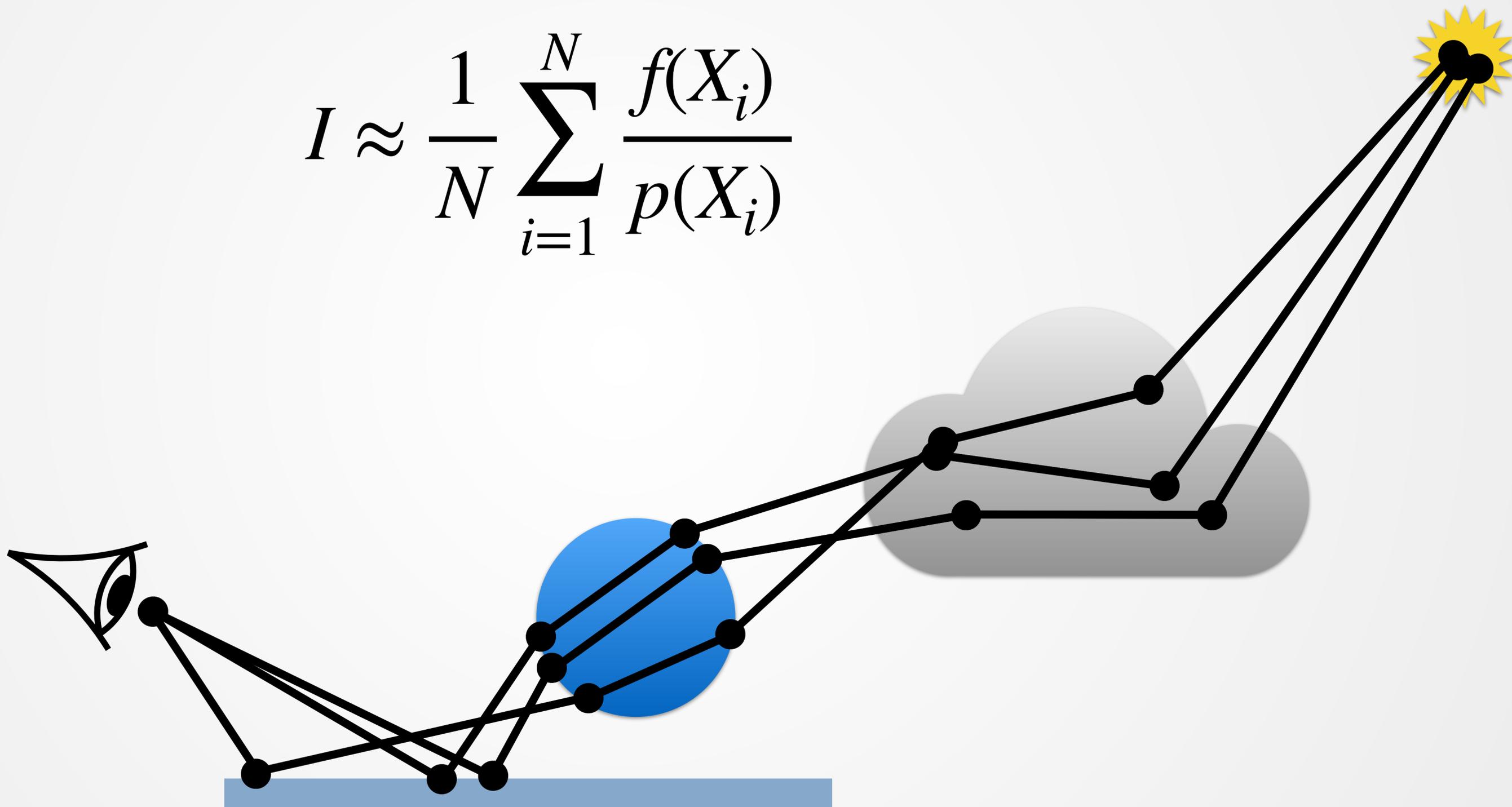
# Path Integral

$$I = \int_{\mathcal{P}} f(X) dX$$



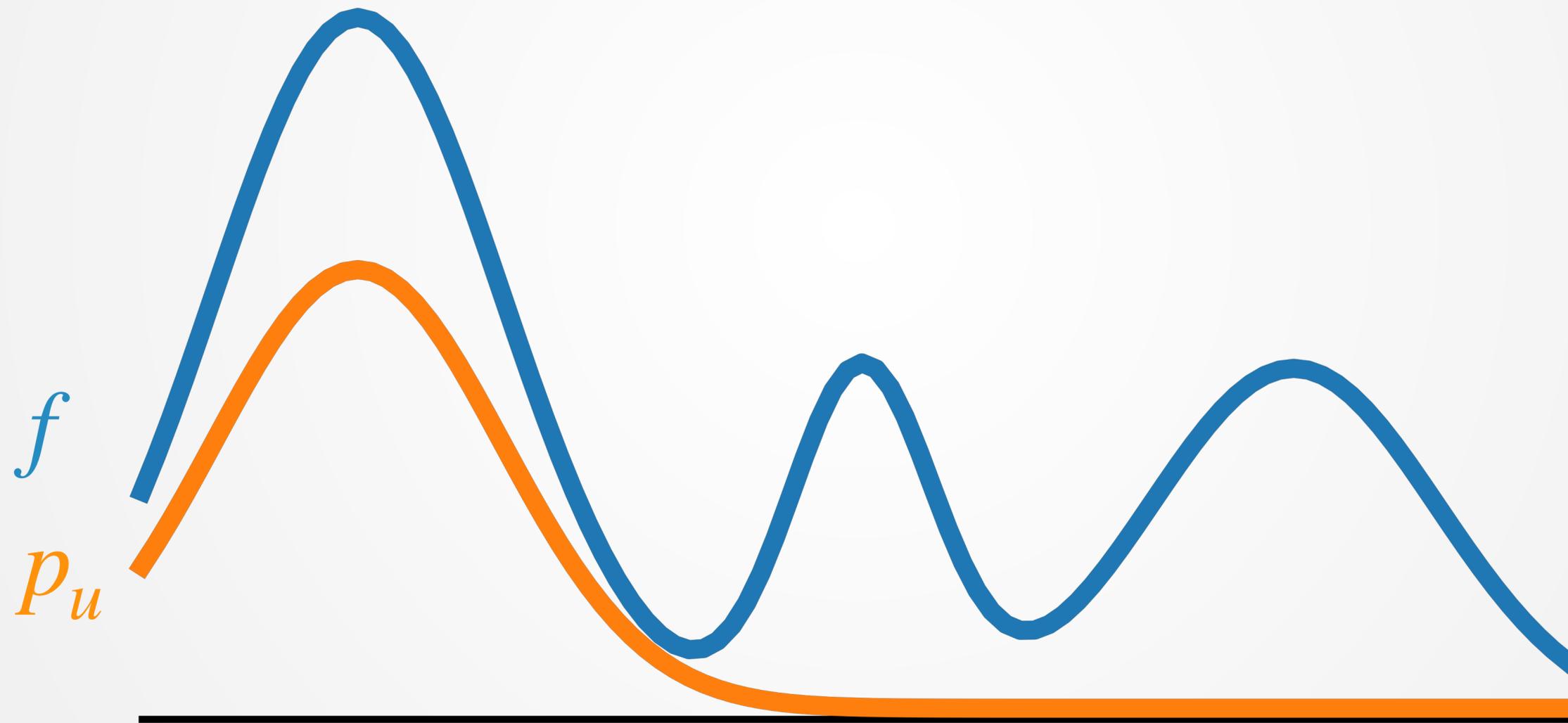
# Monte Carlo Integration

$$I \approx \frac{1}{N} \sum_{i=1}^N \frac{f(X_i)}{p(X_i)}$$



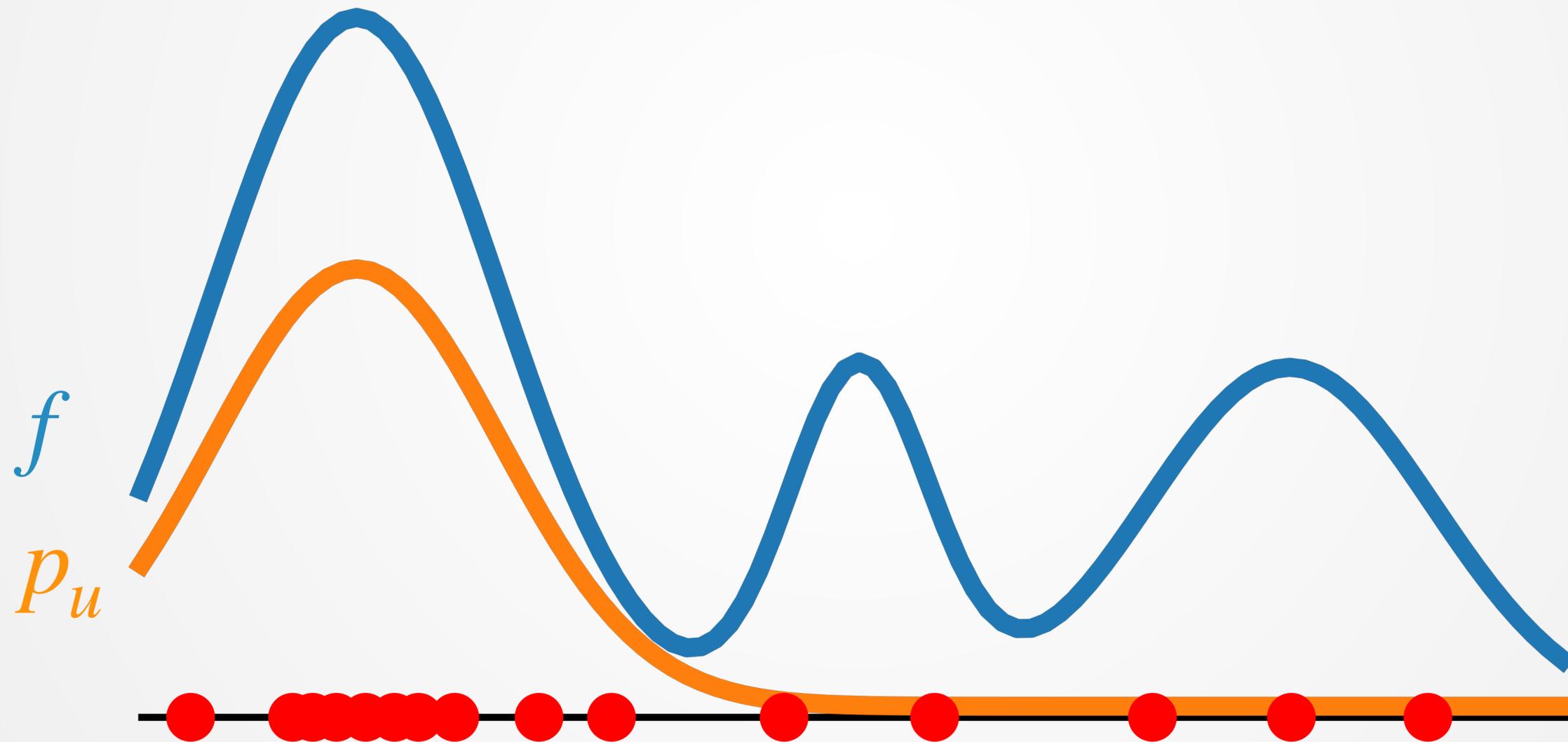
# Illustration in 1D

- Importance sampling?



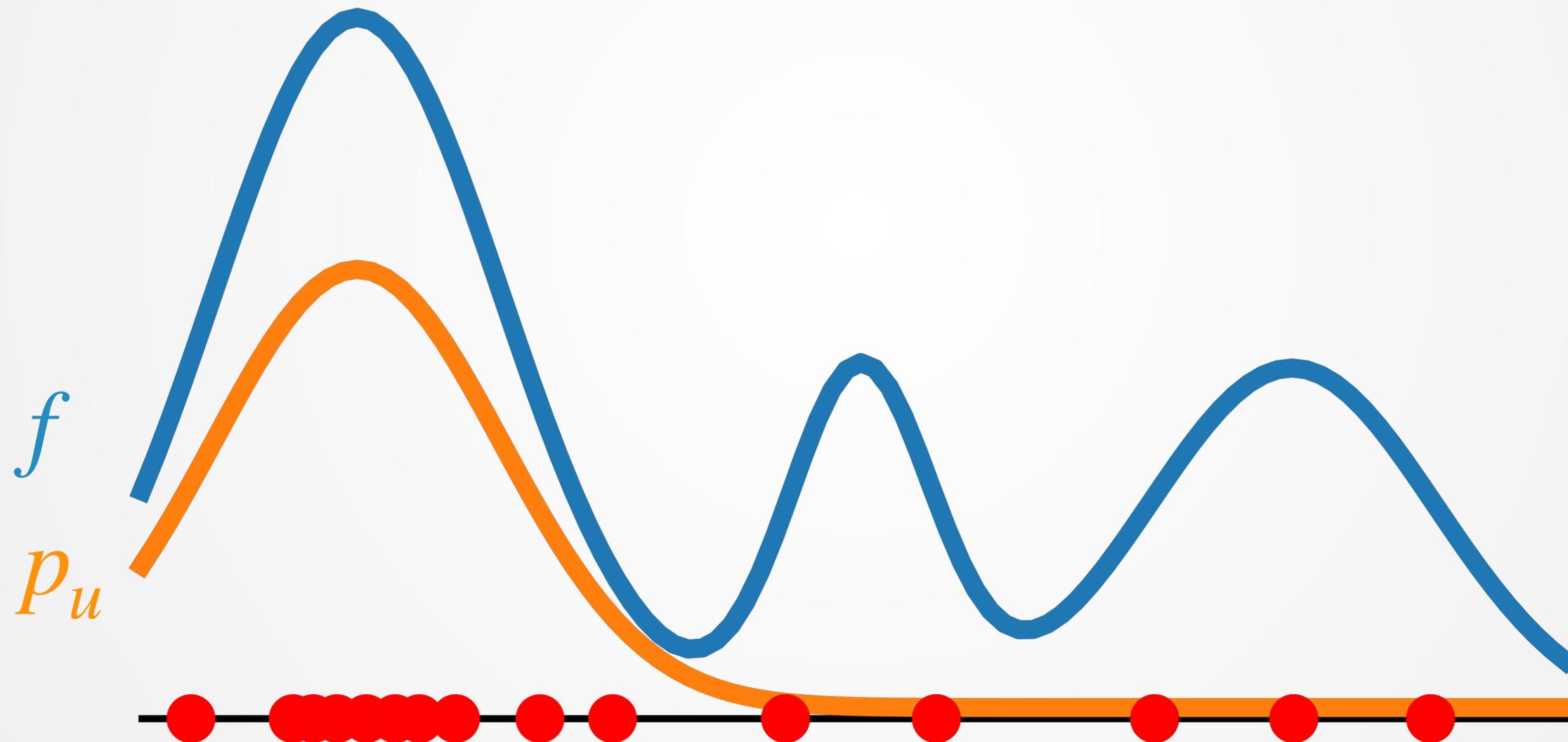
# Guided Sampling in 1D

- Create samples  $X_i \sim p_u$



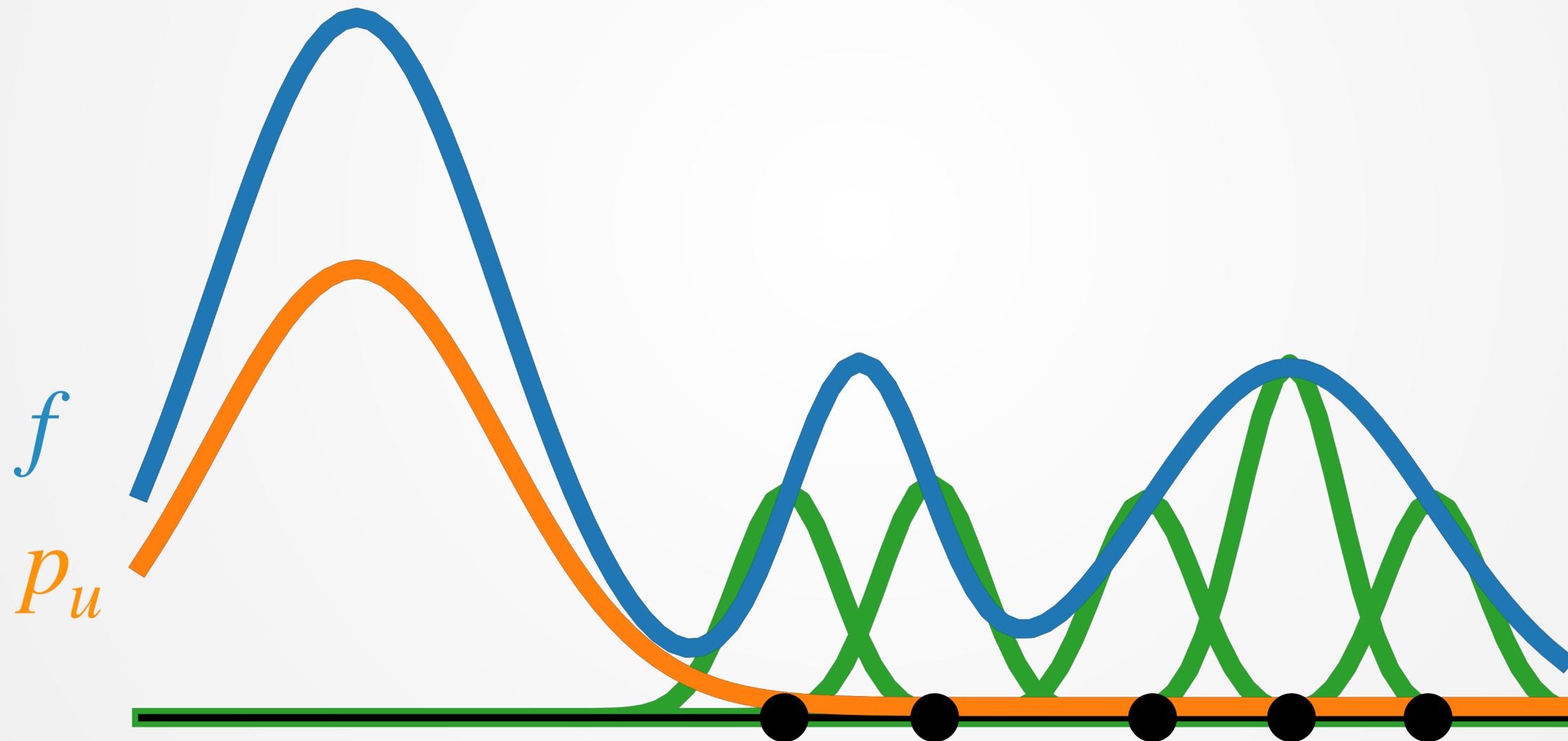
# Guided Sampling in 1D

- Keep outliers



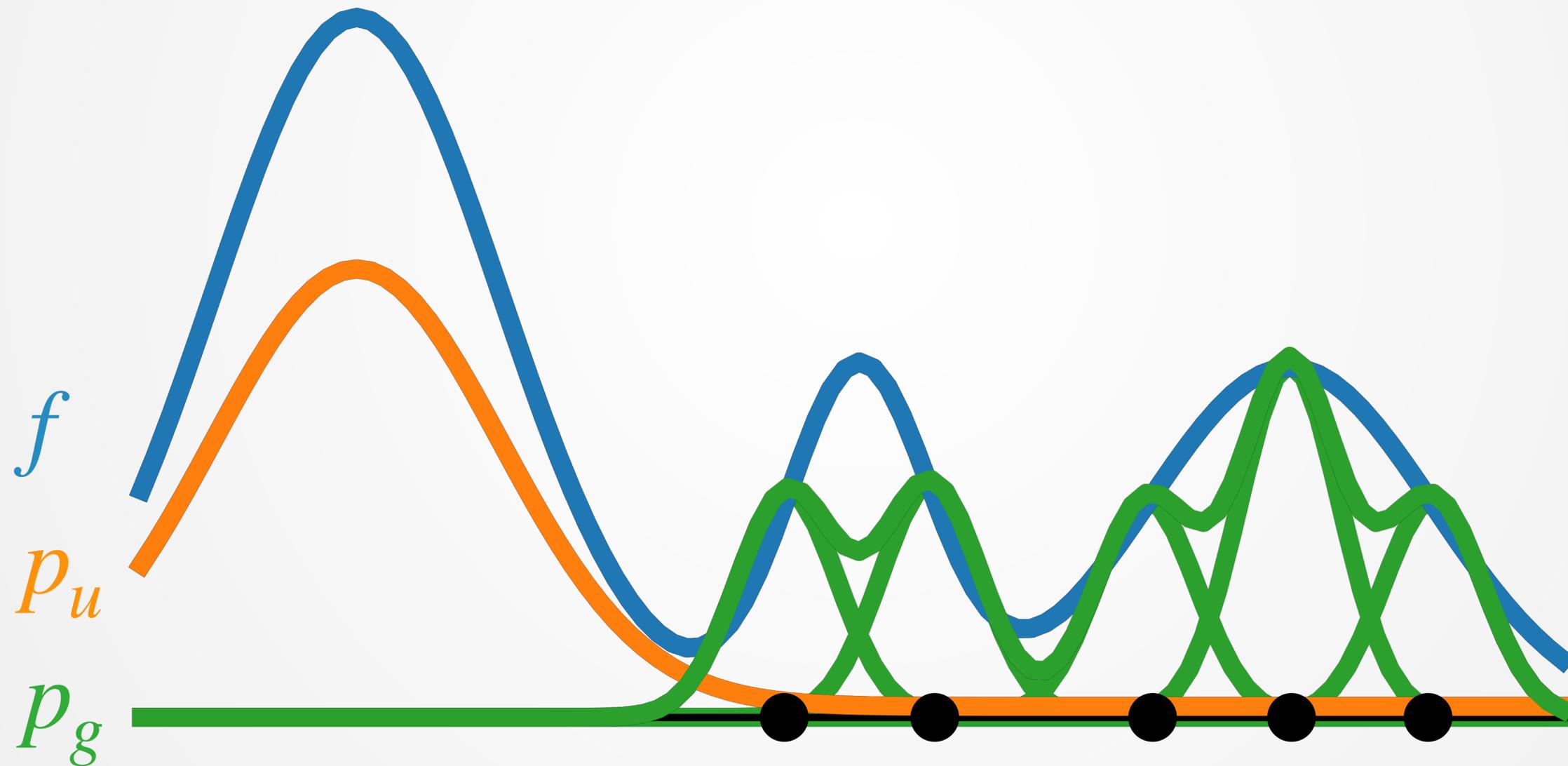
# Guided Sampling in 1D

- Place a Gaussian around each outlier



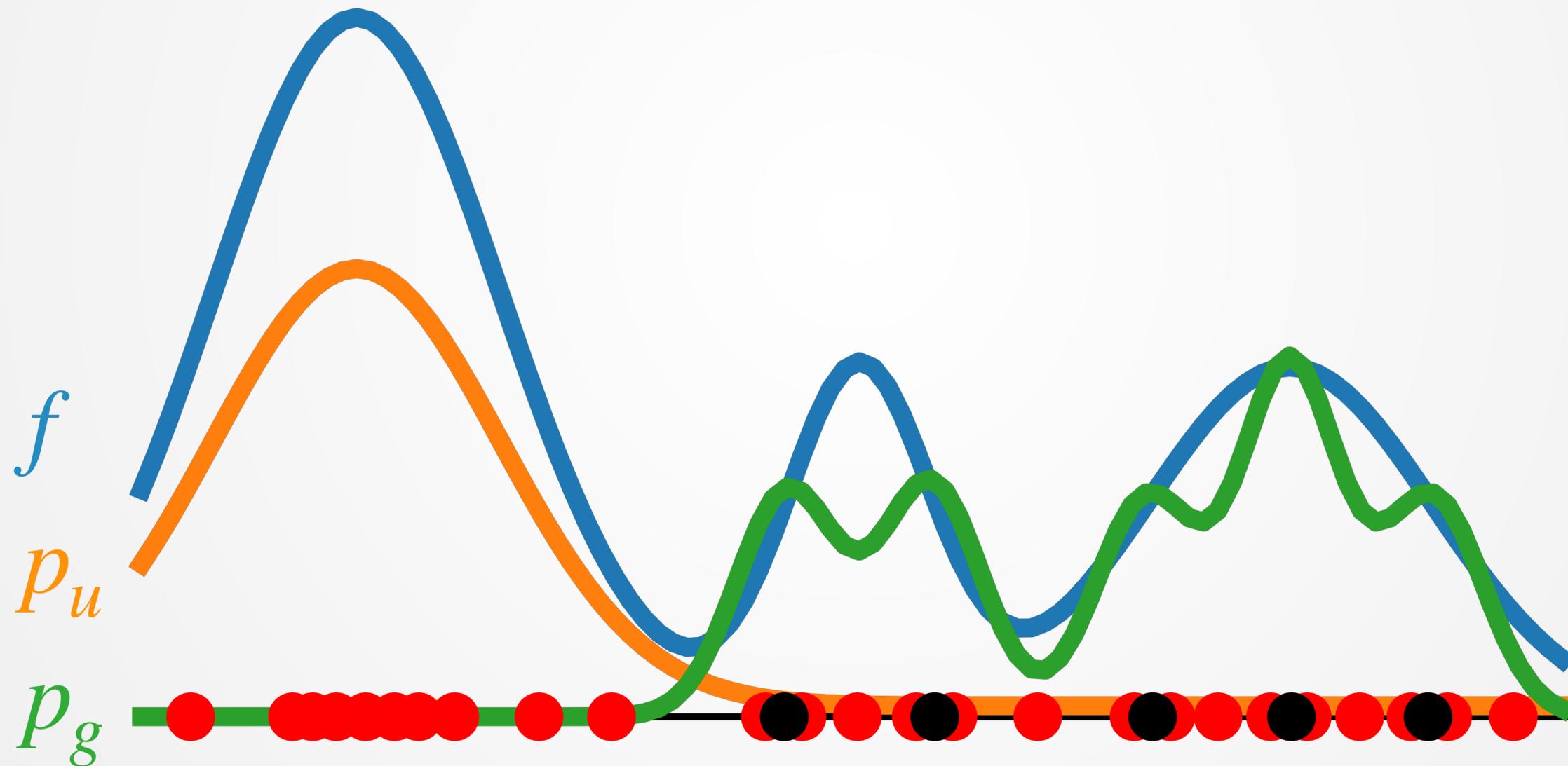
# Guided Sampling in 1D

- Define guided PDF as sum over all Gaussians



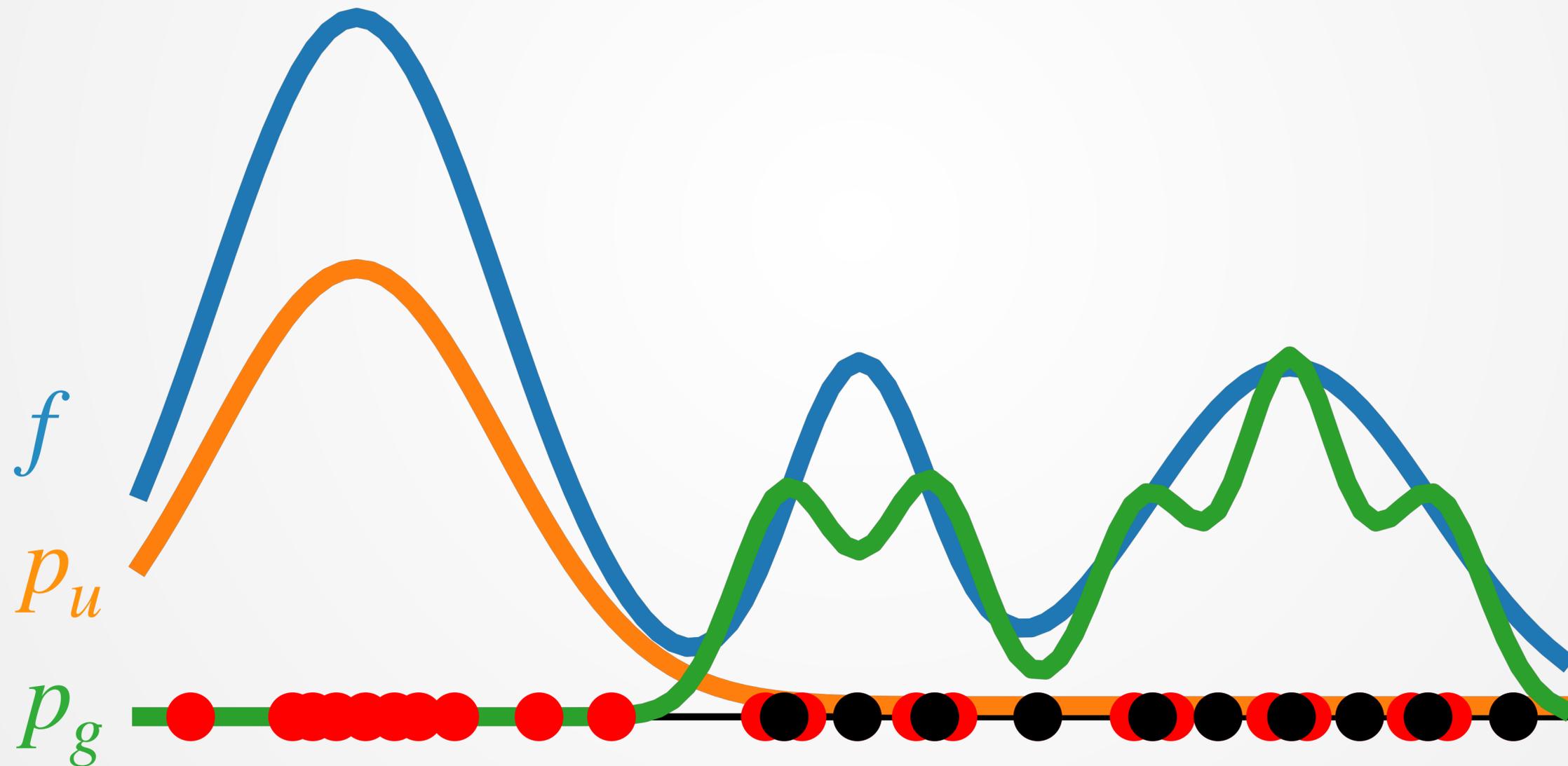
# Guided Sampling in 1D

- Iterate by sampling  $p_u$  and  $p_g$



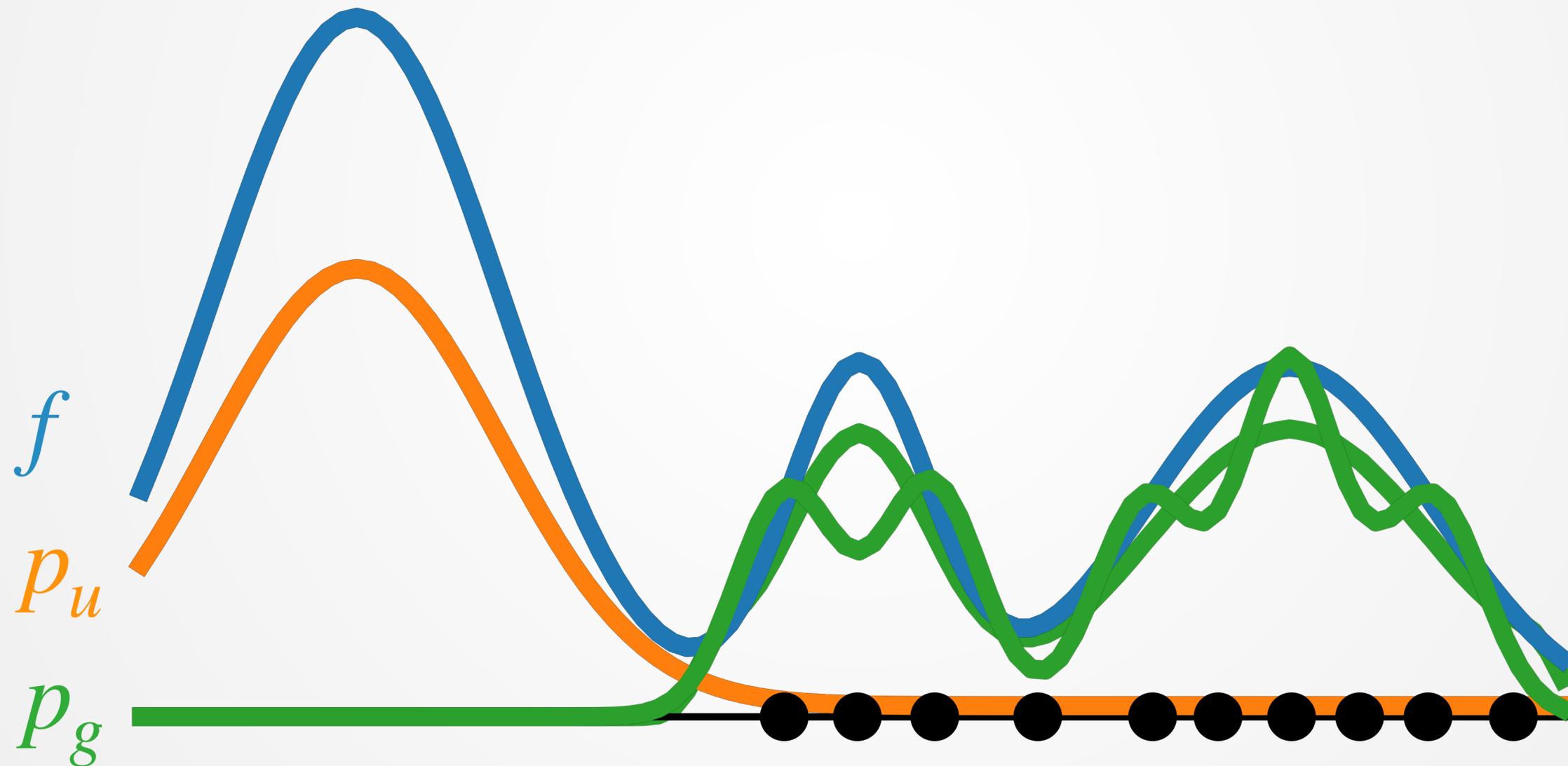
# Guided Sampling in 1D

- Keep outliers wrt.  $p_u$  and  $p_g$



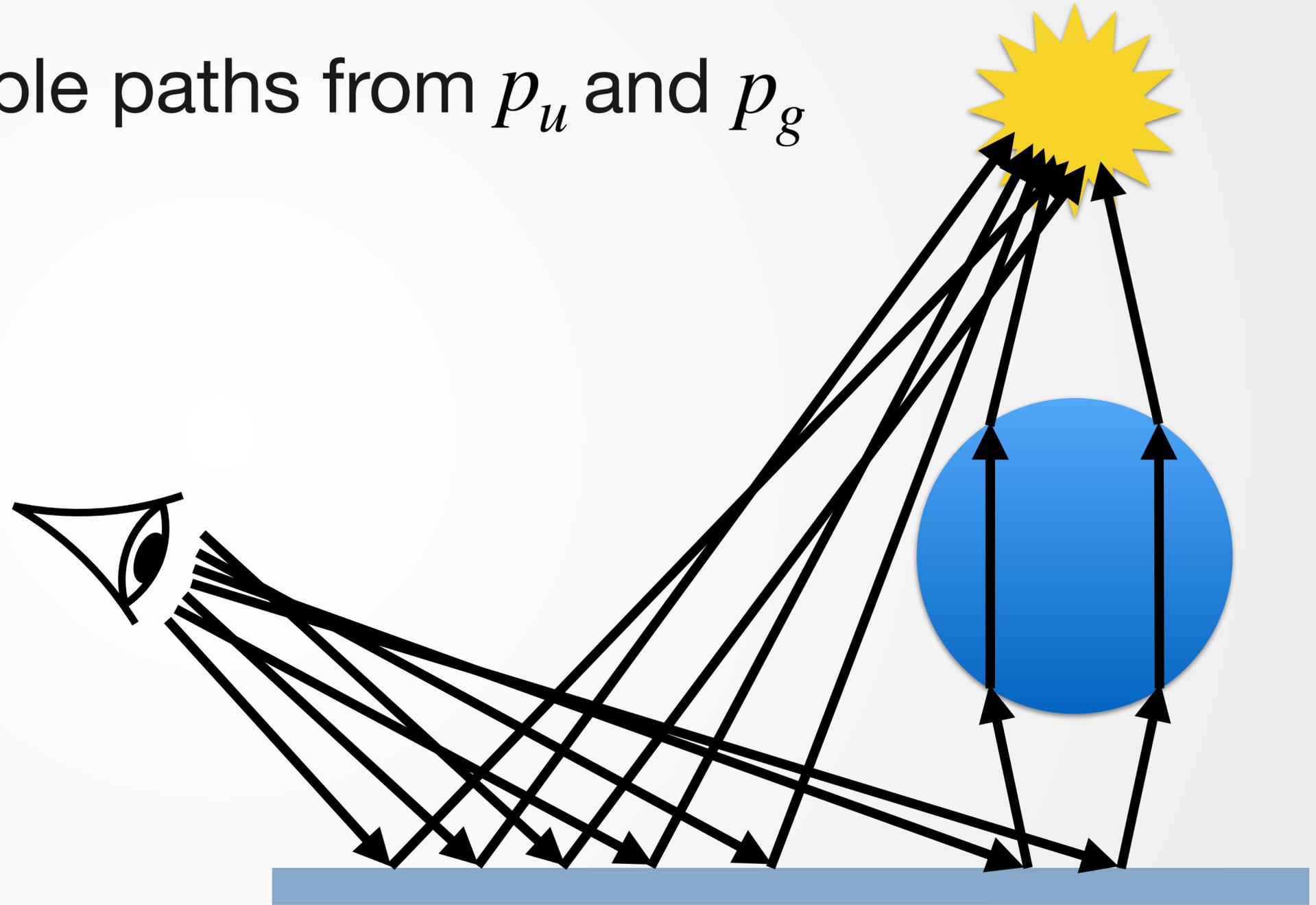
# Guided Sampling in 1D

- Update  $p_g$



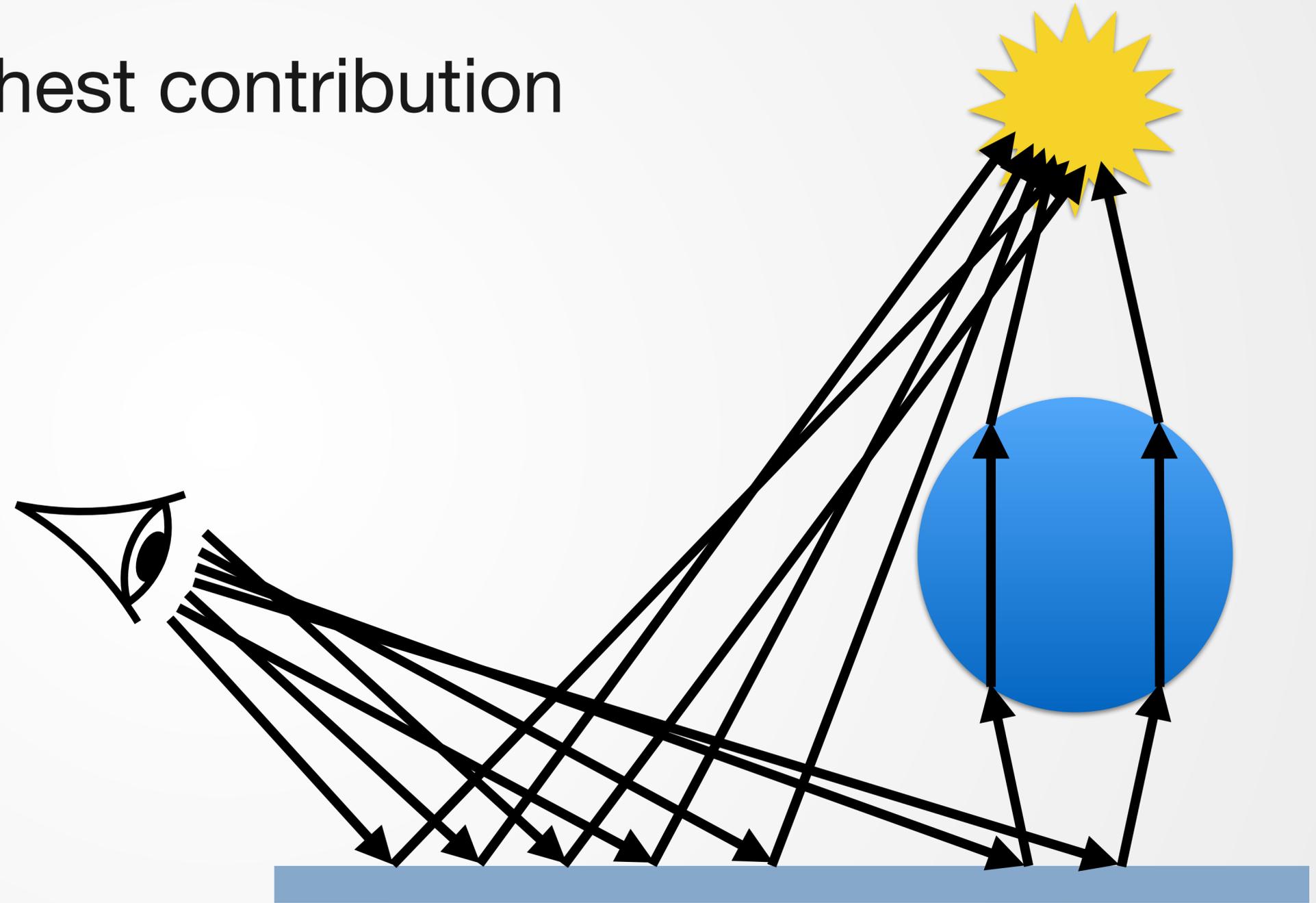
# Guiding Overview

- In each iteration, sample paths from  $p_u$  and  $p_g$



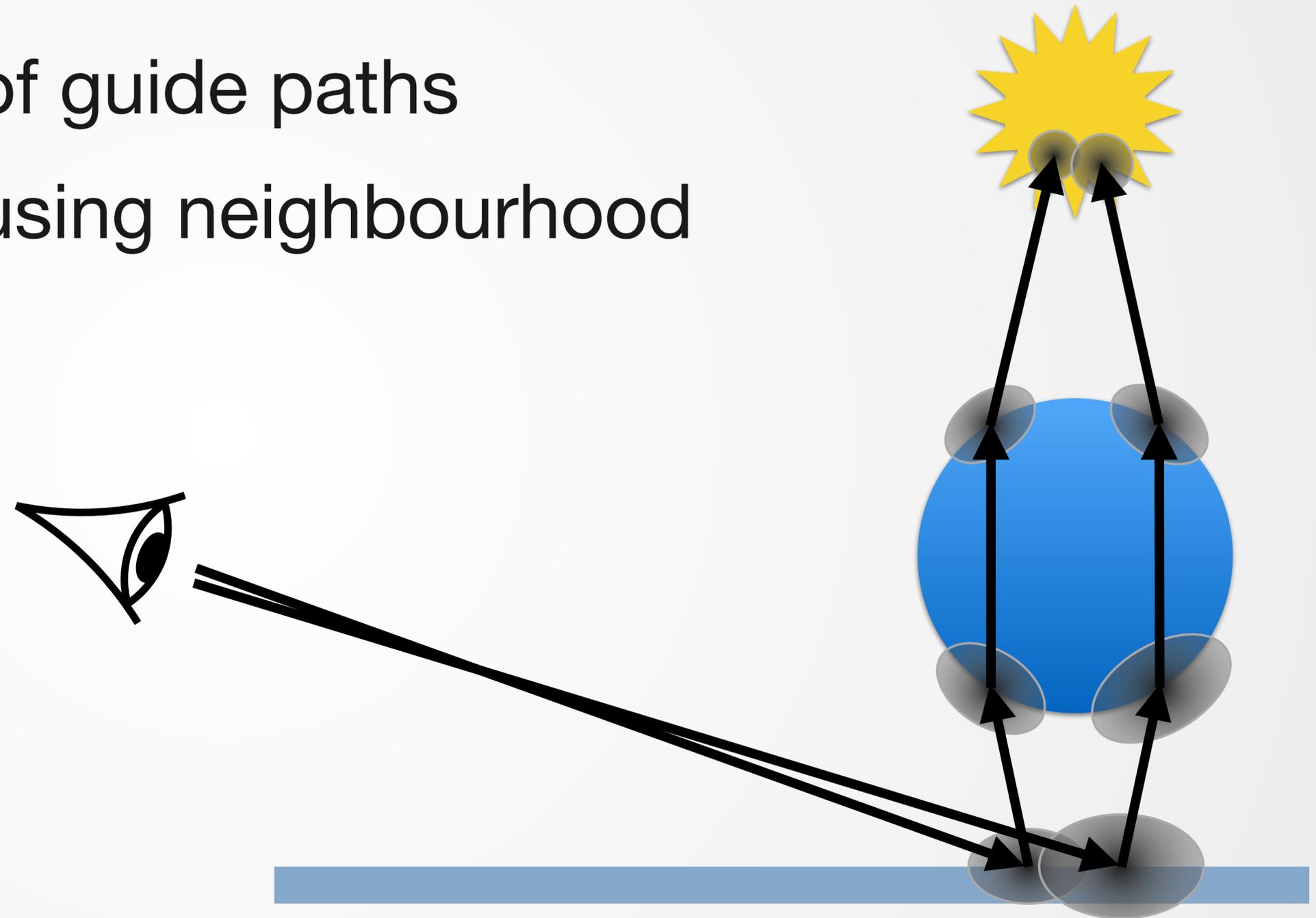
# Guiding Overview

- Keep outliers with highest contribution



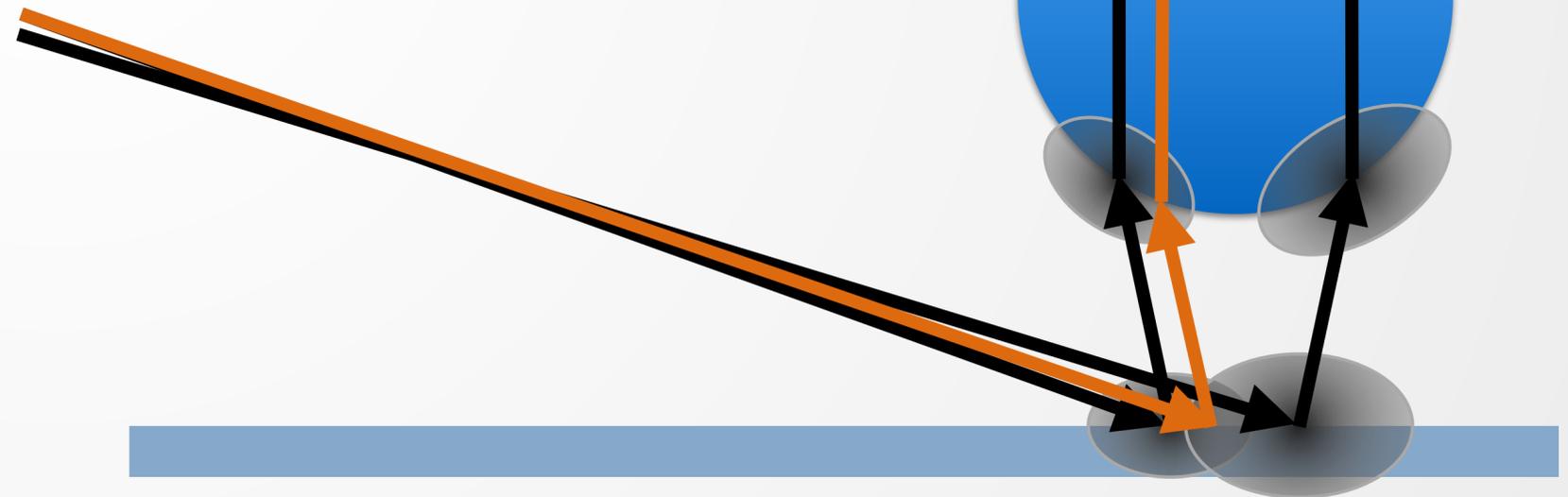
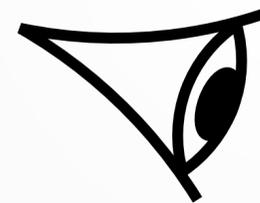
# Guiding Overview

- Add paths to the set of guide paths
- Compute Gaussians using neighbourhood information



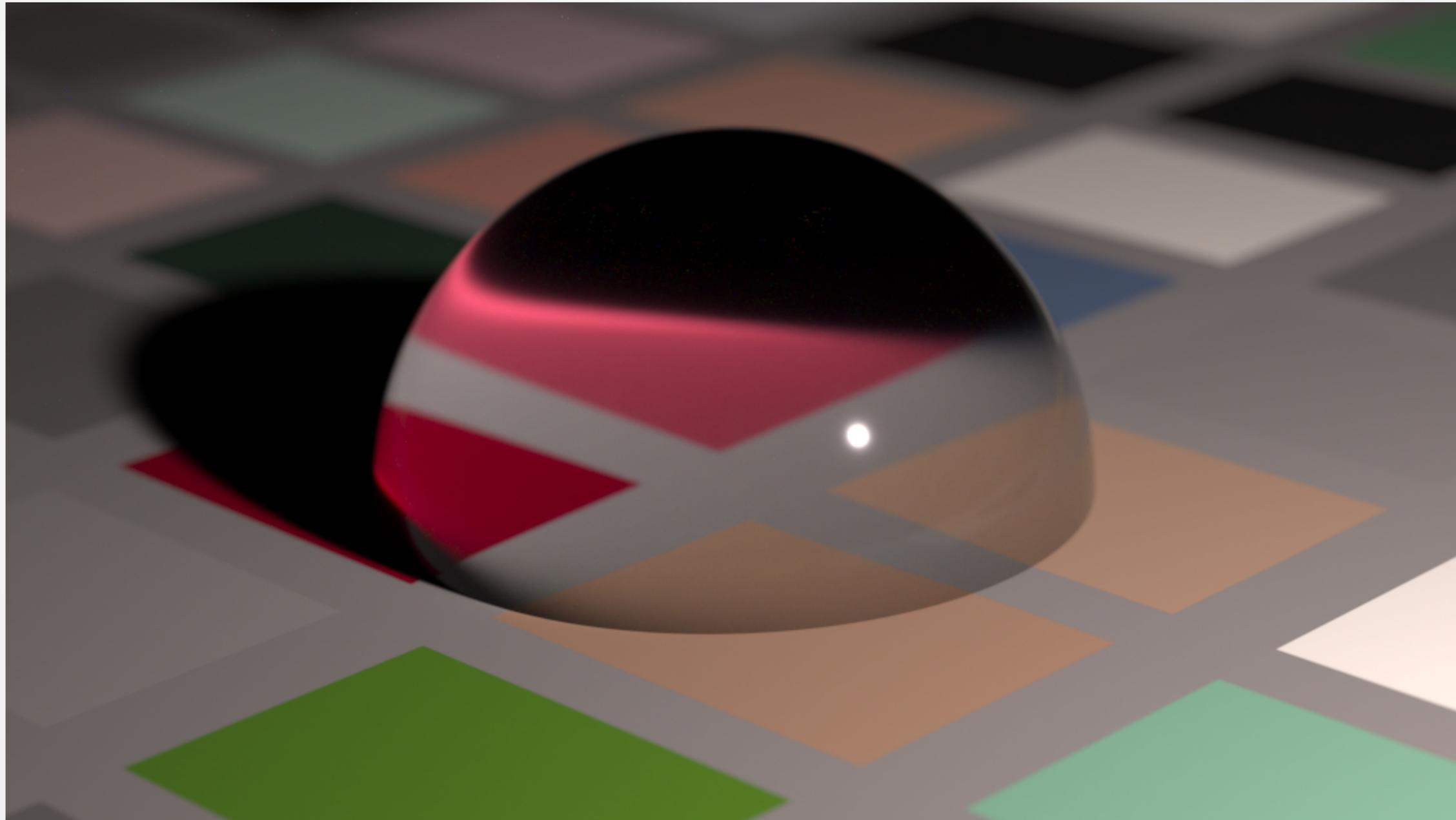
# Guiding Overview

- Guided sampling:
  - Choose guide path randomly and
  - Sample Gaussians incrementally
- Guided and unguided sampling combined with multiple importance sampling



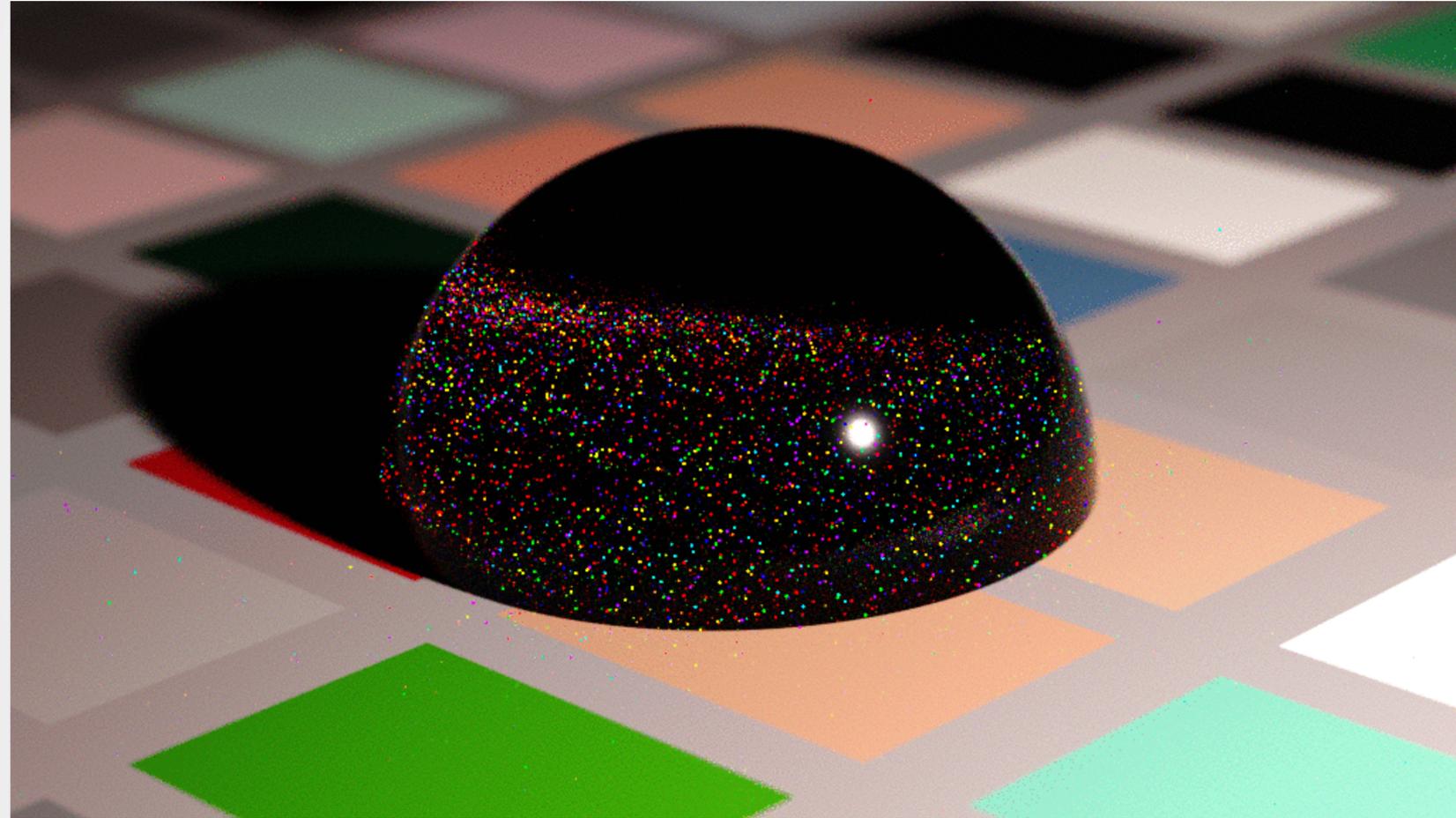
# Guiding Behaviour

Reference

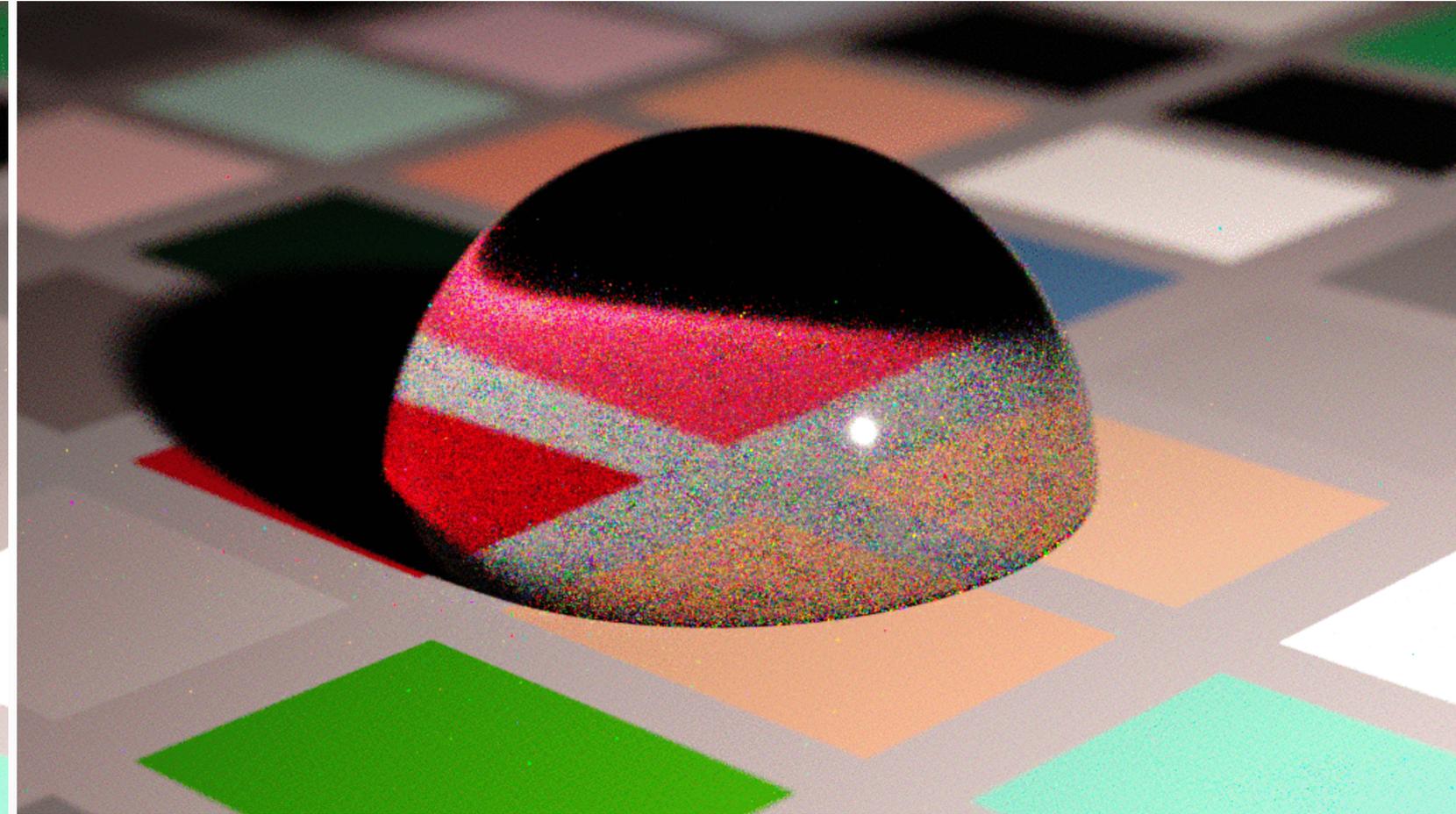


# Guiding Behaviour

## Path tracing

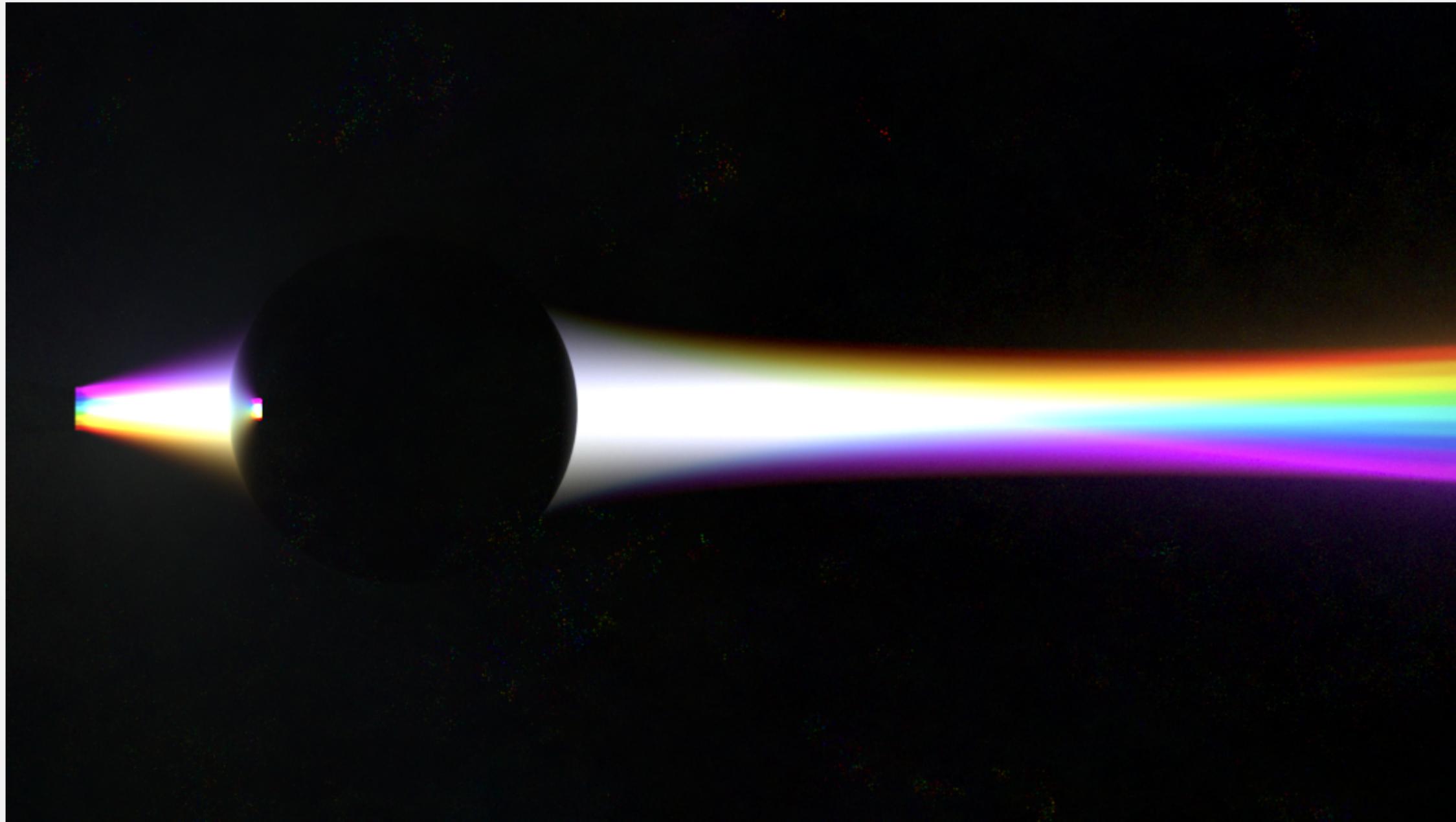


## Guided path tracing



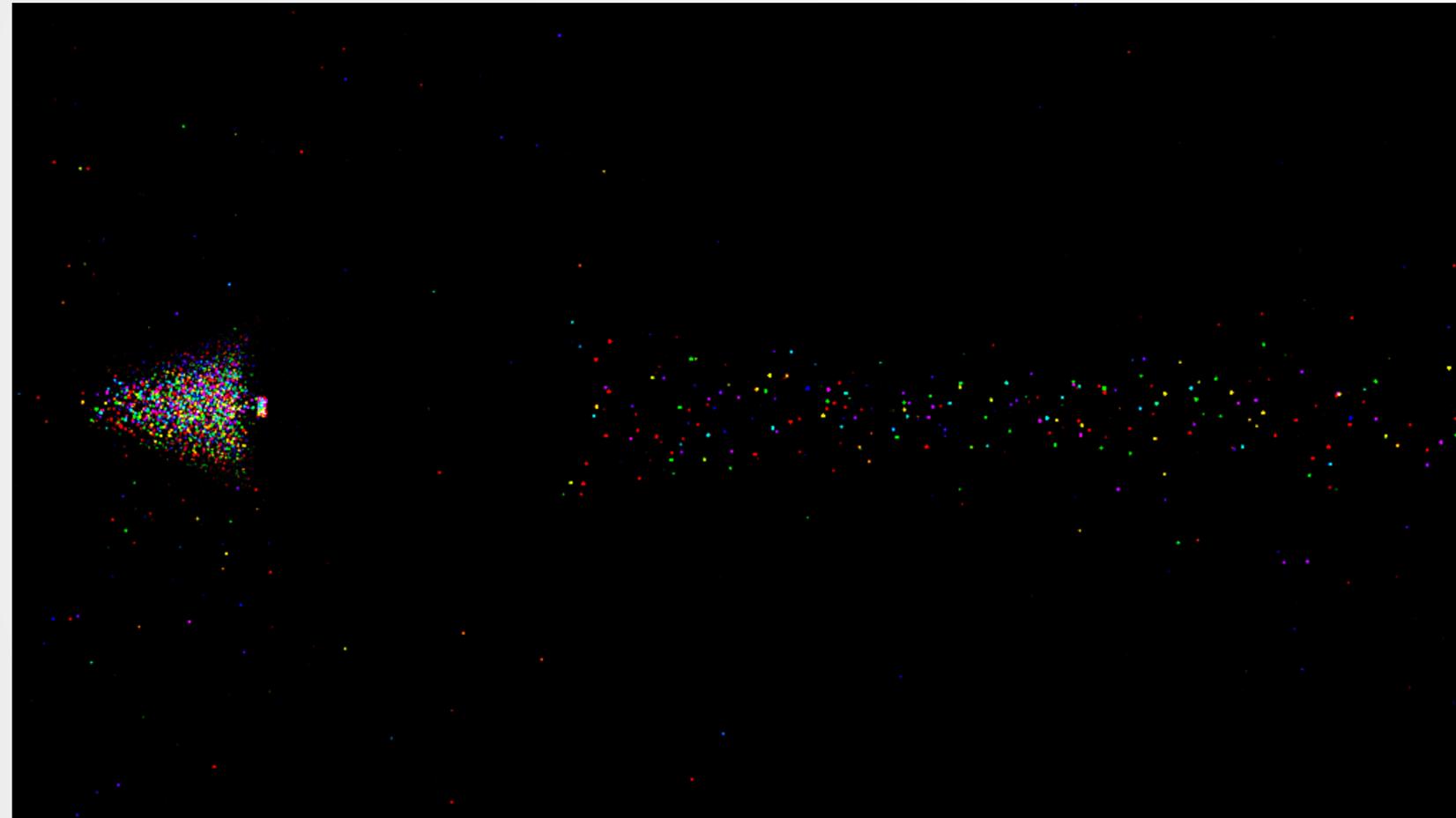
# Guiding Behaviour

Reference

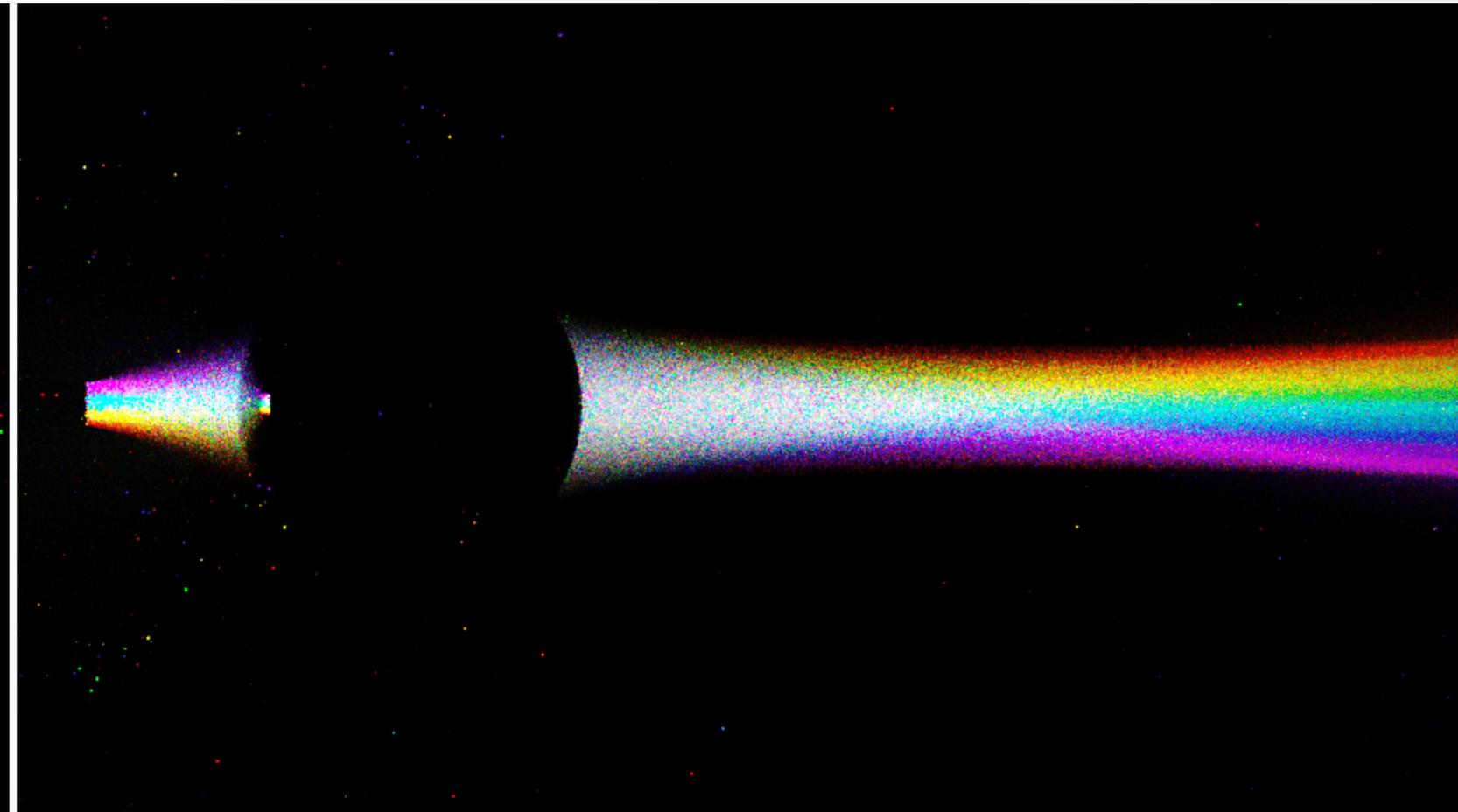


# Guiding Behaviour

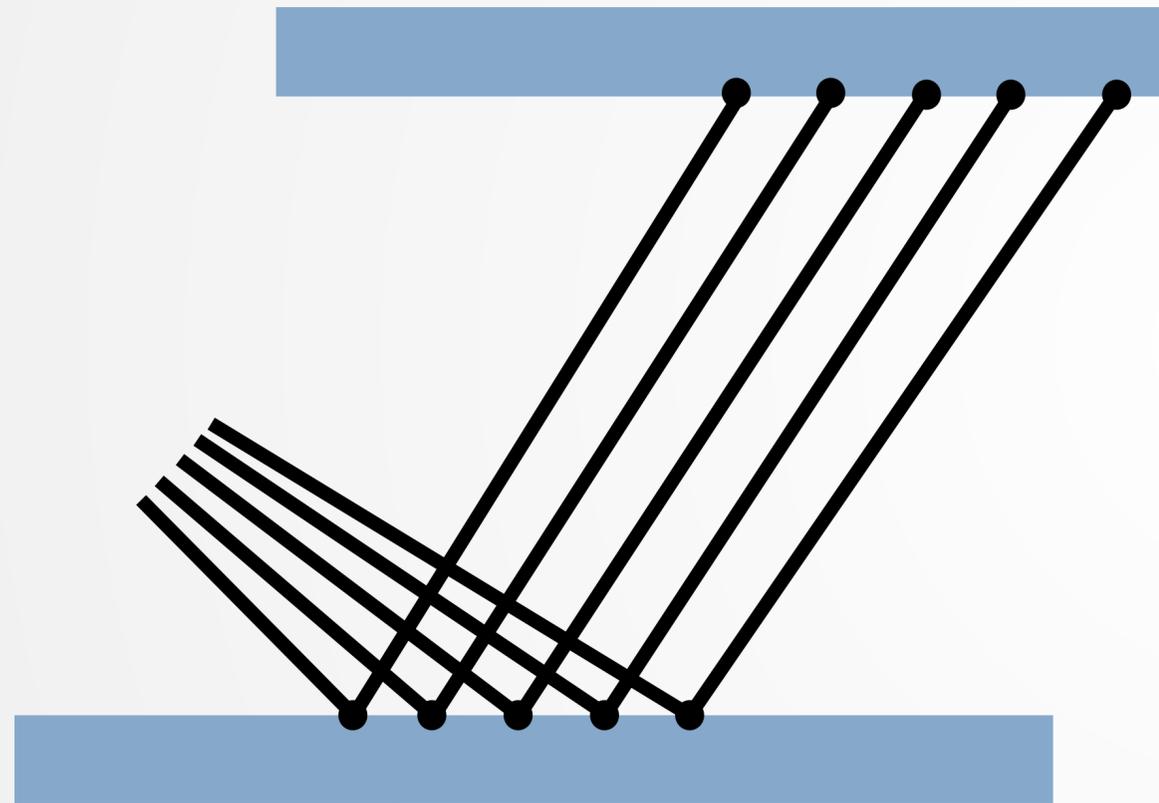
## Path tracing



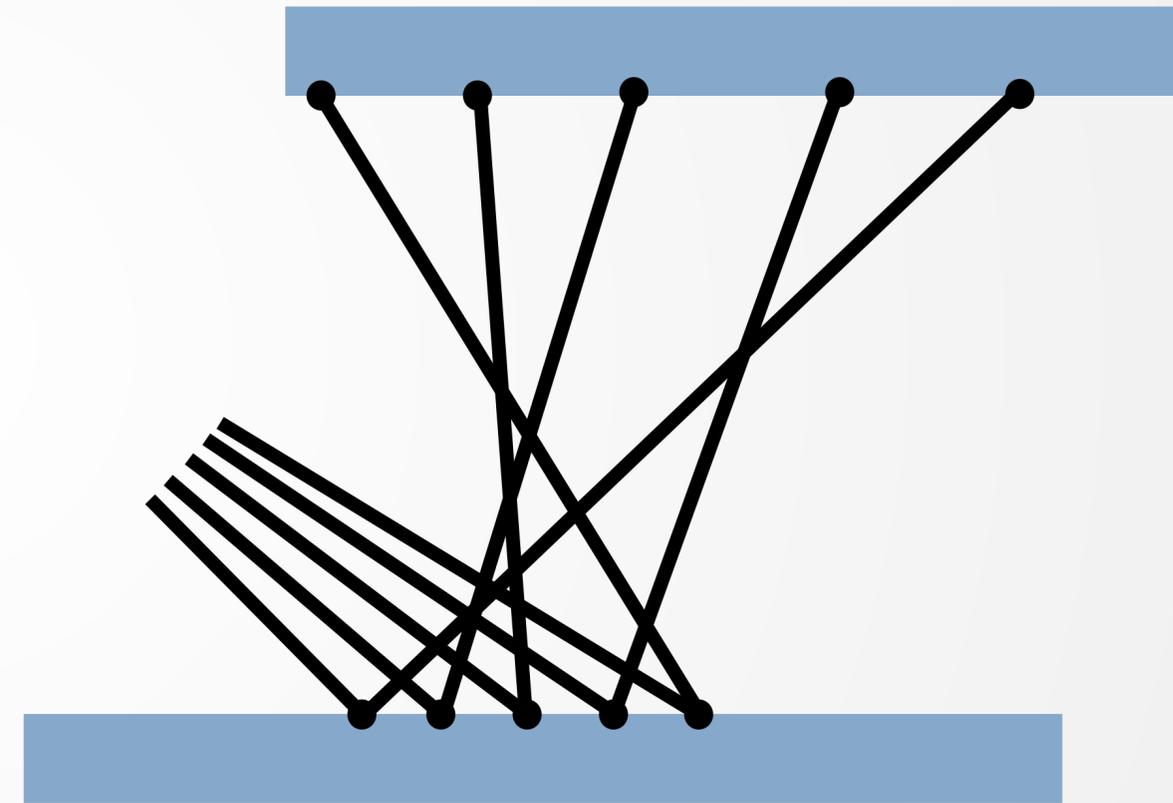
## Guided path tracing



# Path Correlation



Specular/glossy

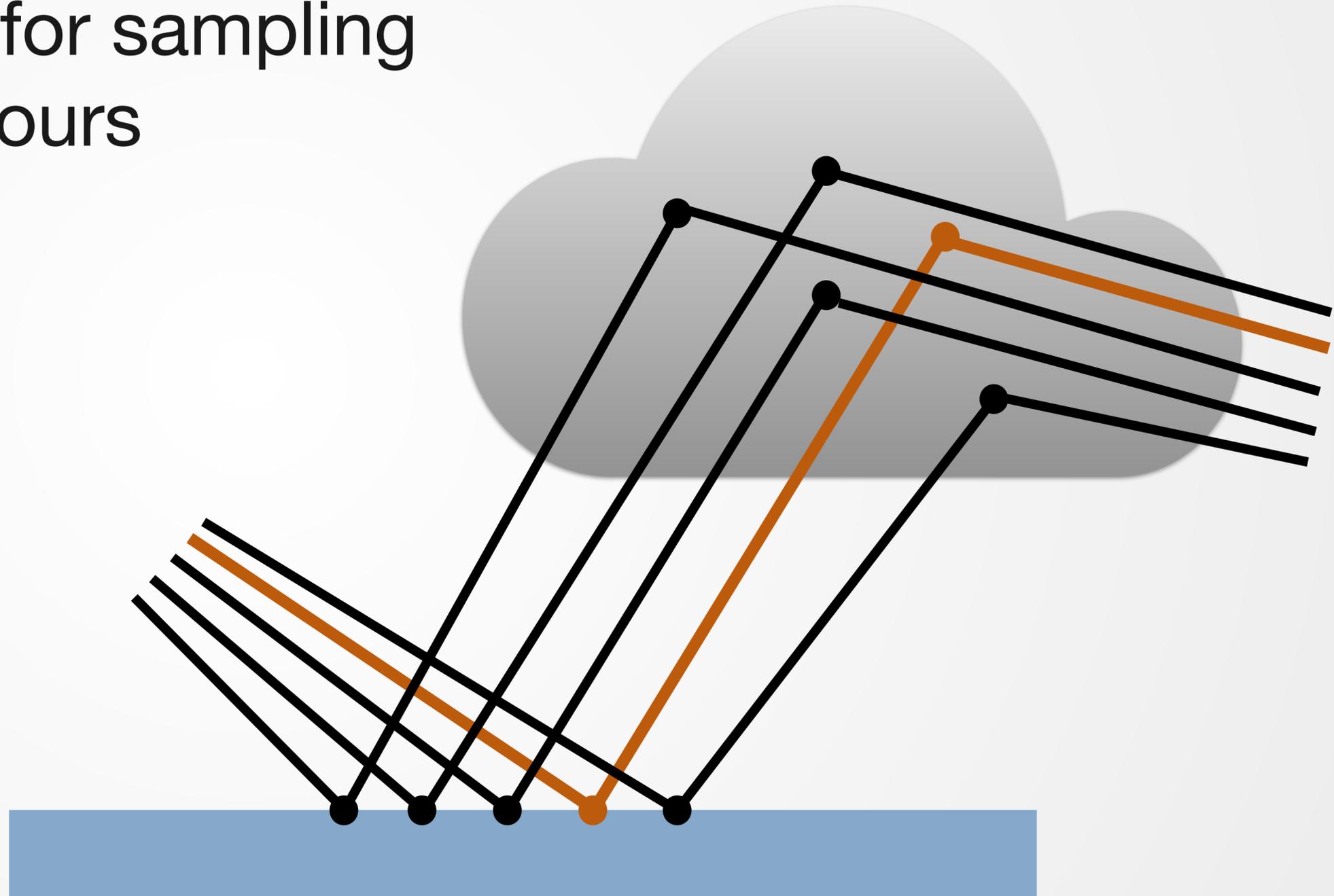


Rough/diffuse

# Gaussians

- Compute Gaussians for sampling using nearest neighbours

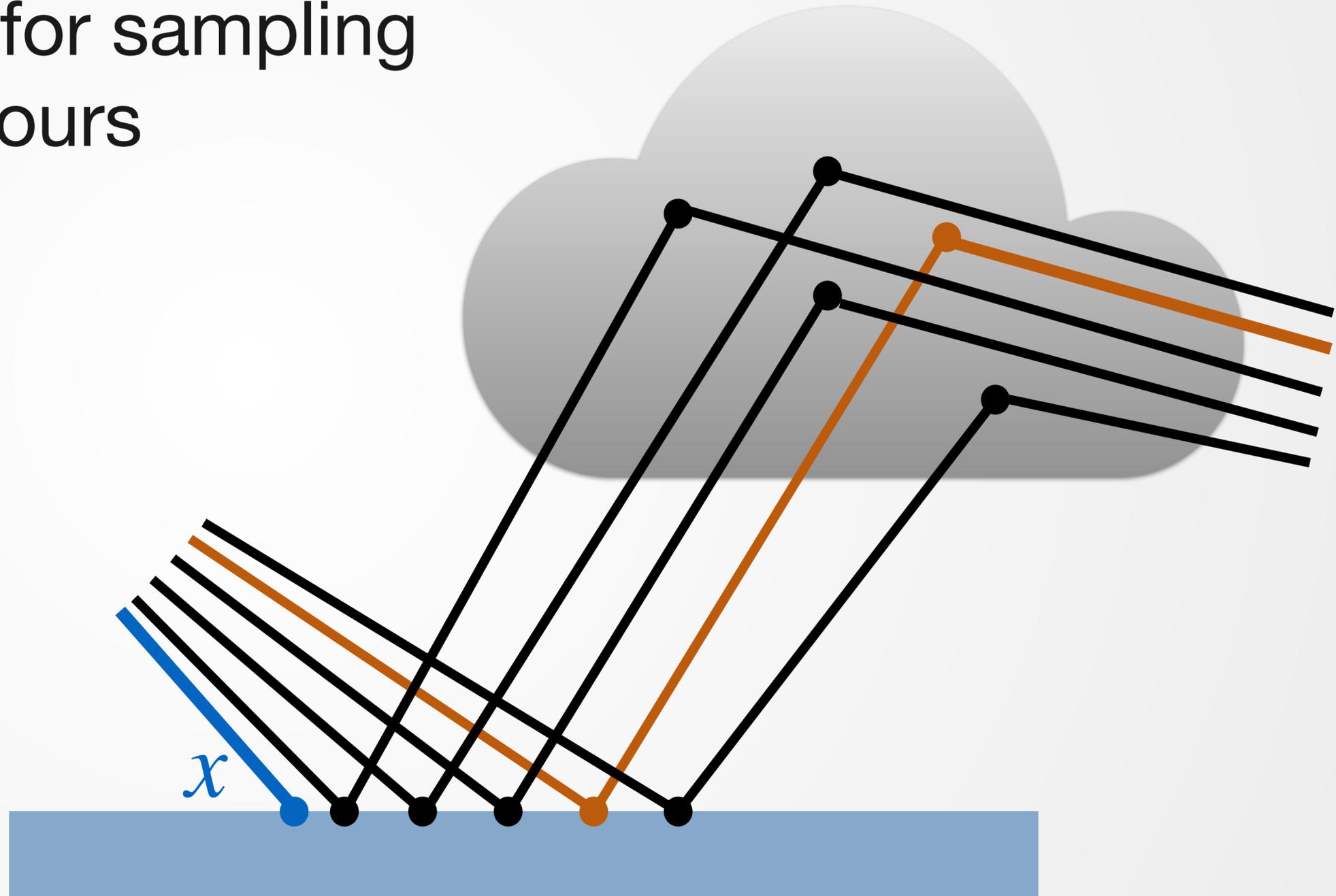
— Guide path  
— Nearest neighbours



# Gaussians

- Compute Gaussians for sampling using nearest neighbours

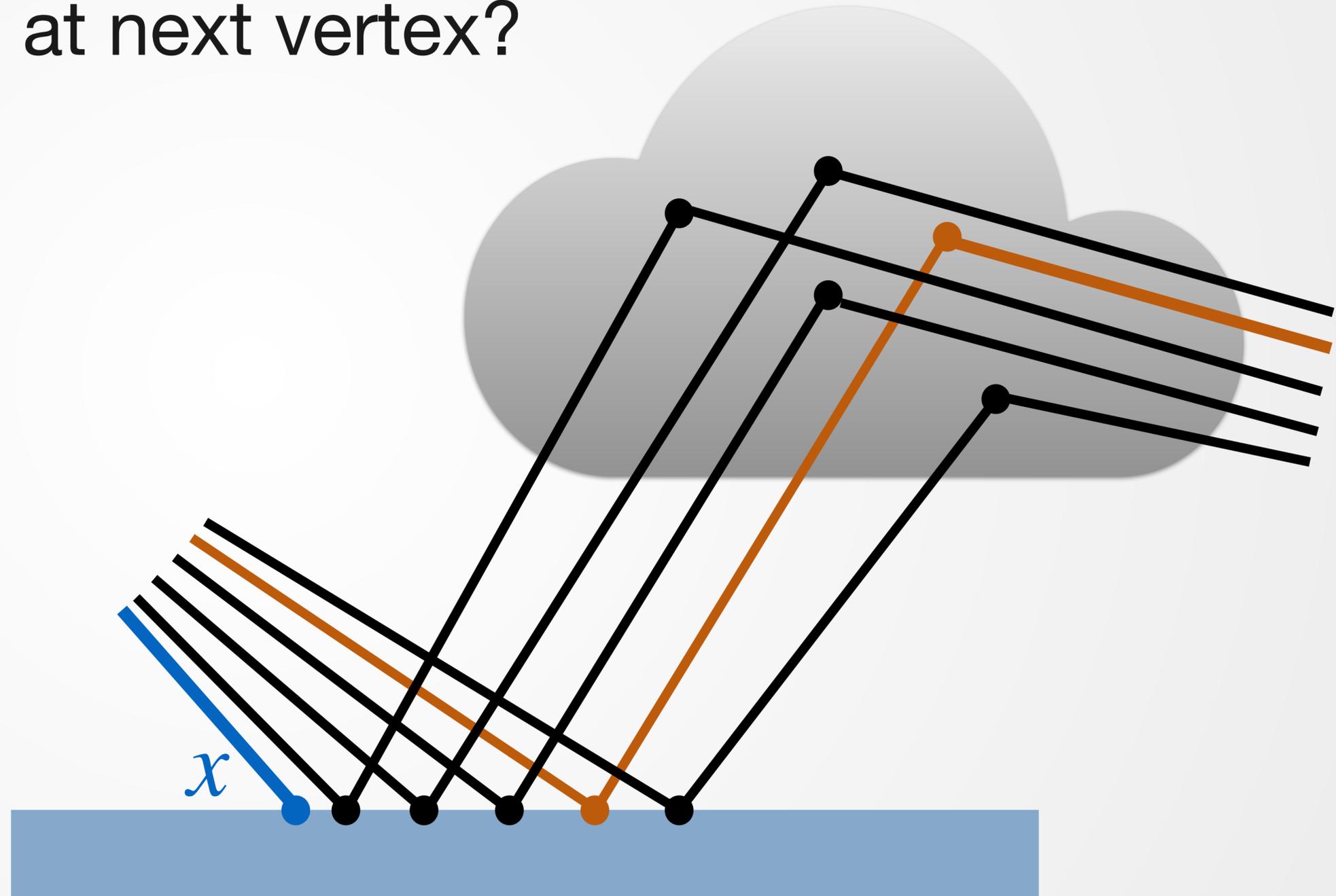
- Guide path
- Nearest neighbours
- New path



# Gaussians

- Sample 3D Gaussian at next vertex?

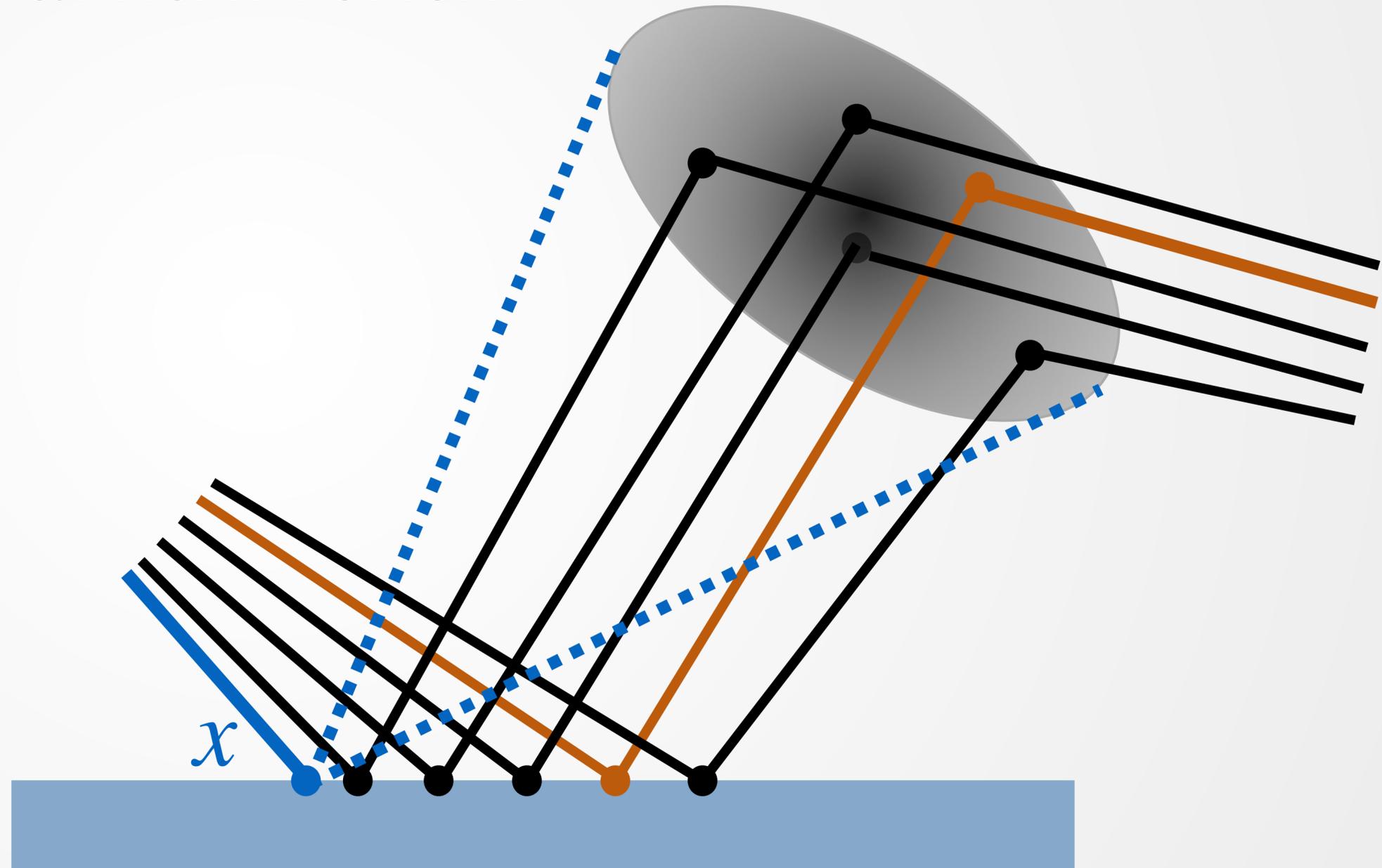
- Guide path
- Nearest neighbours
- New path



# Gaussians

- Sample 3D Gaussian at next vertex?

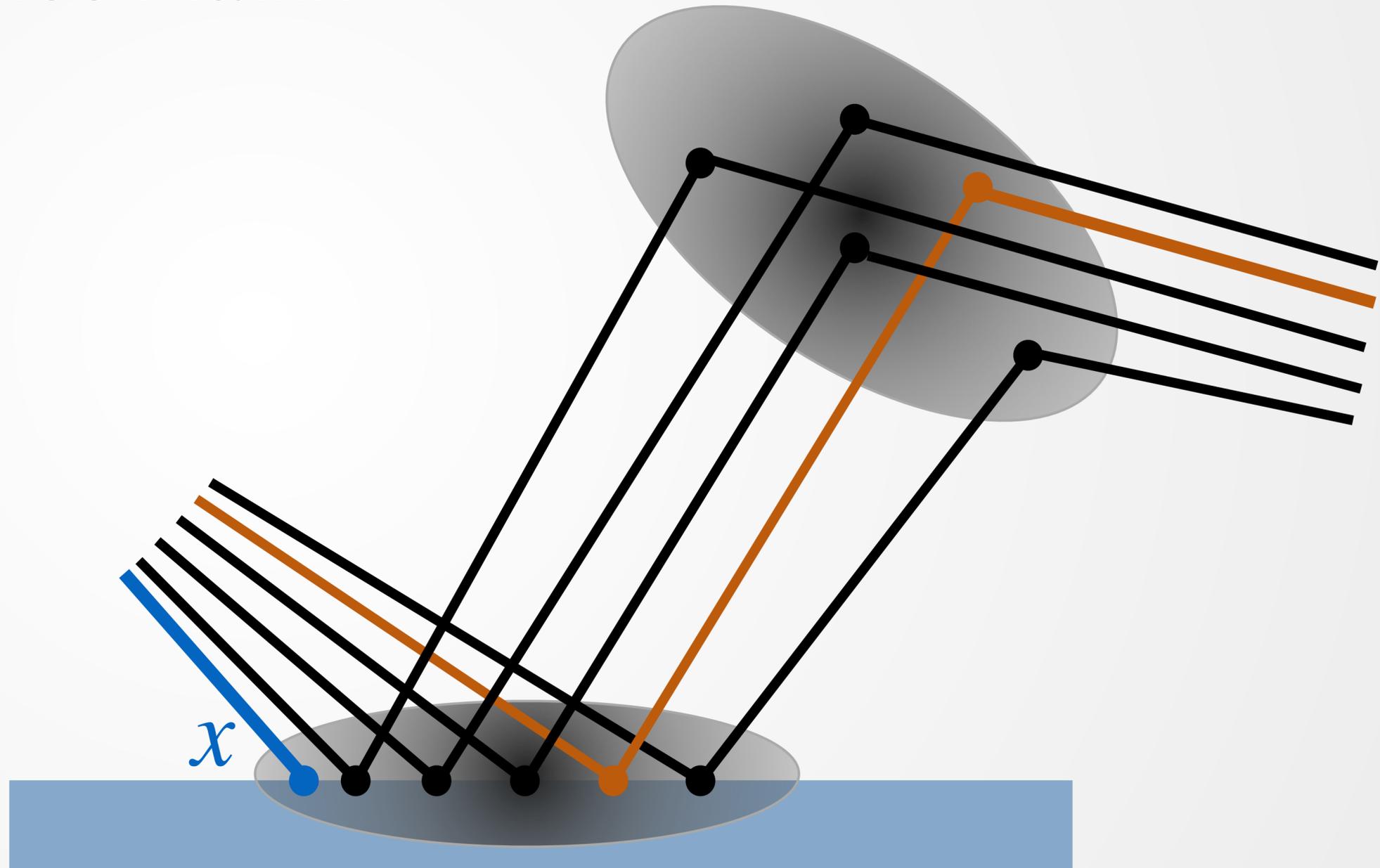
- Guide path
- Nearest neighbours
- New path



# Gaussians

- Compute 6D covariance matrix for path segments

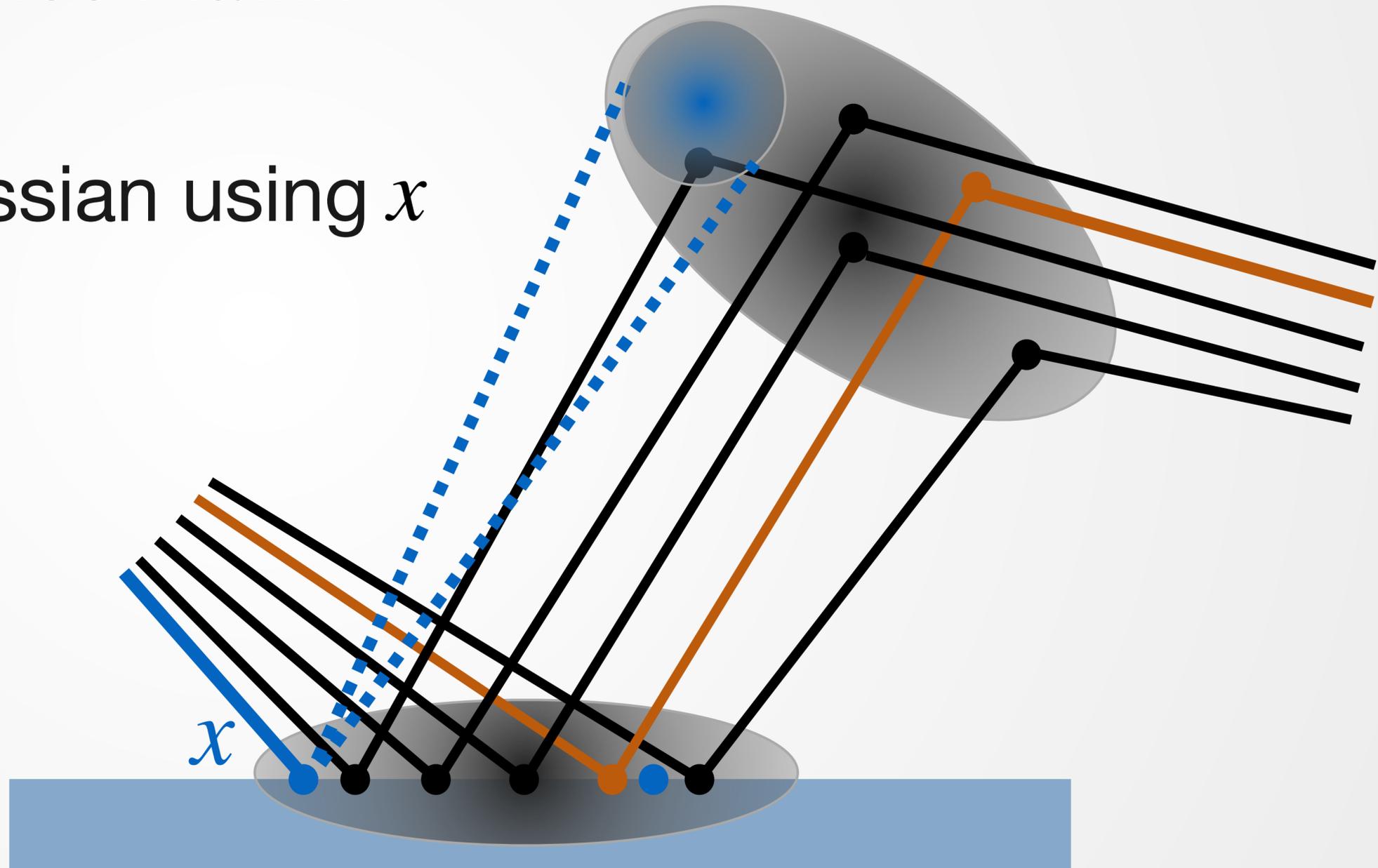
- Guide path
- Nearest neighbours
- New path



# Gaussians

- Compute 6D covariance matrix for path segments
- And conditional Gaussian using  $x$

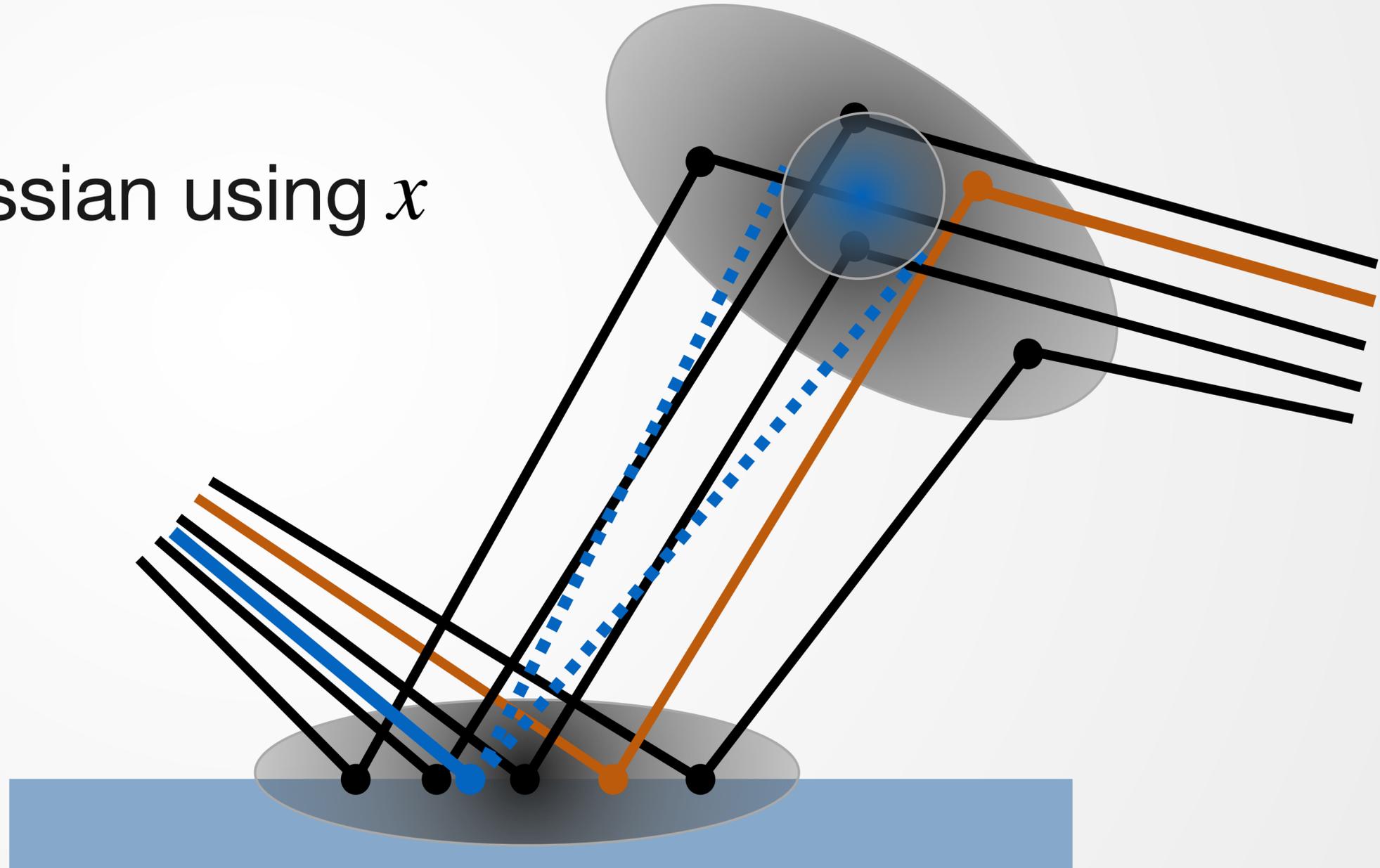
- Guide path
- Nearest neighbours
- New path



# Gaussians

- Compute 6D covariance matrix for path segments
- And conditional Gaussian using  $x$

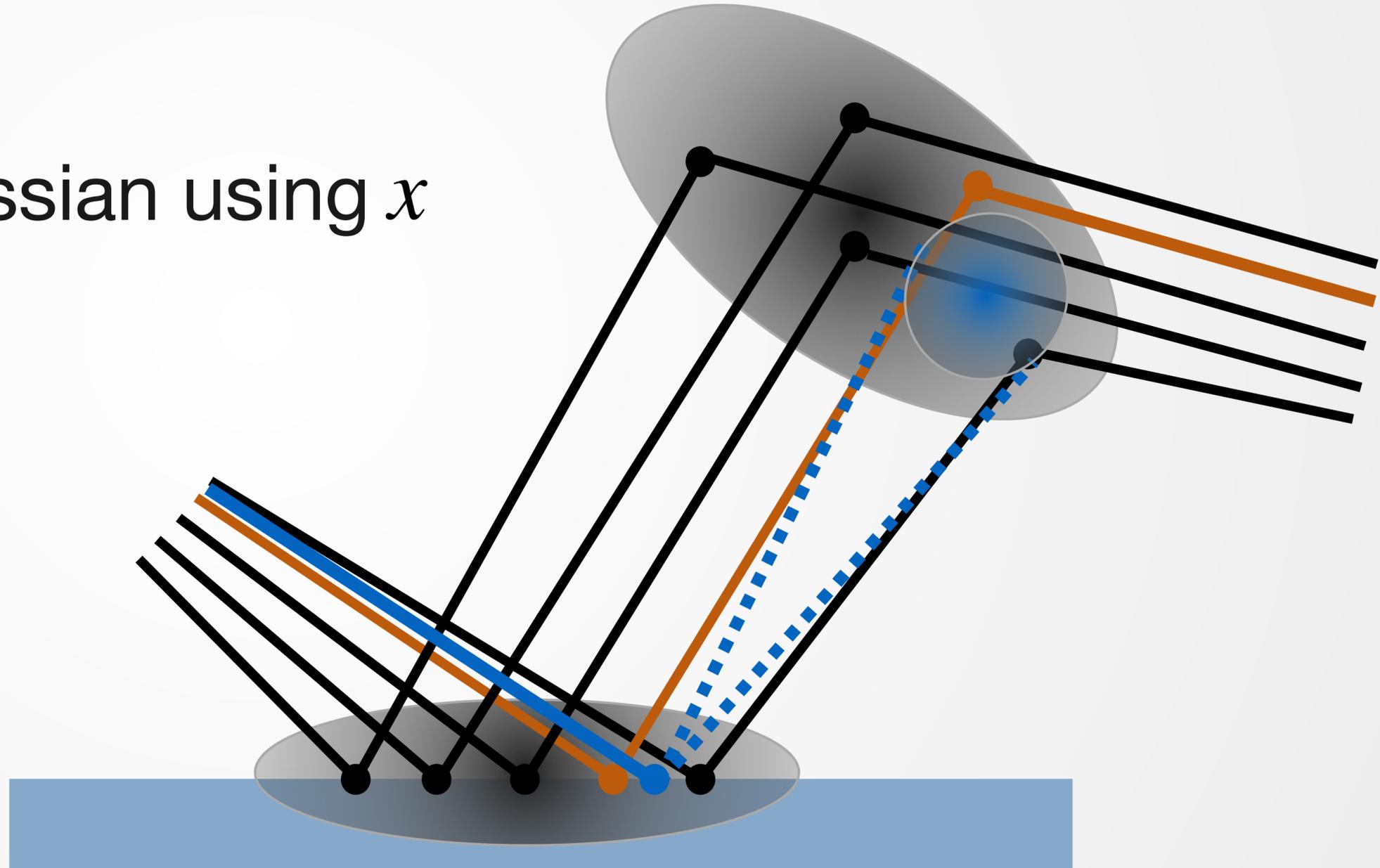
- Guide path
- Nearest neighbours
- New path



# Gaussians

- Compute 6D covariance matrix for path segments
- And conditional Gaussian using  $x$

- Guide path
- Nearest neighbours
- New path



# Sampling next vertex

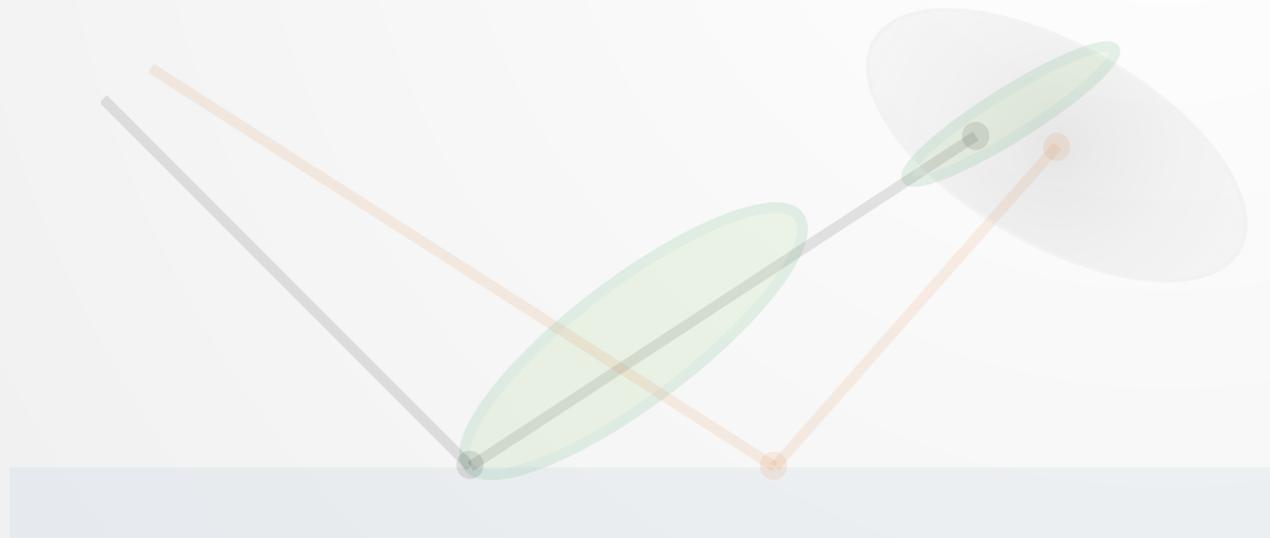
Next vertex in volume

Next vertex on surface

Sampling  
of  
Gaussian



Sampling  
of  
BSDF

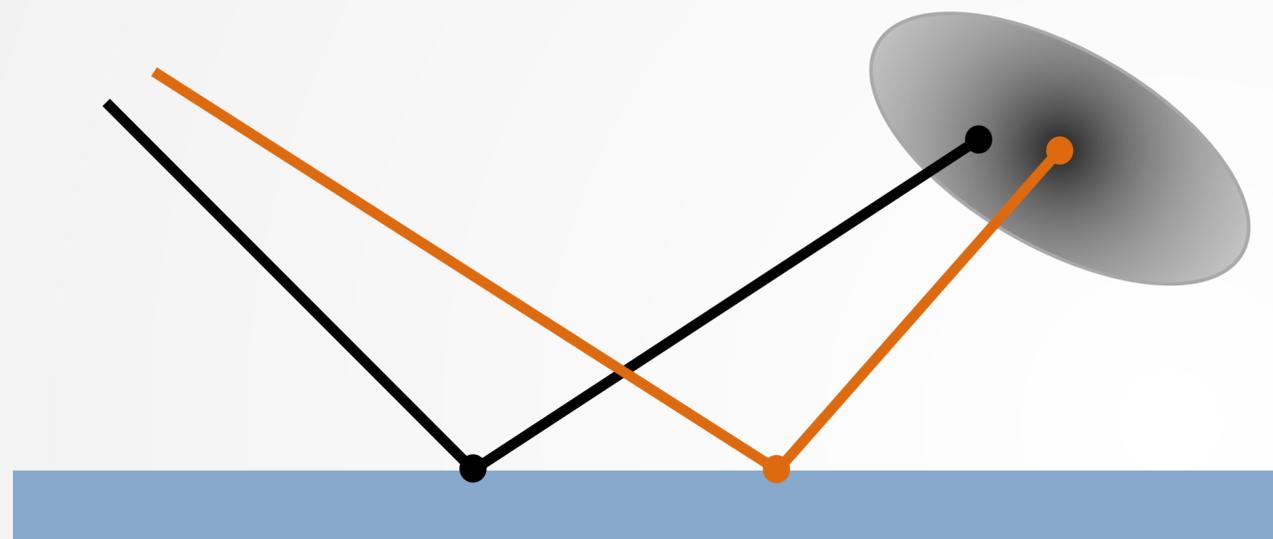


# Sampling next vertex

## Next vertex in volume

## Next vertex on surface

Sampling  
of  
Gaussian



Sampling  
of  
BSDF

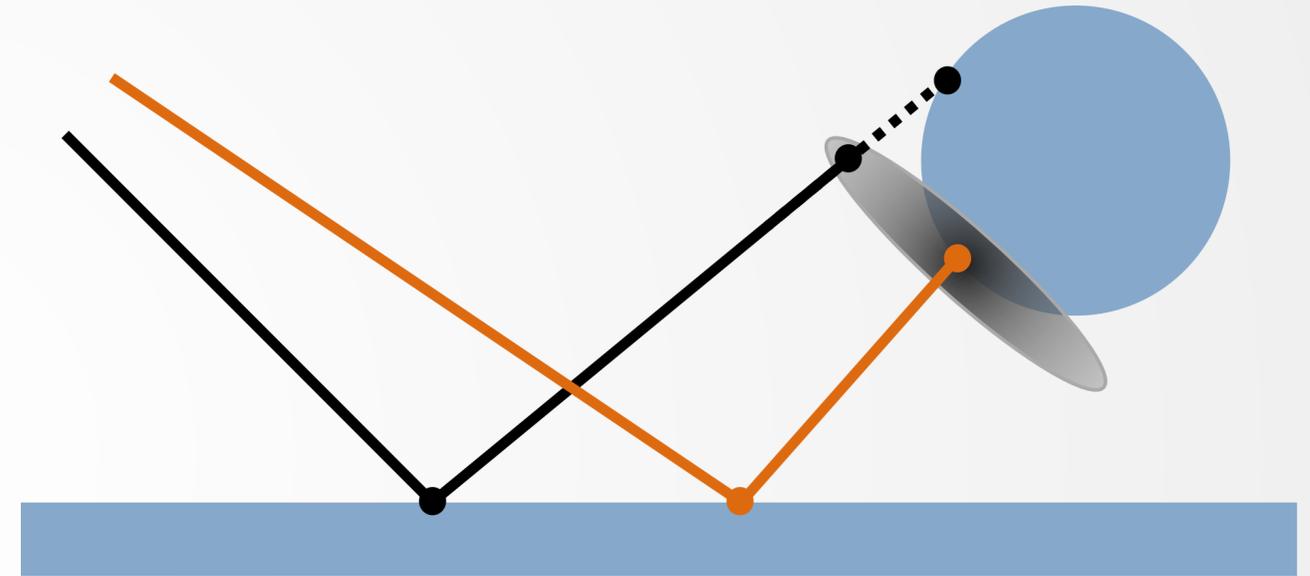
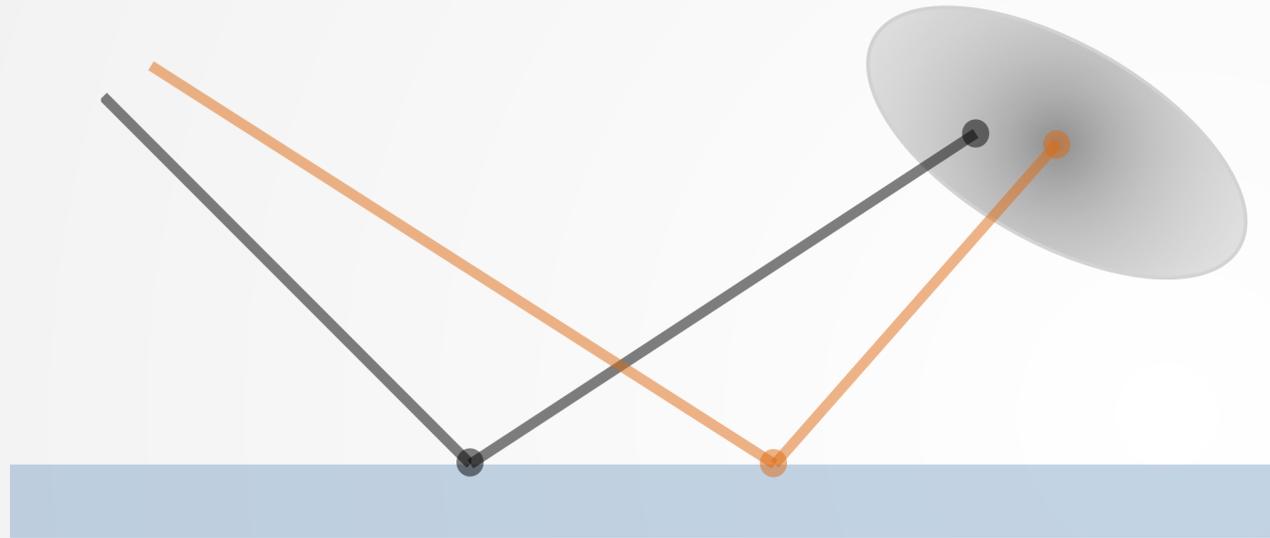


# Sampling next vertex

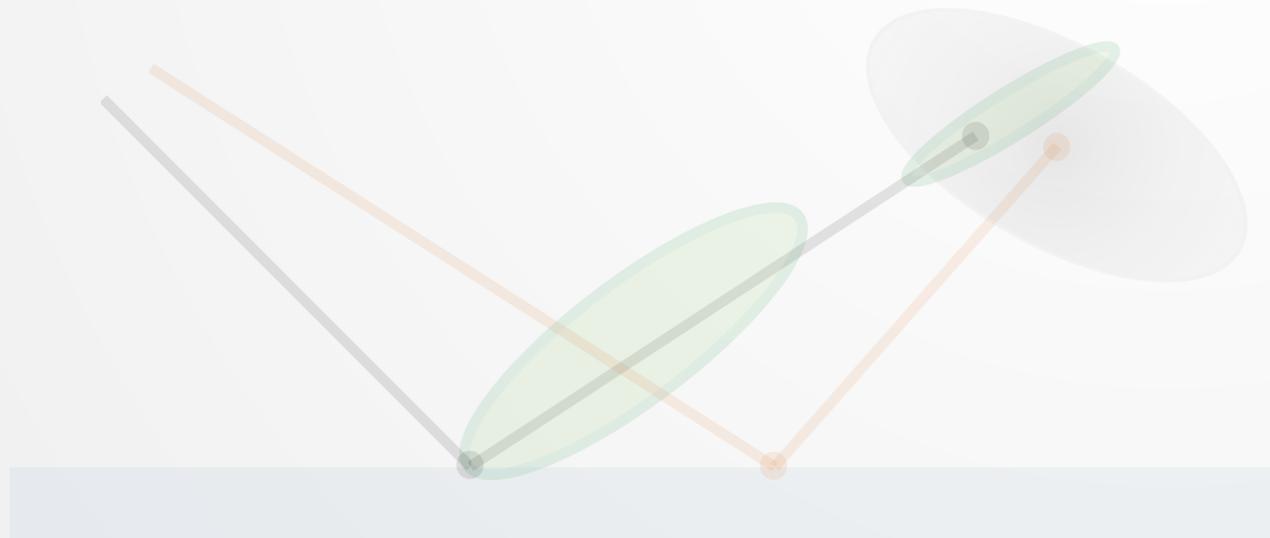
Next vertex in volume

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BSDF

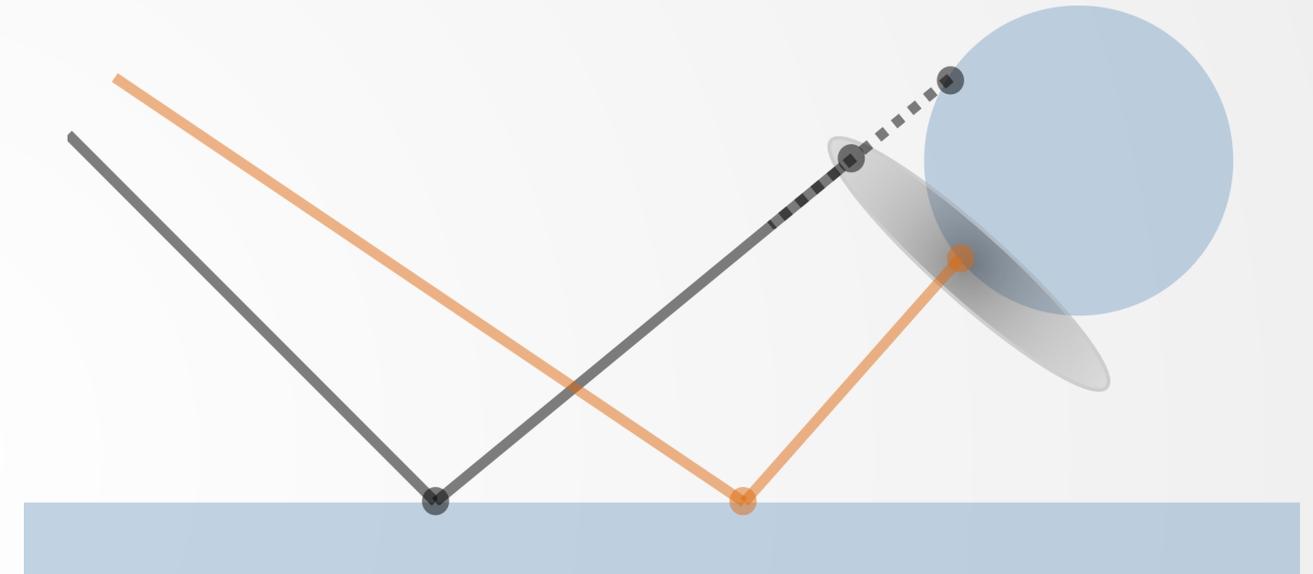
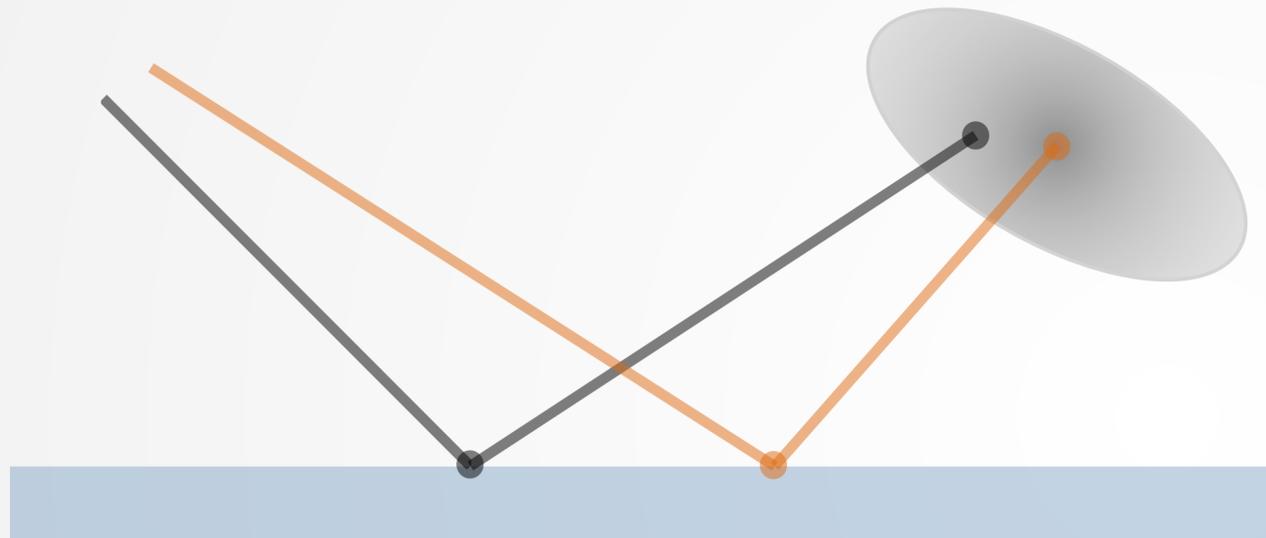


# Sampling next vertex

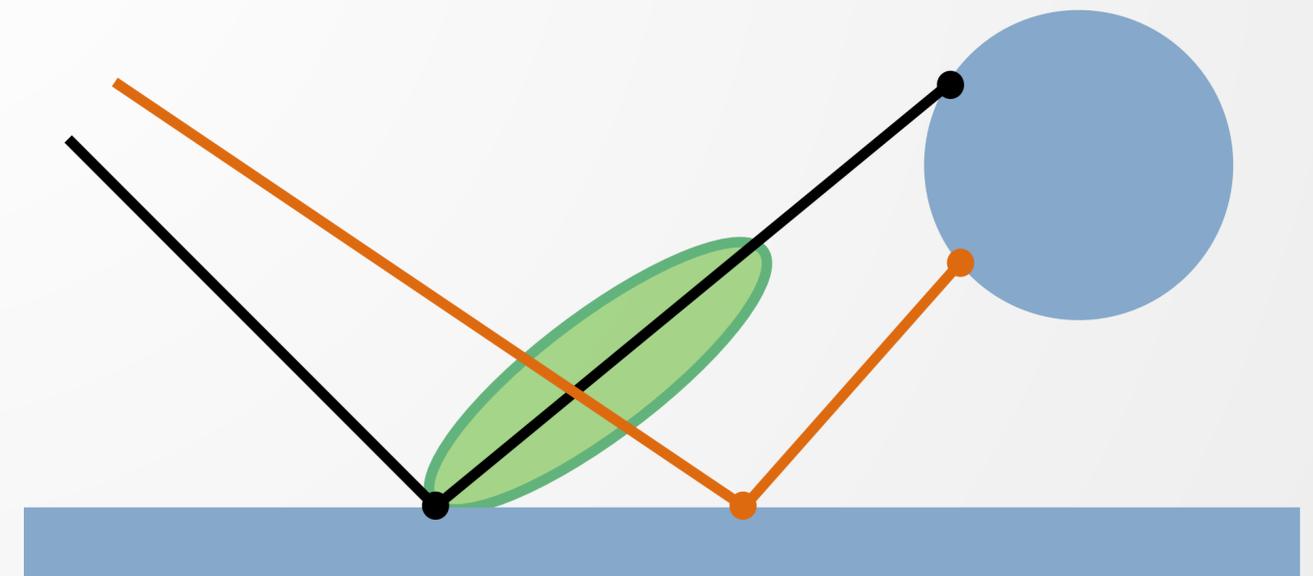
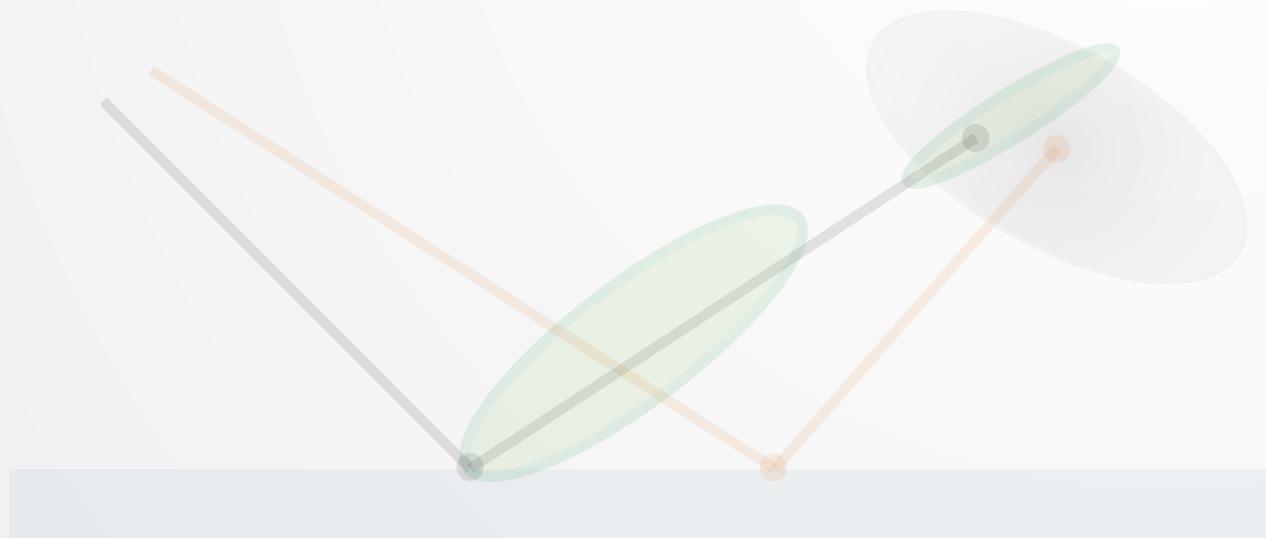
## Next vertex in volume

## Next vertex on surface

Sampling  
of  
Gaussian



Sampling  
of  
BSDF

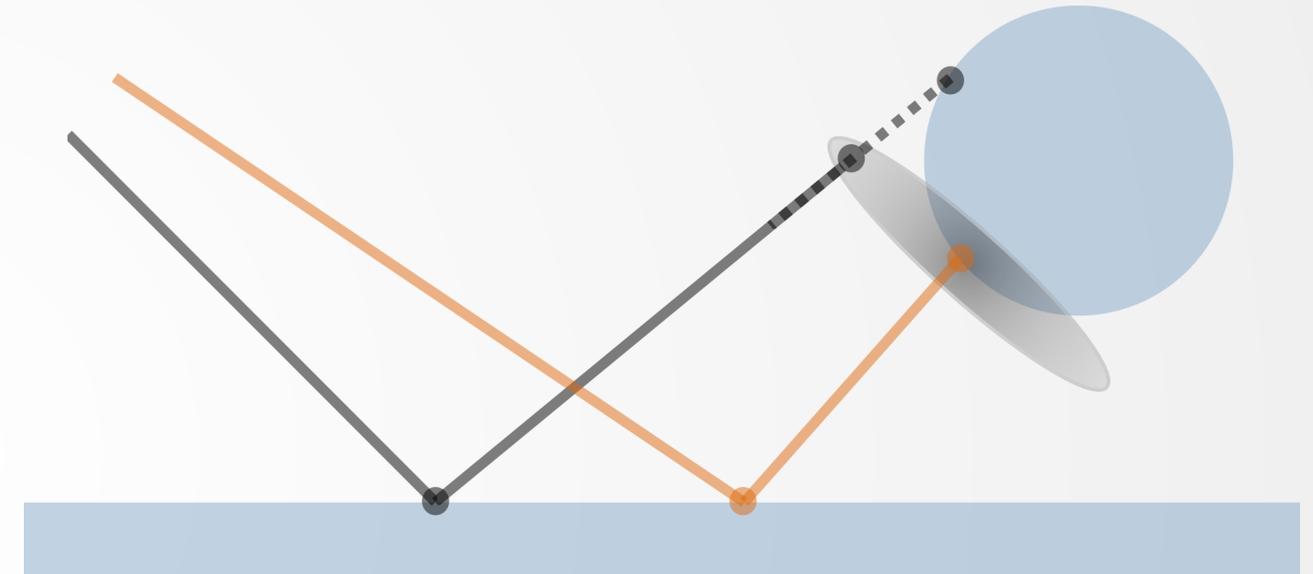
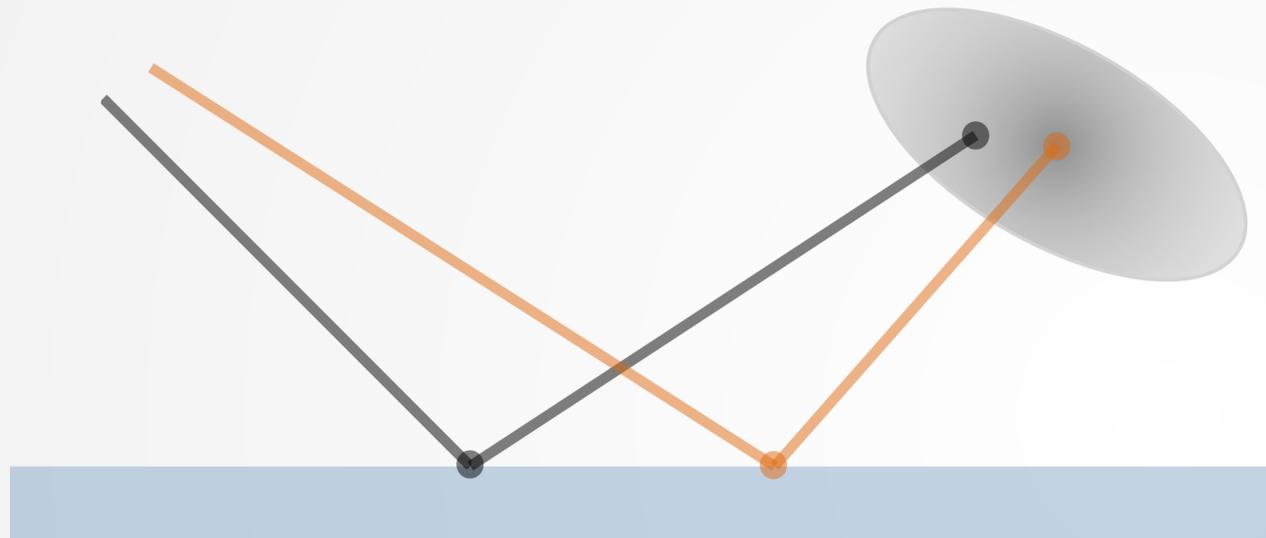


# Sampling next vertex

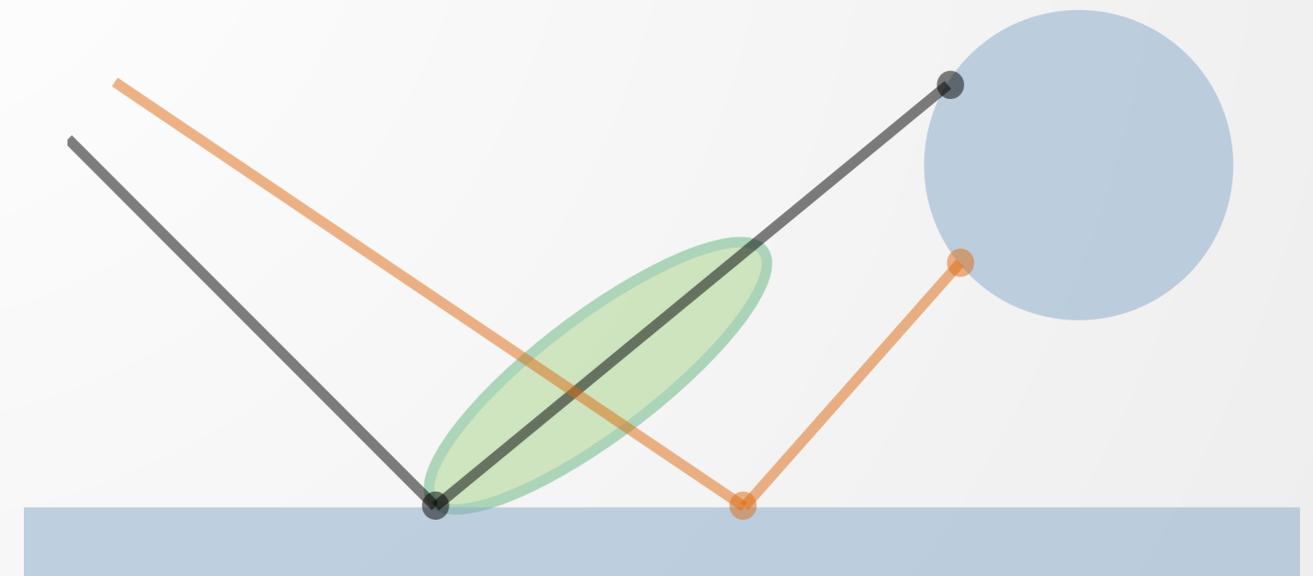
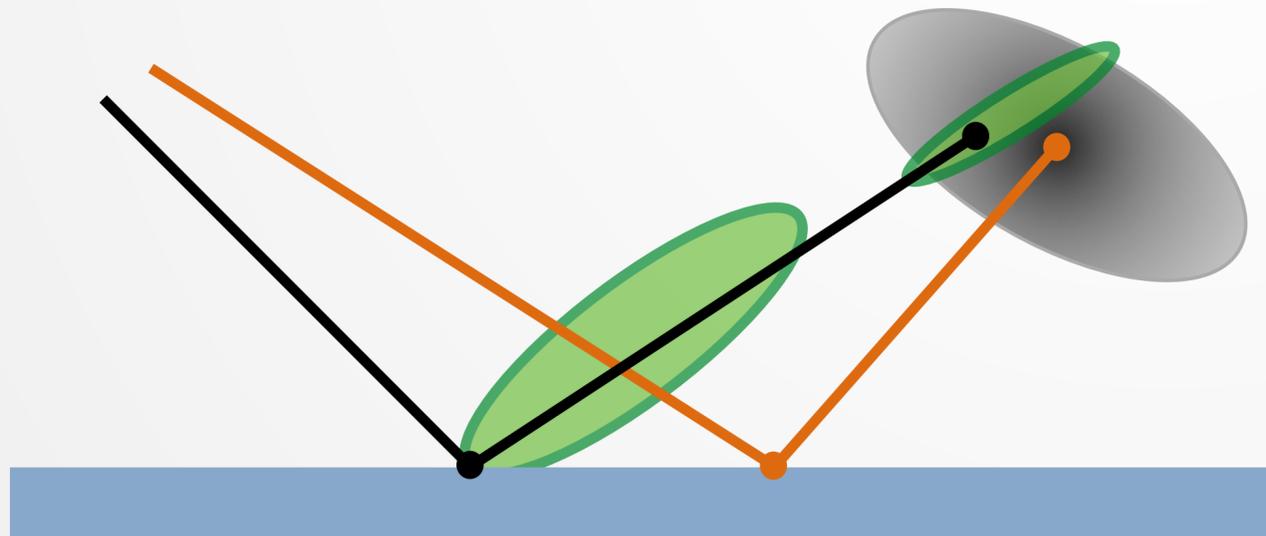
## Next vertex in volume

## Next vertex on surface

Sampling  
of  
Gaussian



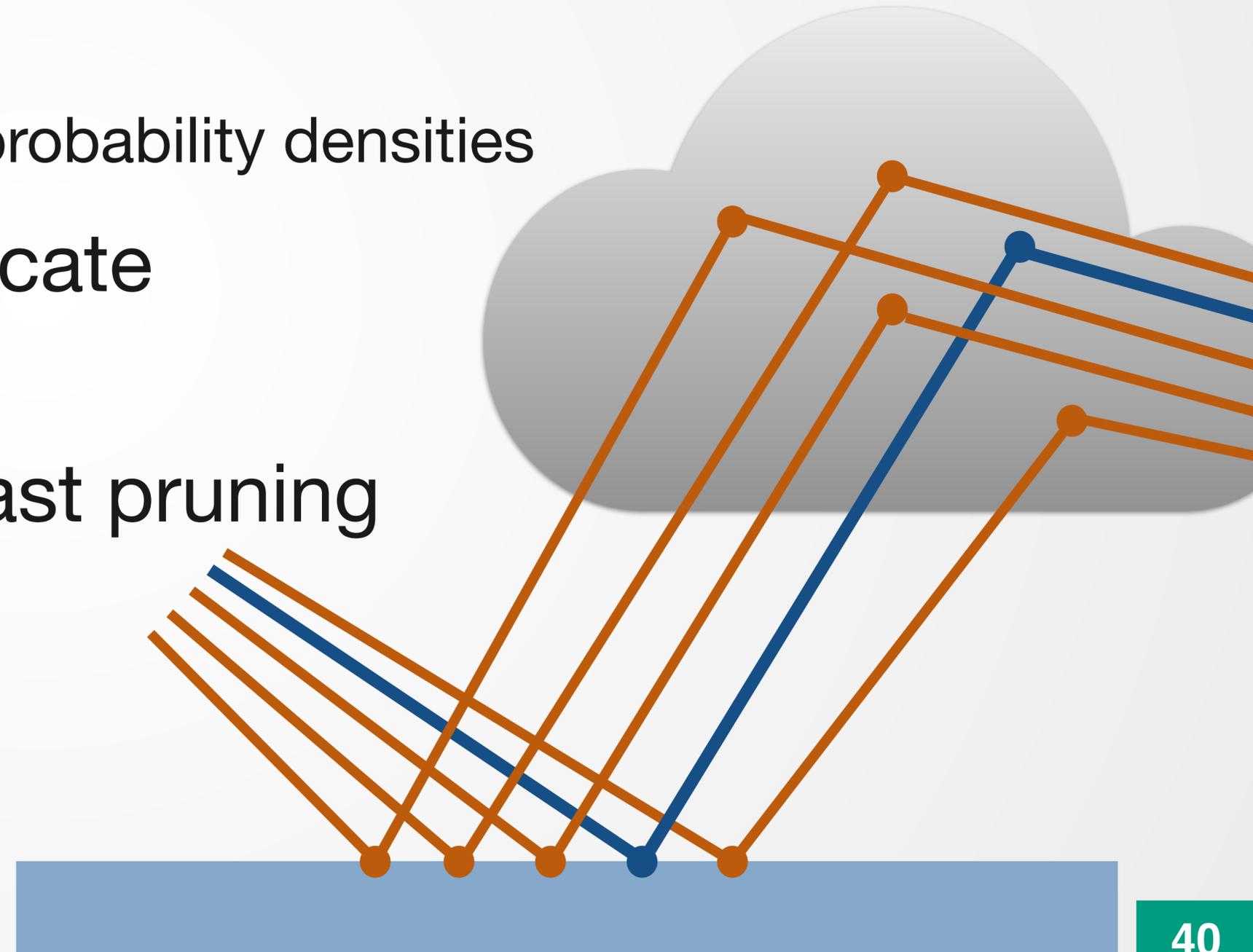
Sampling  
of  
BSDF



# Guided PDF

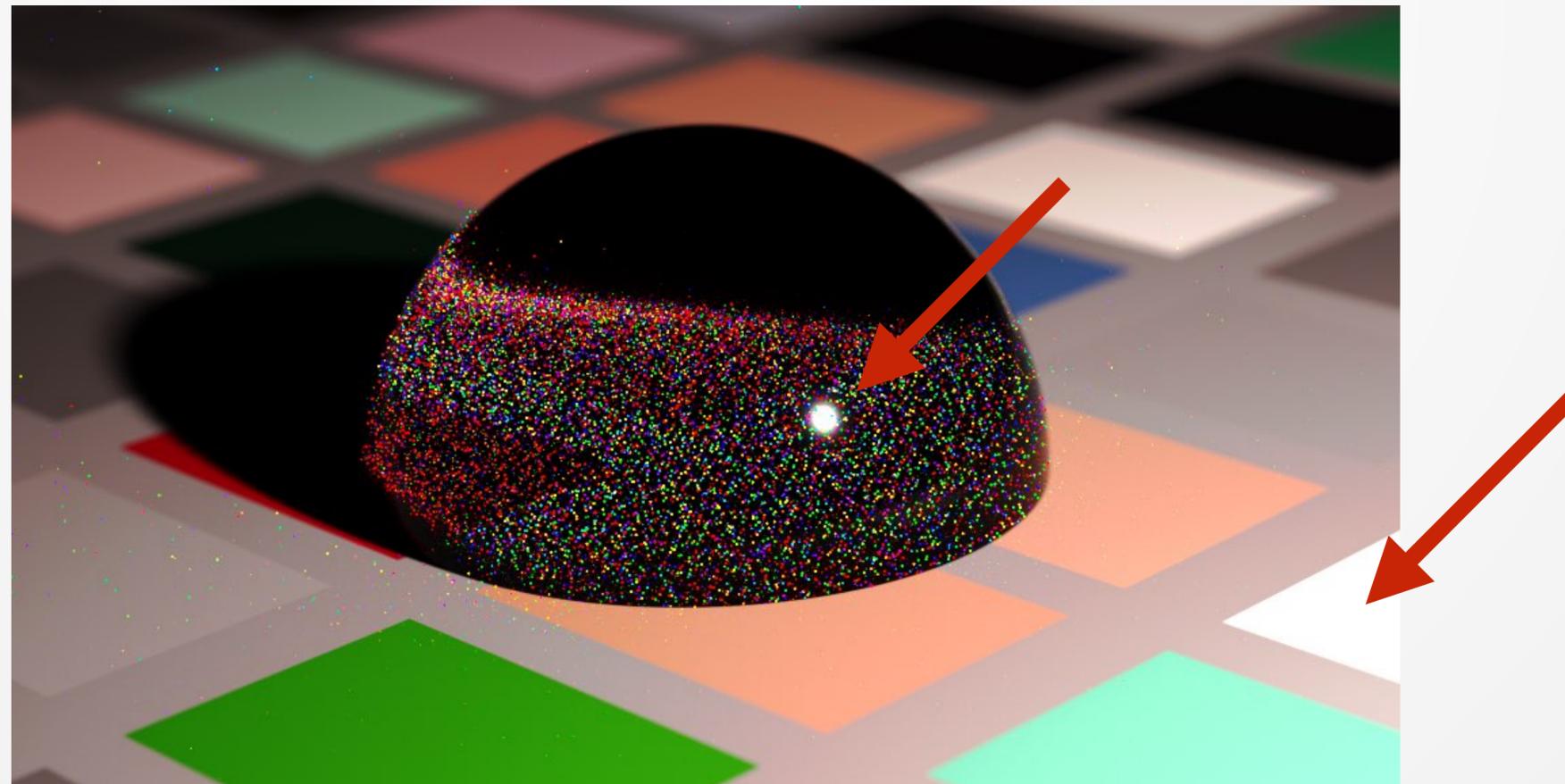
- Many guide paths could sample the same path  $X$ 
  - We have to sum up all individual probability densities
- For fast evaluation, we truncate Gaussians ( $\approx 3\sigma$ )
- Acceleration structure for fast pruning

— Guide paths  $X_l$   
— Path  $X$



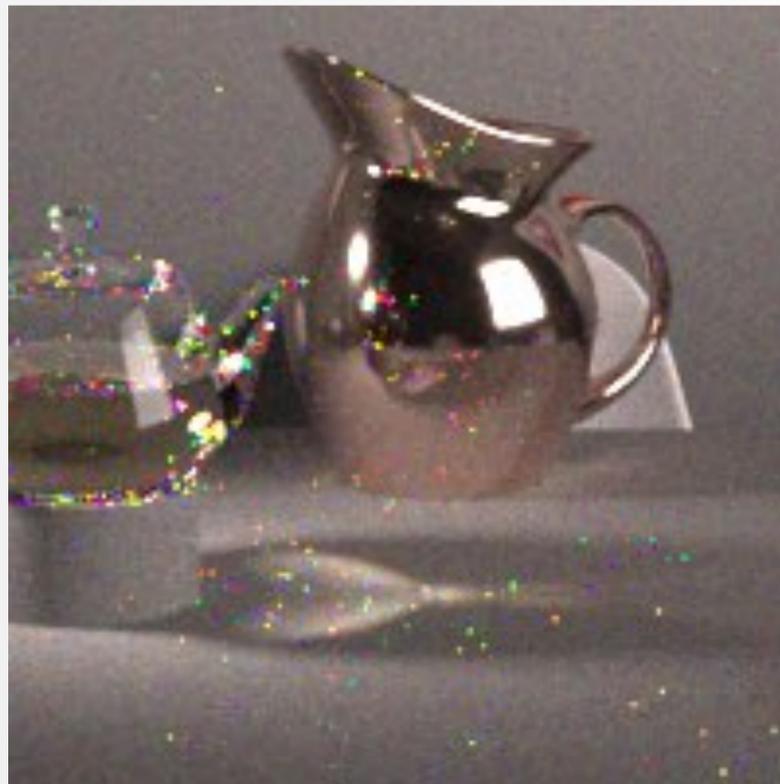
# Selecting Guide Paths

- Outliers  $\neq$  samples with high contribution
- Outliers classification: Density based outlier rejection (DBOR, Zirr et al. [2018])



# Remaining outliers

- Outliers contribute fully to the image
- We remove outliers with DBOR to get clean images

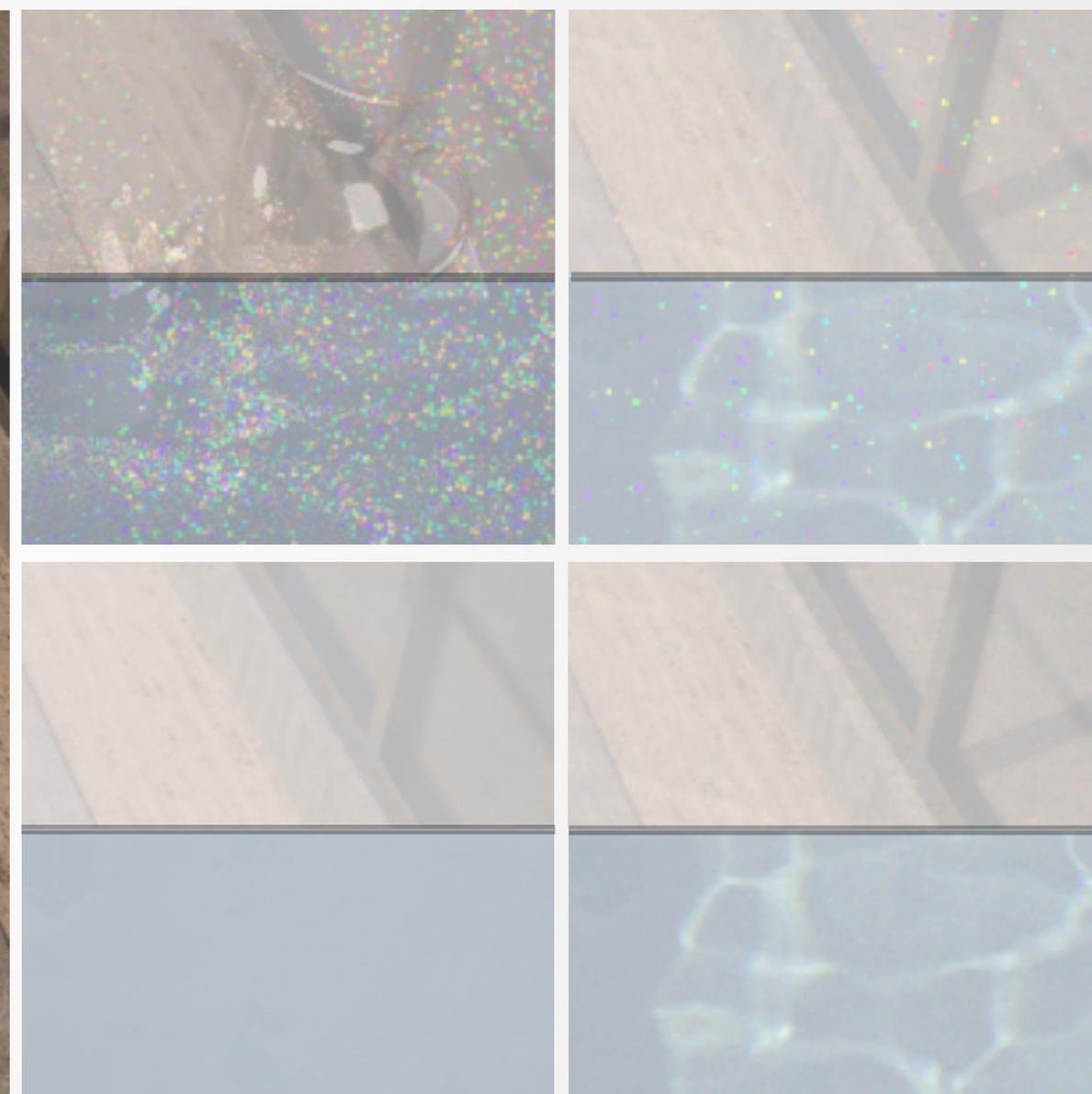
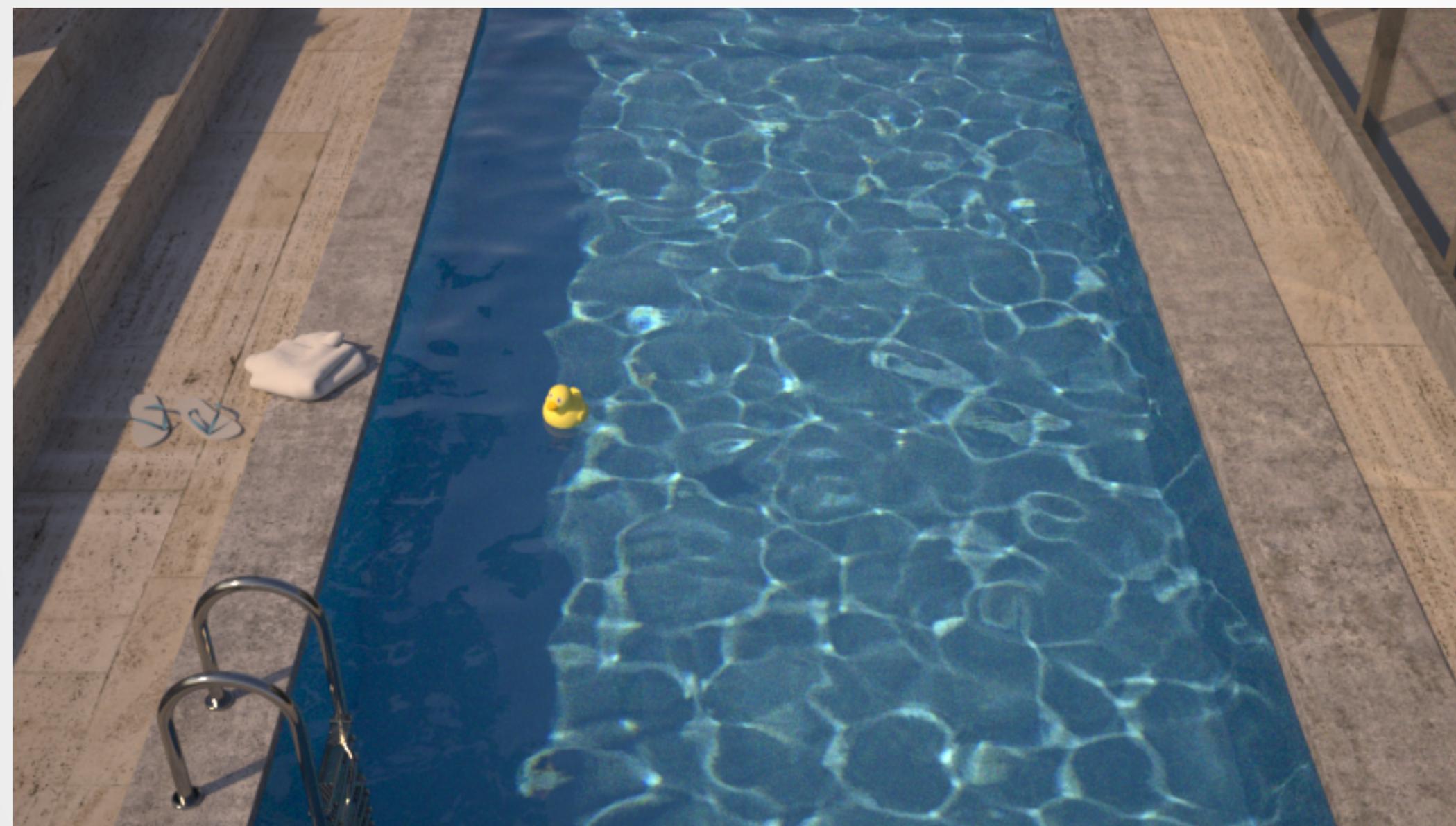


Outliers  
removed



# Pool

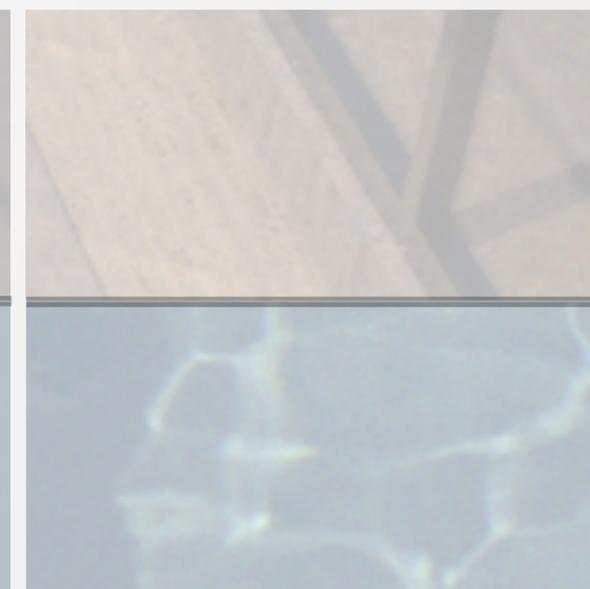
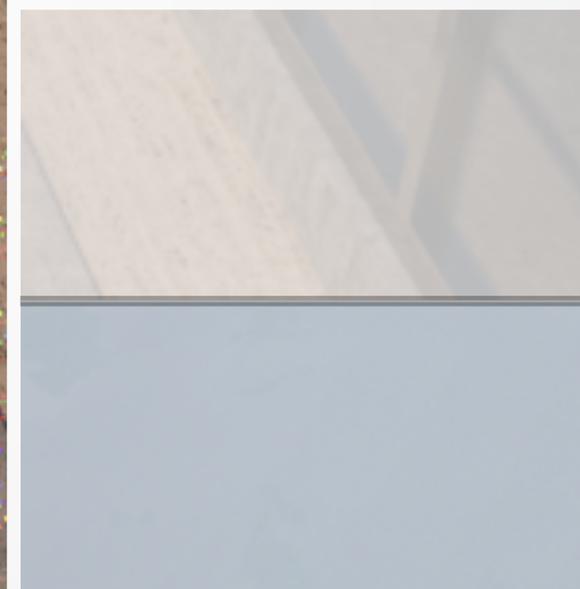
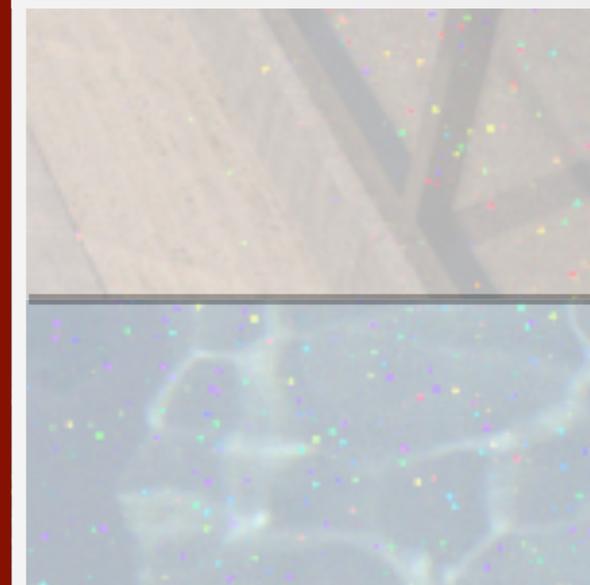
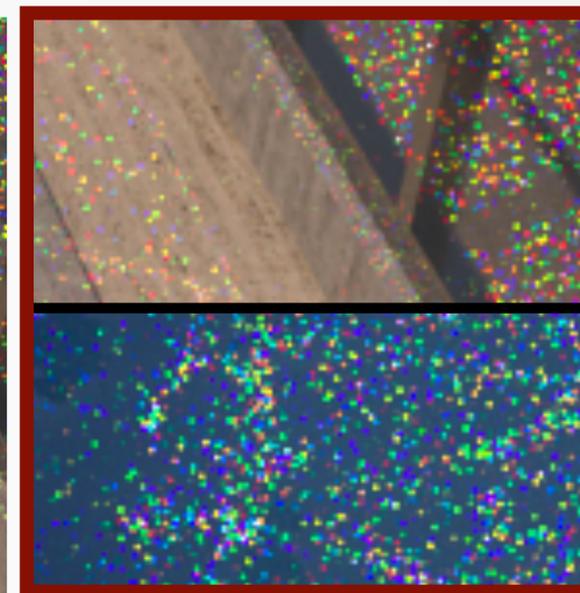
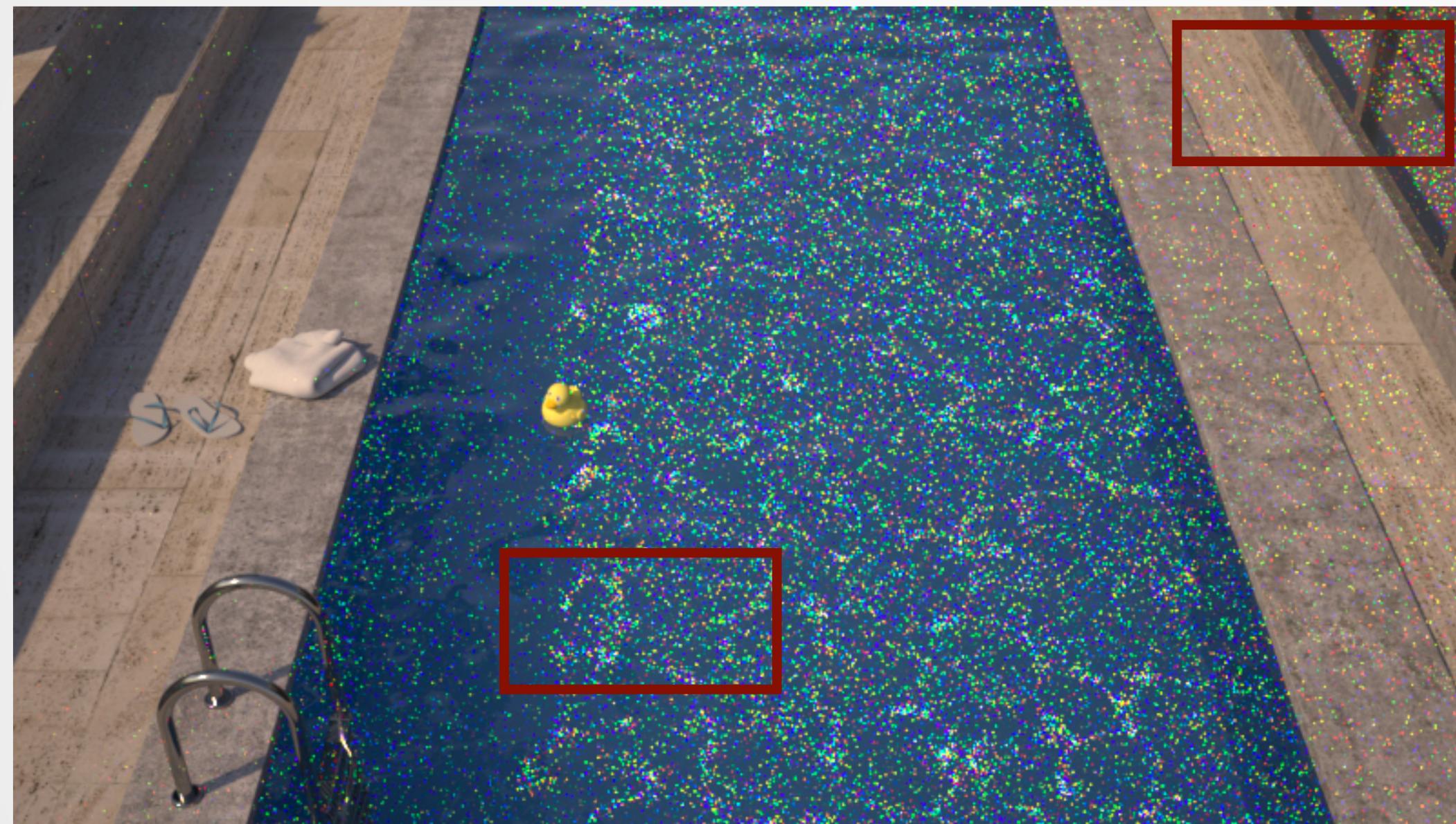
## Reference



# Pool - 30min

## Path tracing

PT

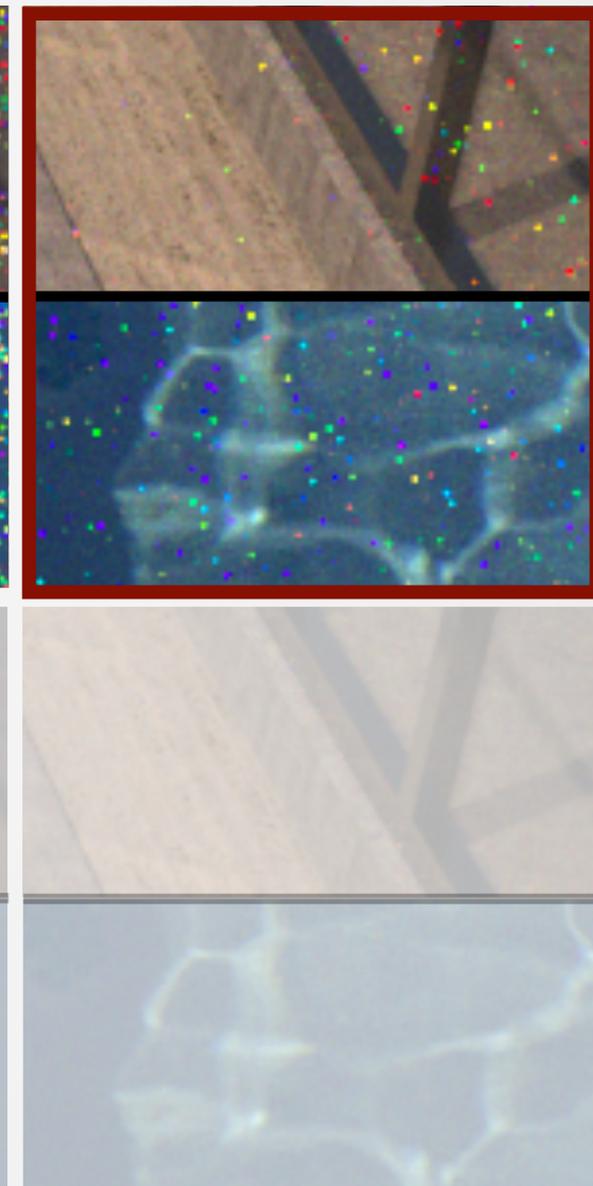
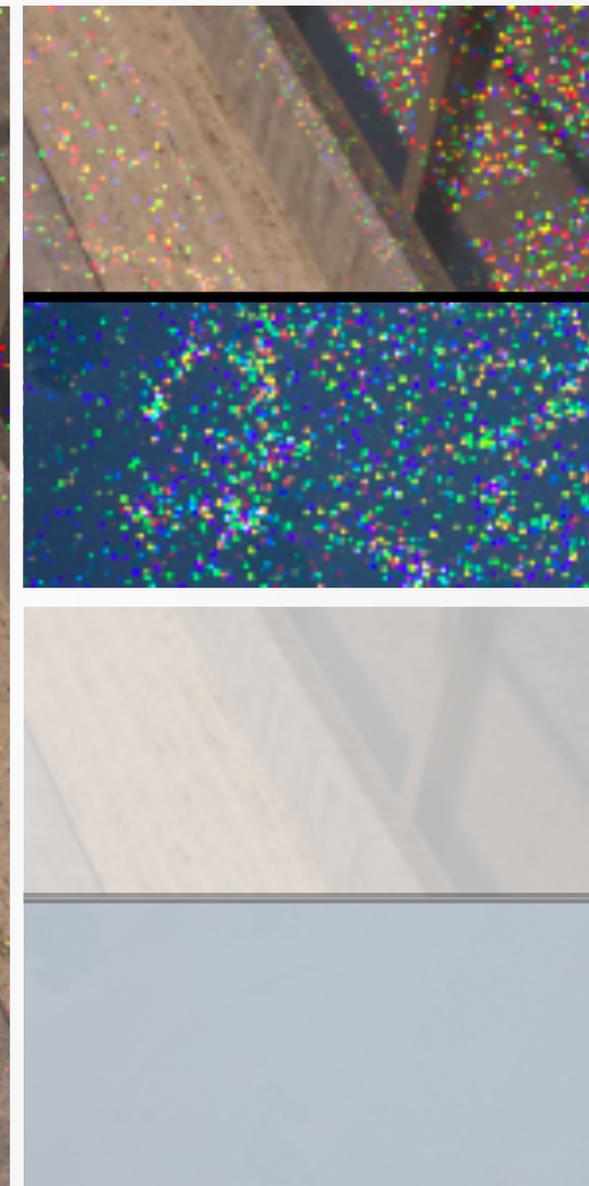
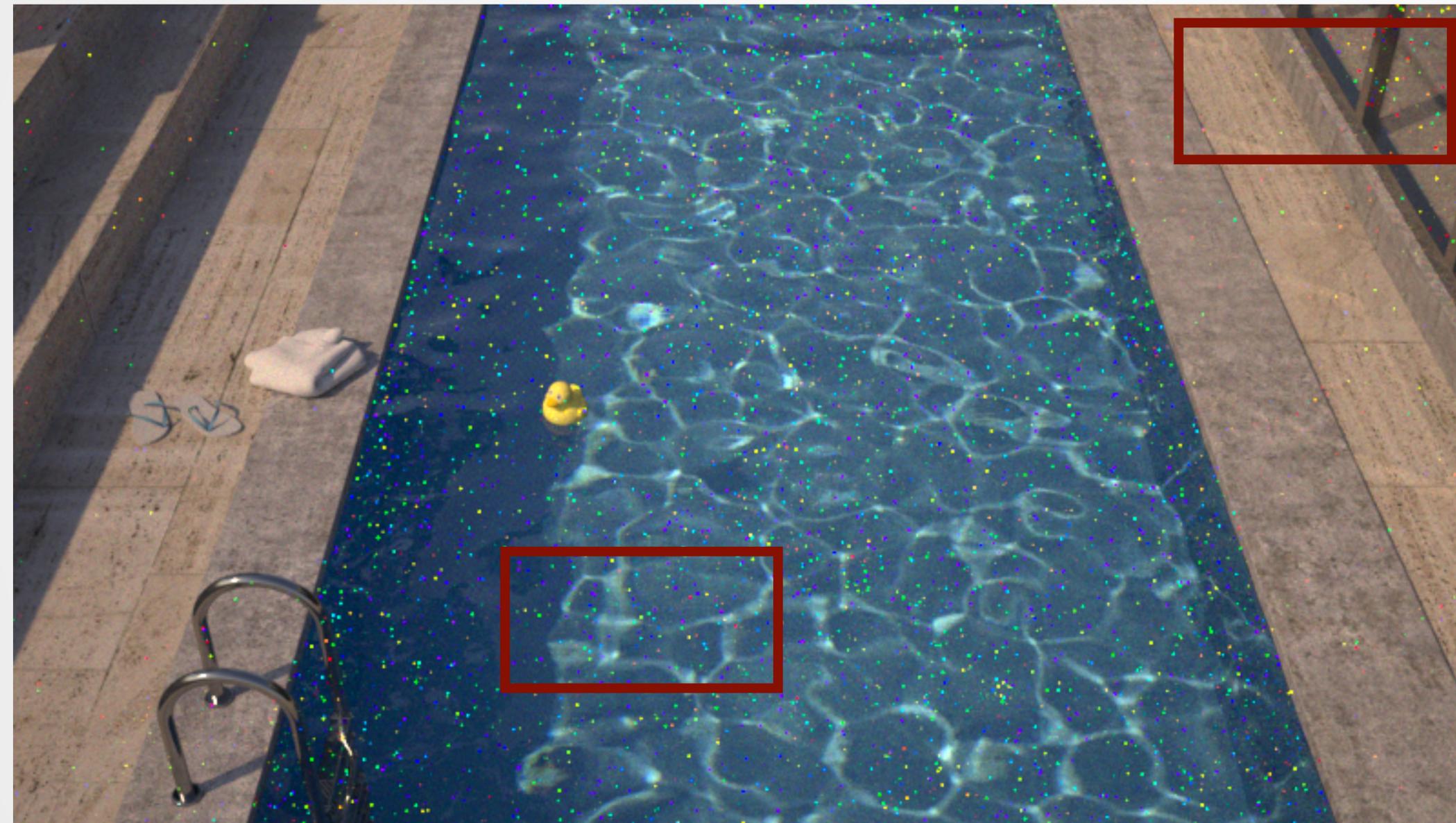


# Pool - 30min

## Guided path tracing

PT

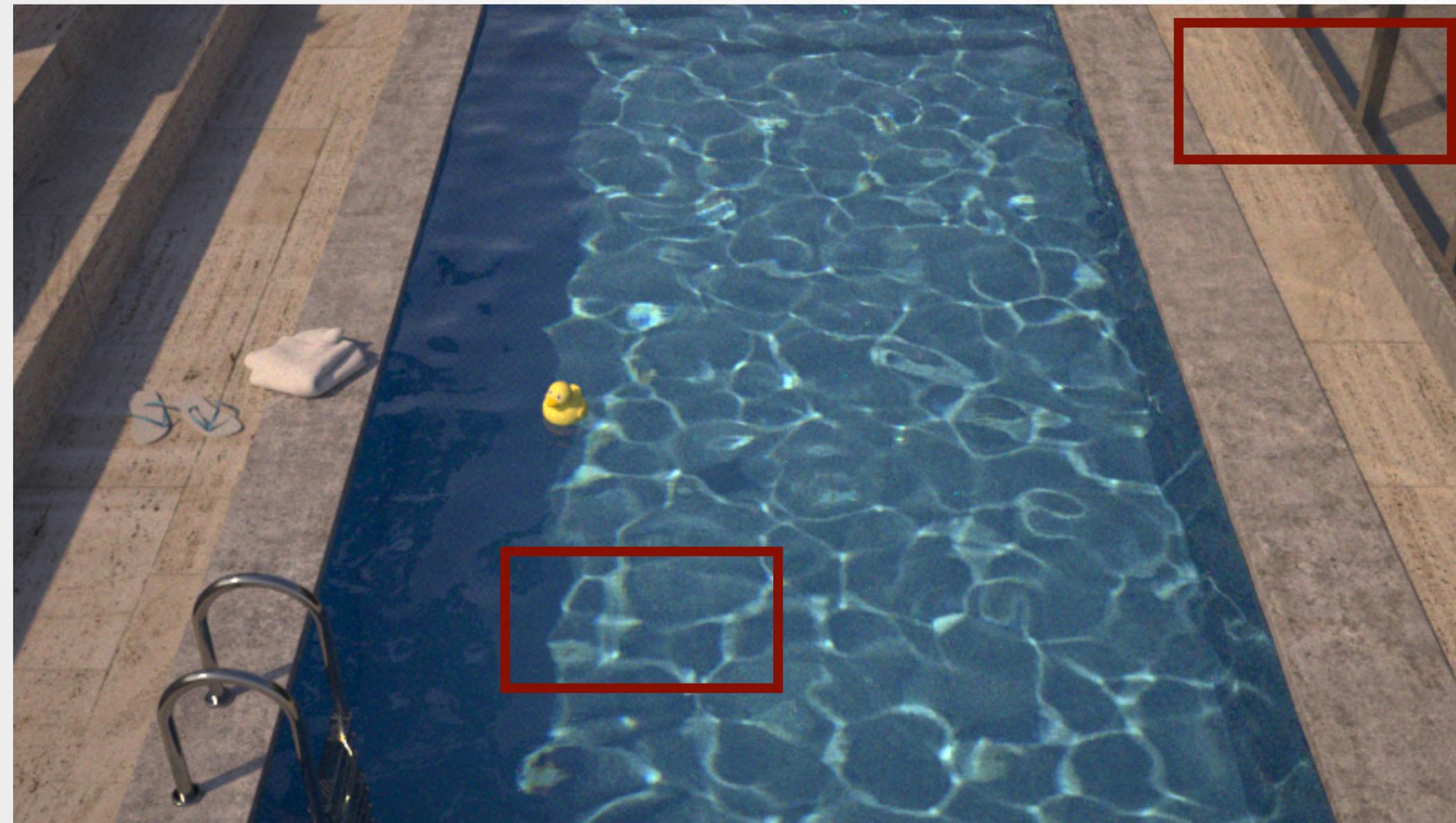
Guided PT



**104k guide paths ( $\approx 310\text{MB}$ )**

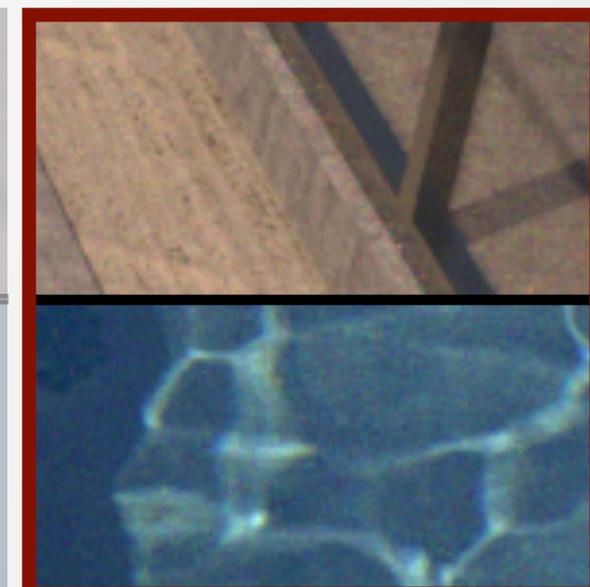
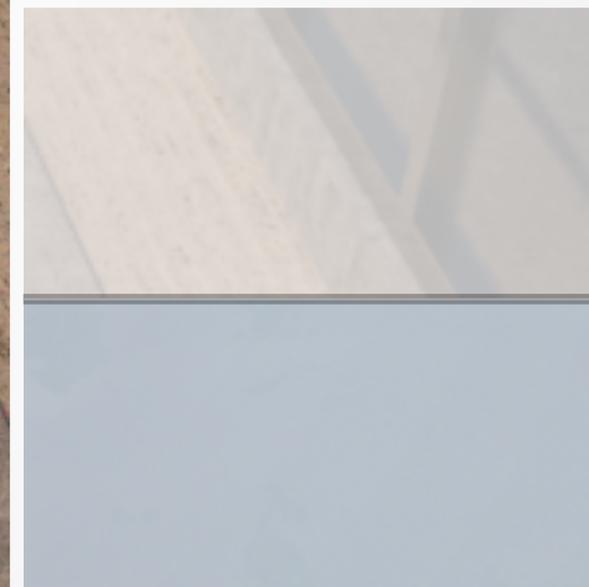
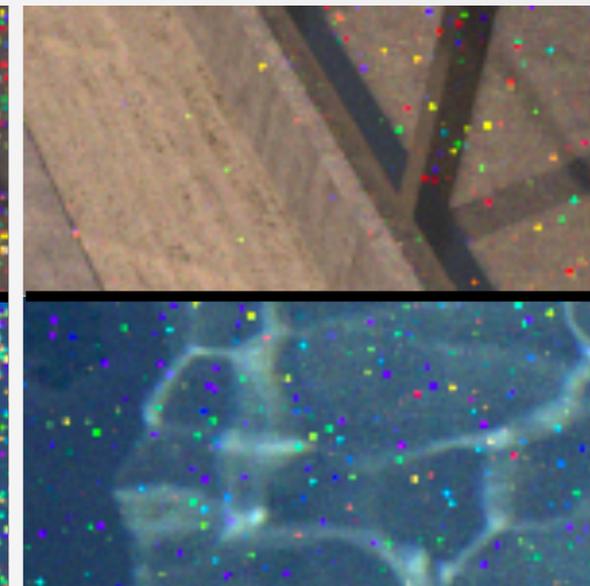
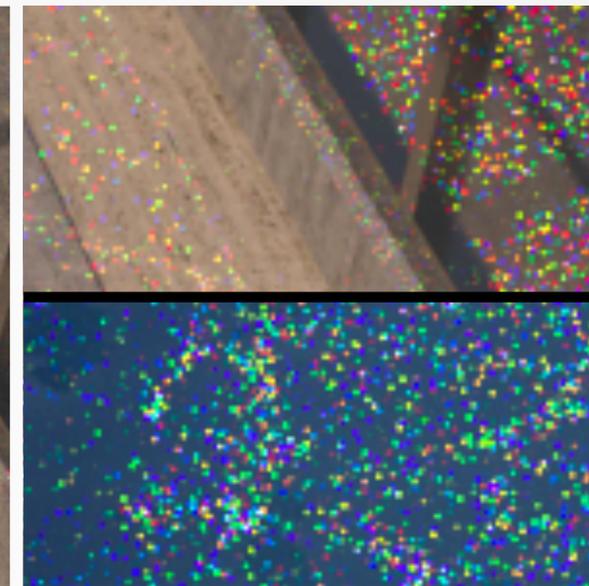
# Pool - 30min

## Guided path tracing + DBOR



PT

Guided PT

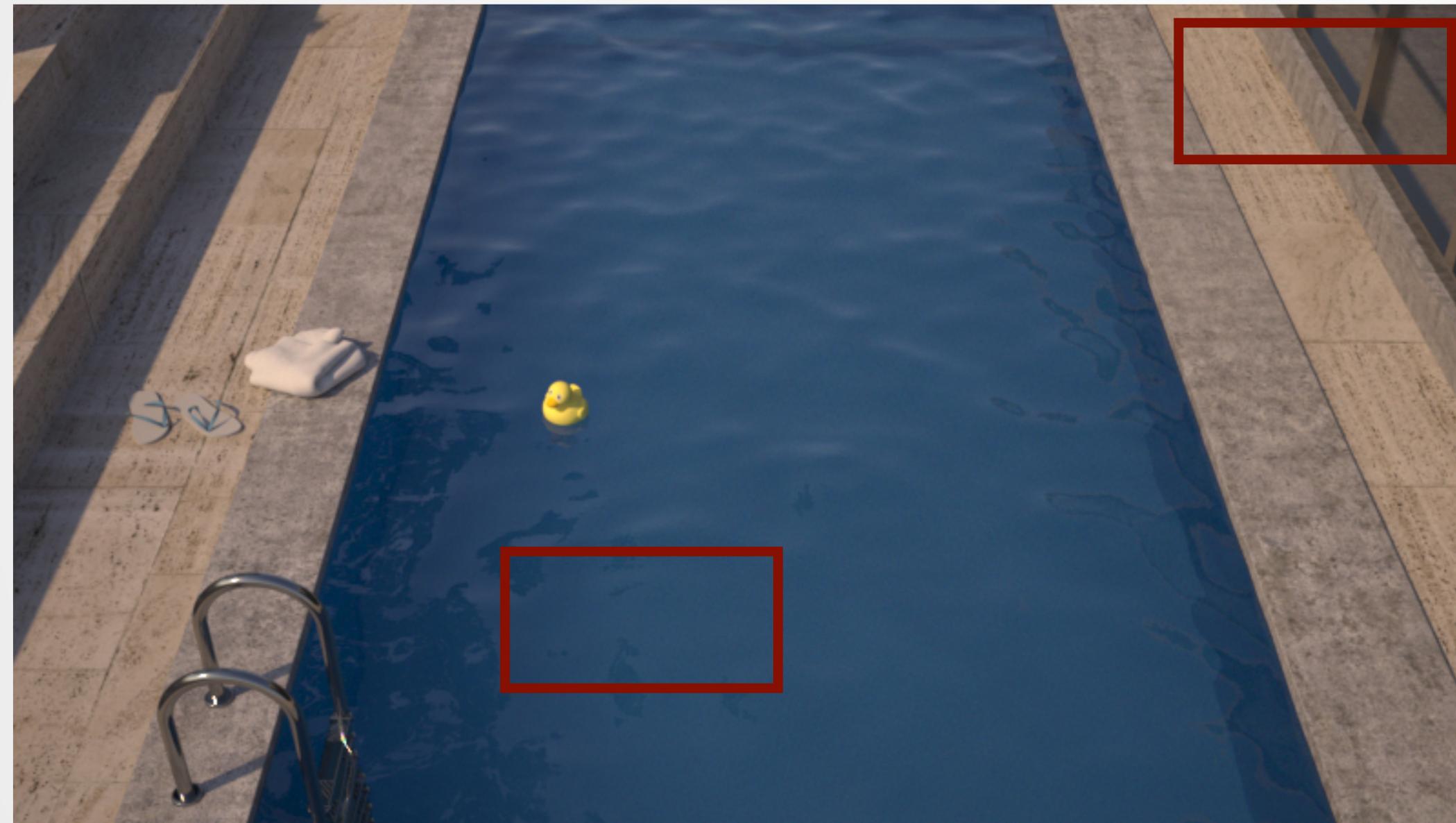


104k guide paths ( $\approx 310\text{MB}$ )

Guided PT+DBOR

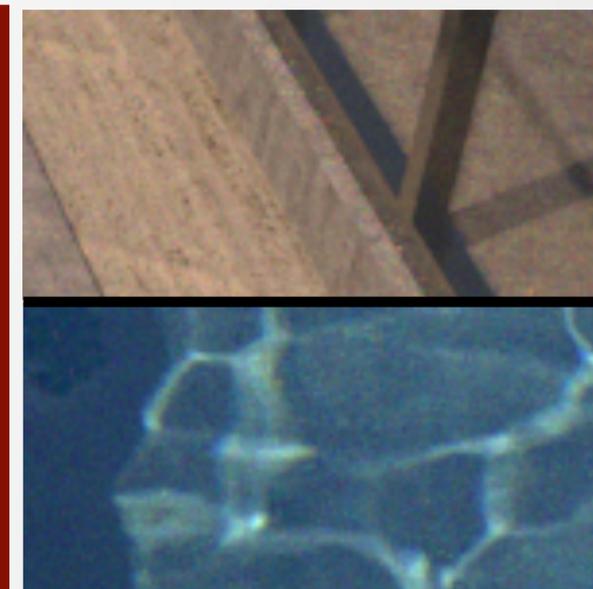
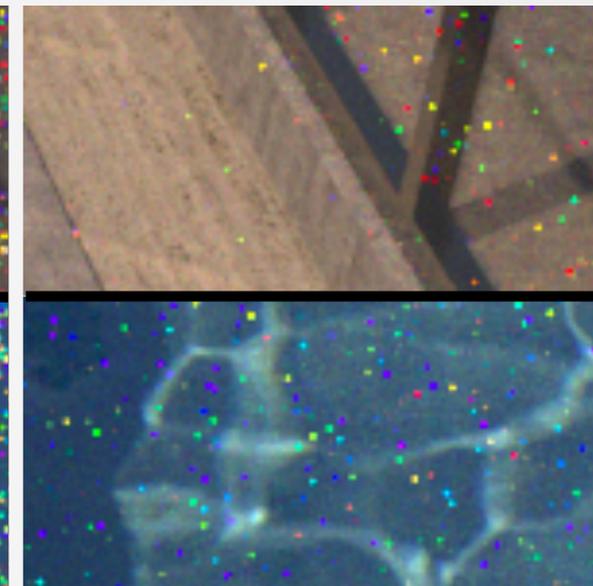
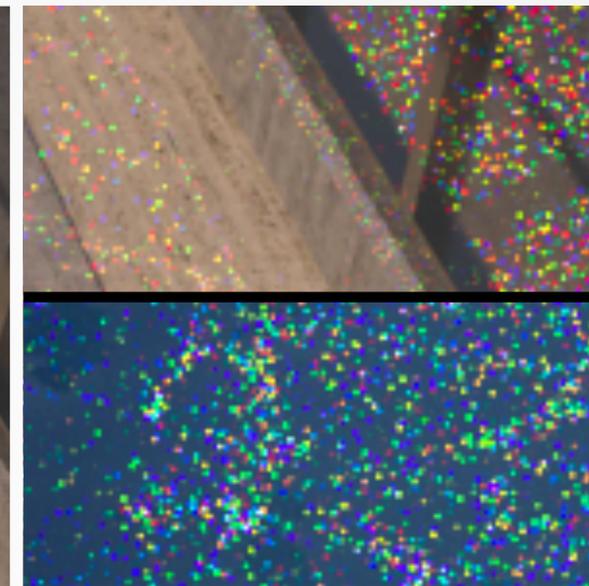
# Pool - 30min

## Path tracing + DBOR



PT

guided PT

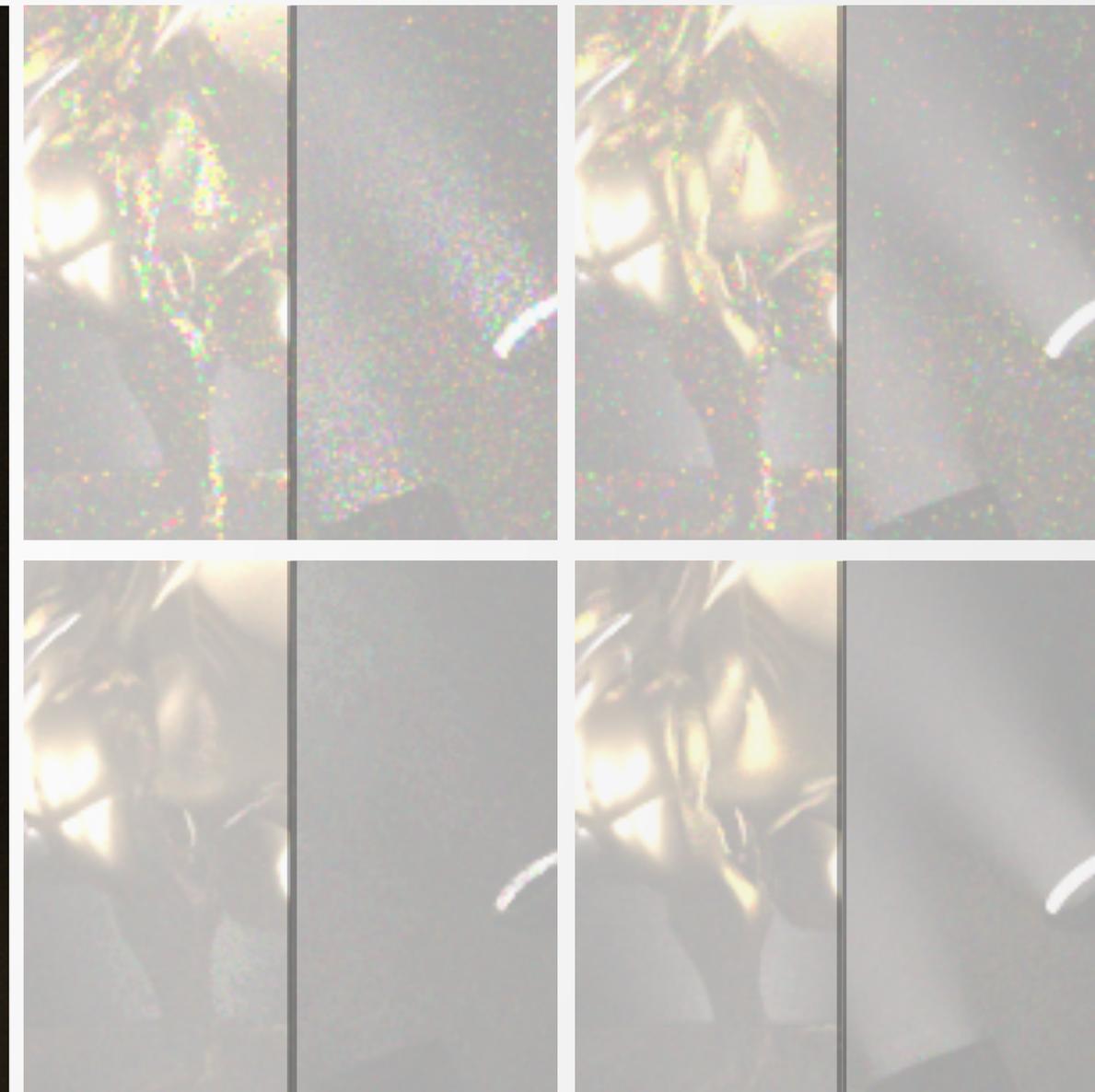


PT + DBOR

guided PT+DBOR

# Dragon

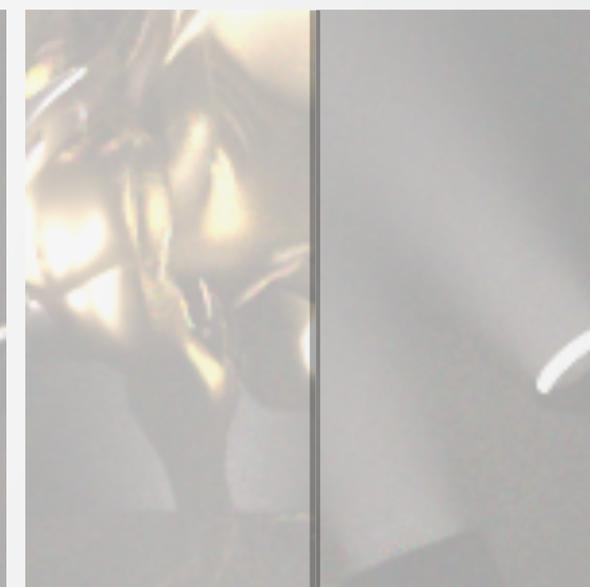
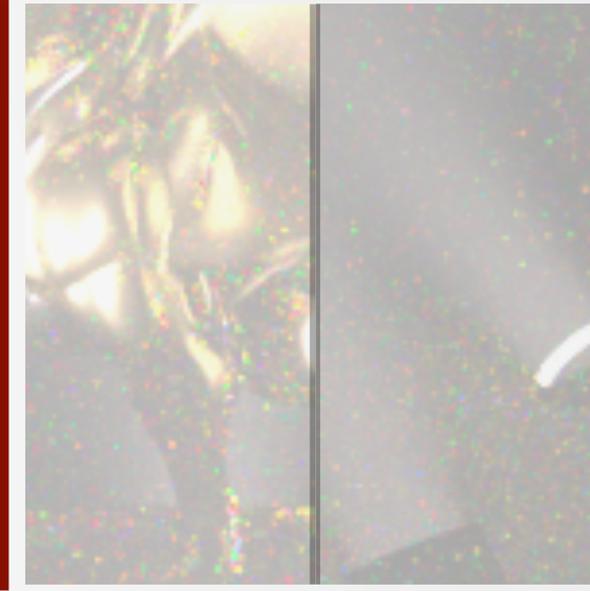
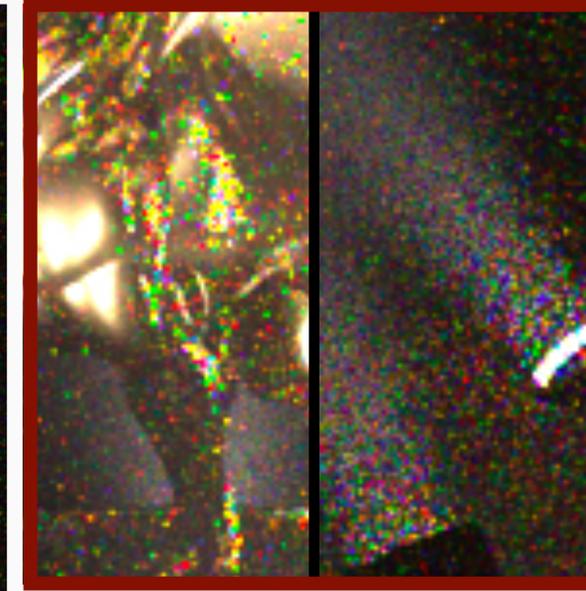
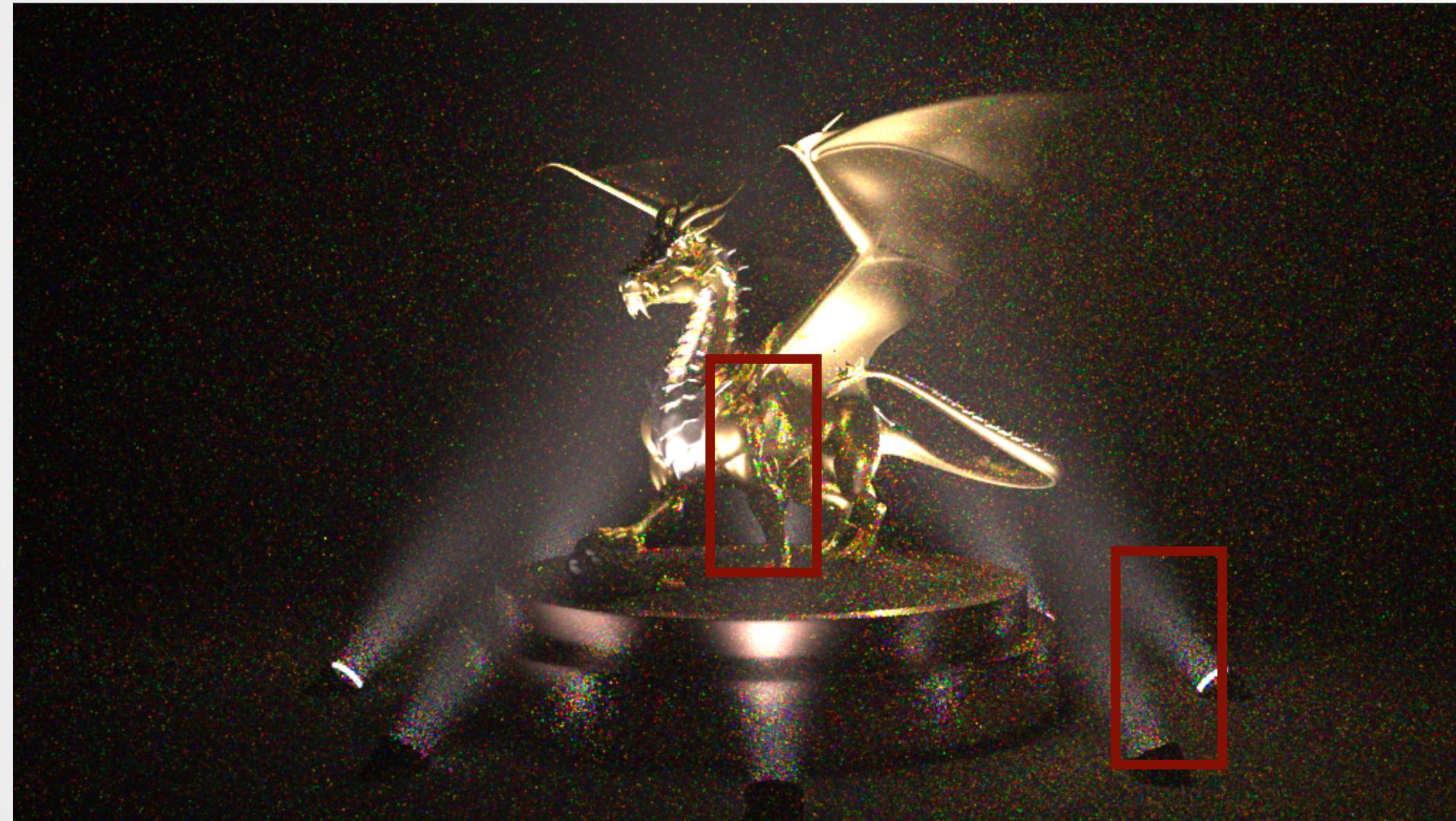
## Reference



# Dragon - 10h

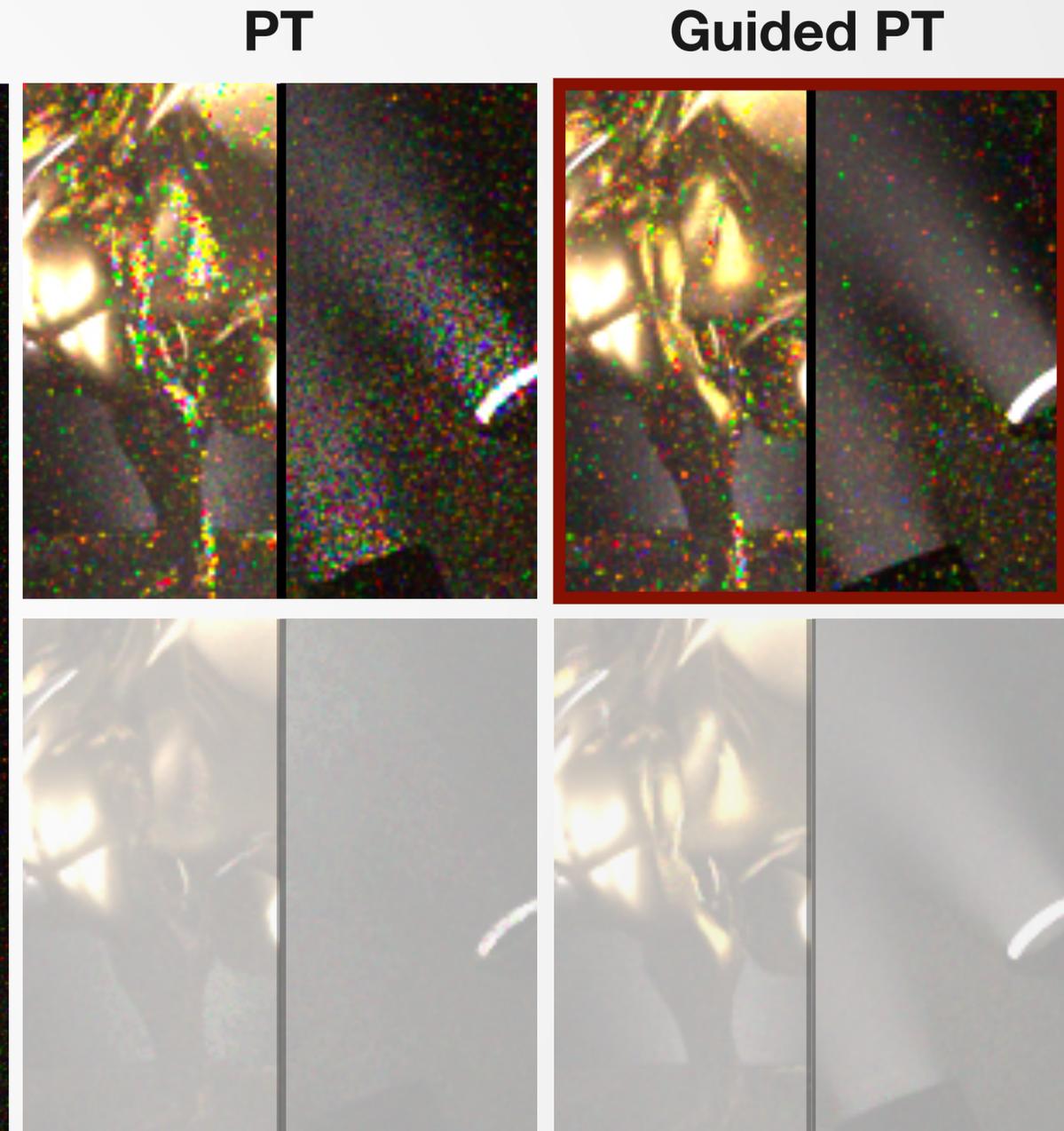
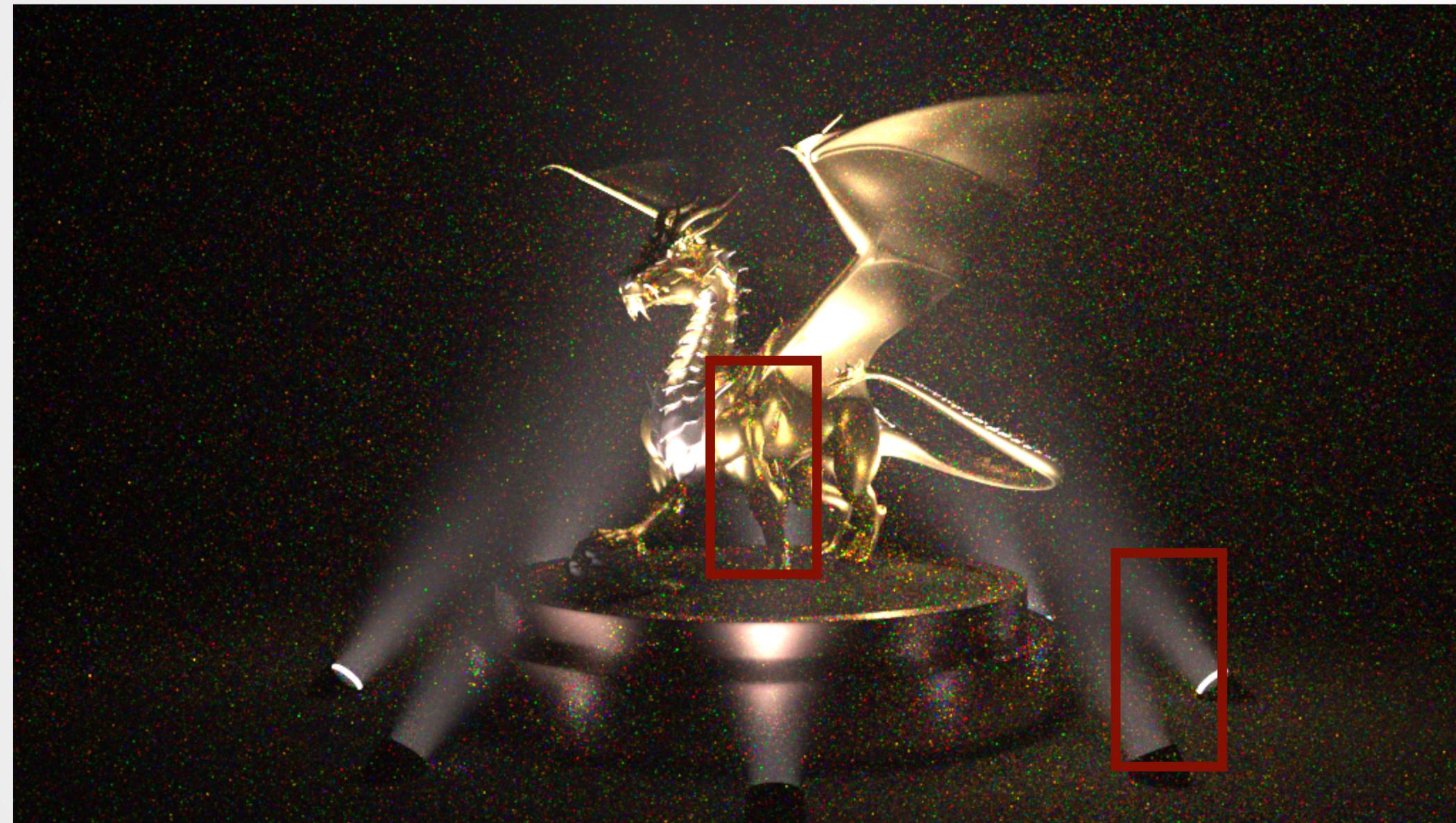
## Path tracing

PT



# Dragon - 10h

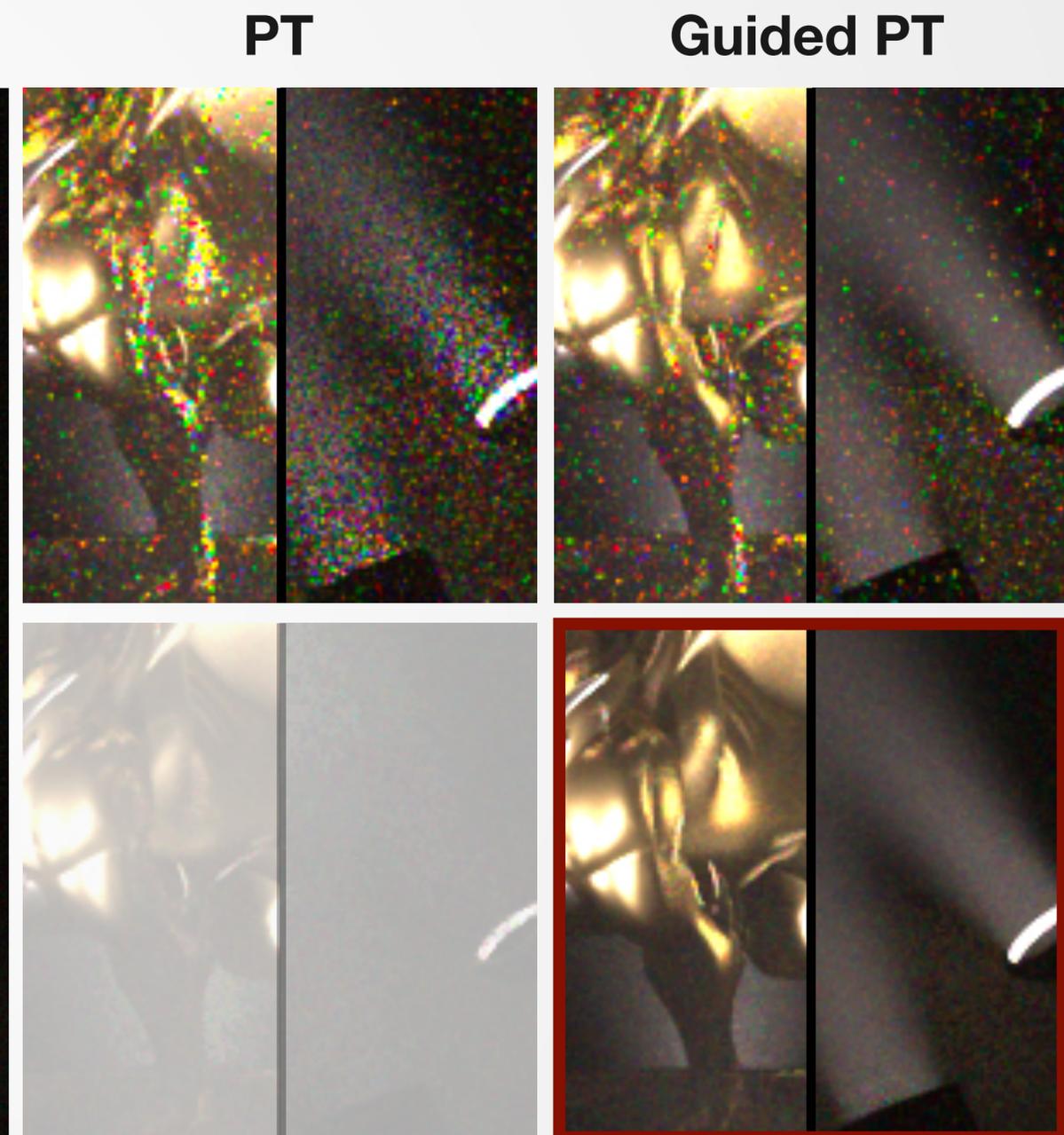
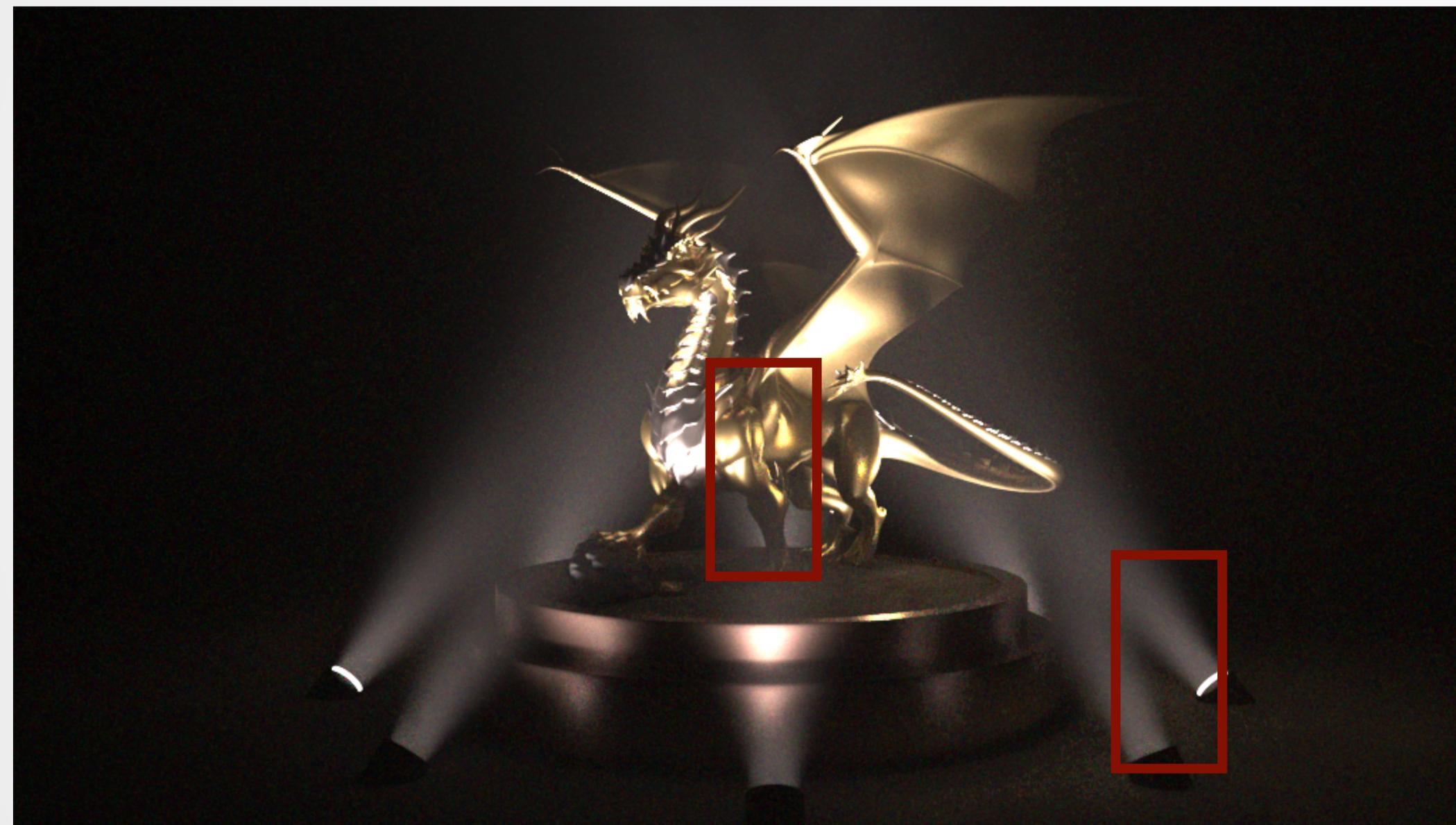
## Guided path tracing



69k guide paths ( $\approx 207\text{MB}$ )

# Dragon - 10h

## Guided path tracing + DBOR

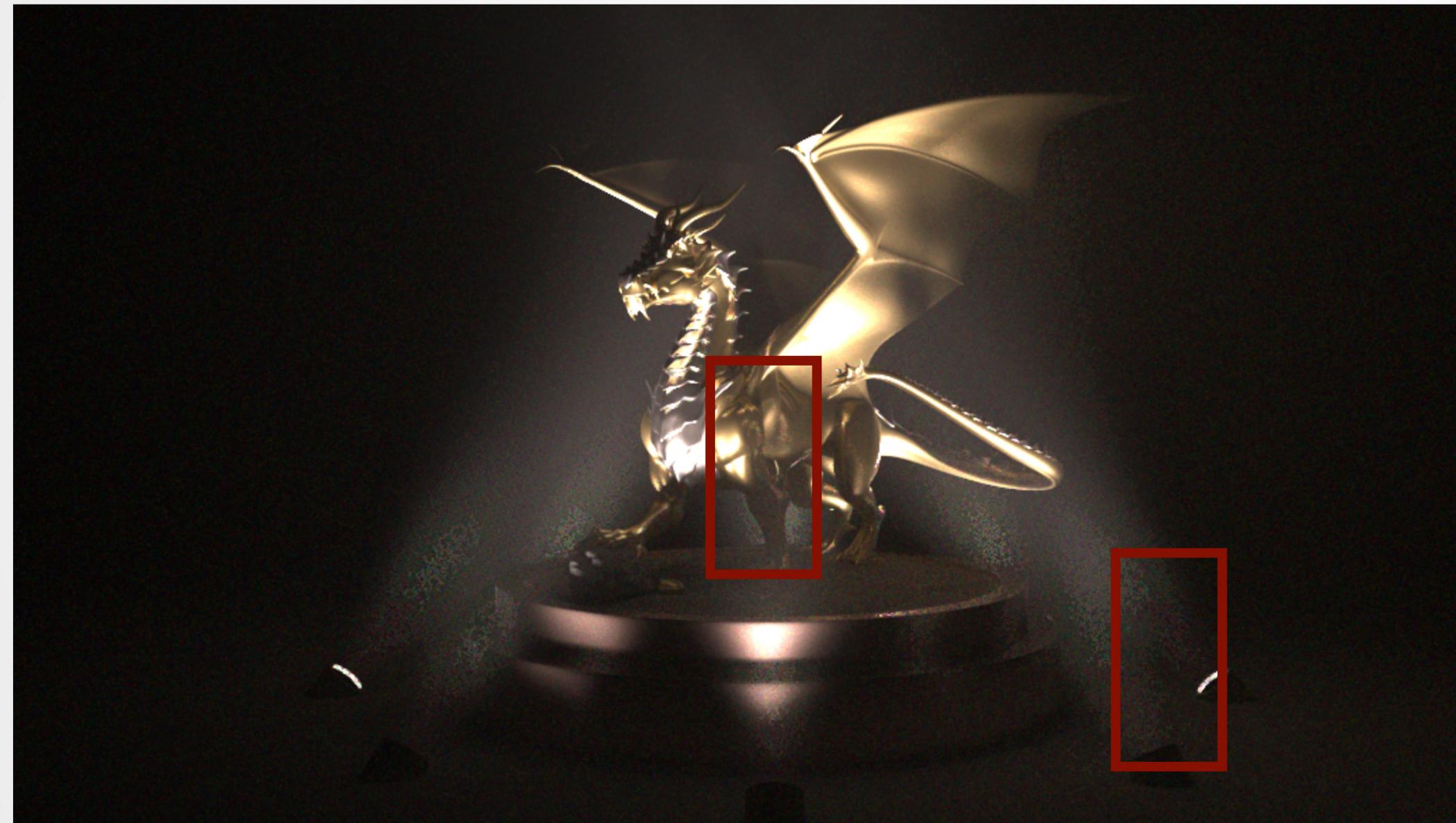


69k guide paths ( $\approx 207\text{MB}$ )

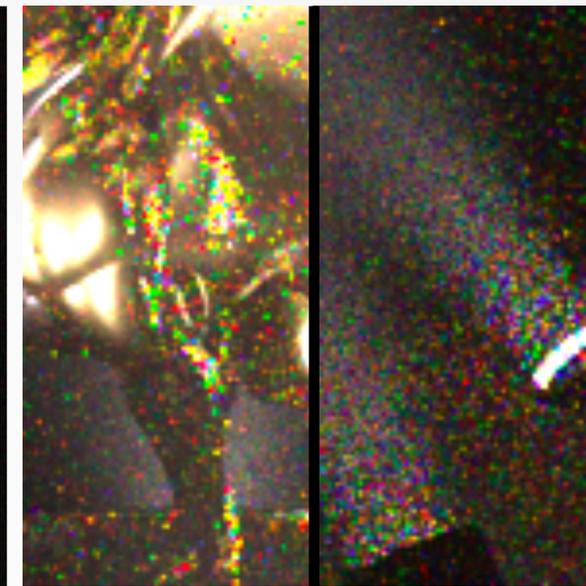
Guided PT+DBOR

# Dragon - 10h

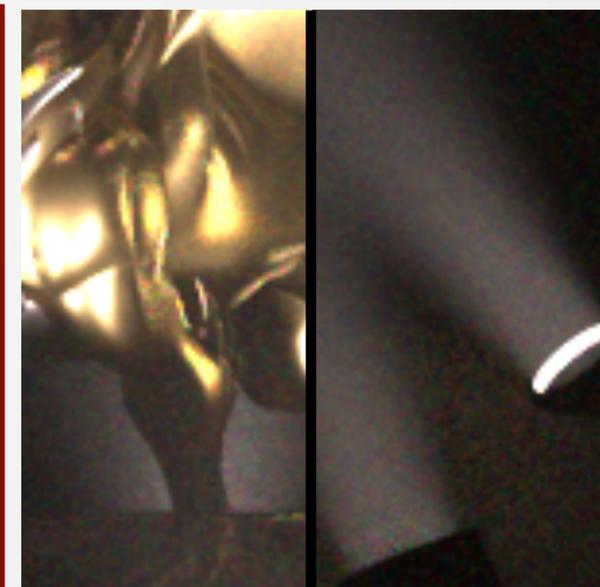
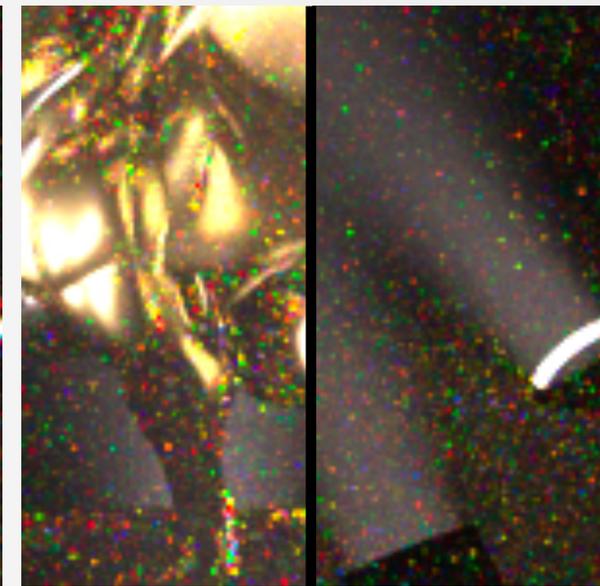
## Path tracing + DBOR



PT



Guided PT

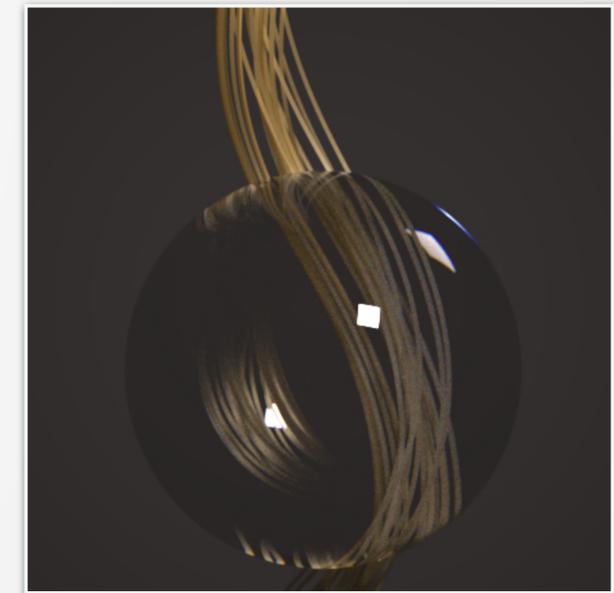


PT + DBOR

Guided PT+DBOR

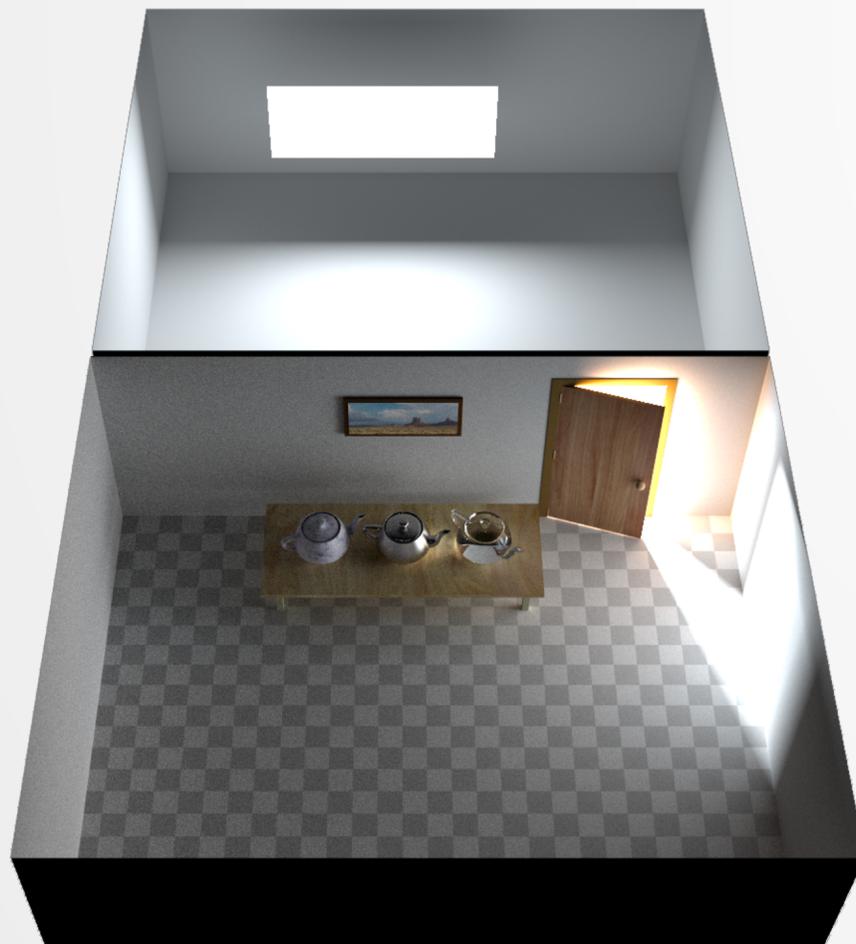
# Results

- More results in the paper/supplemental document



# Limitations & Future Work

- When every path is an outlier, no path is an outlier 🤔
- Impossible to cover all of path space with guide paths

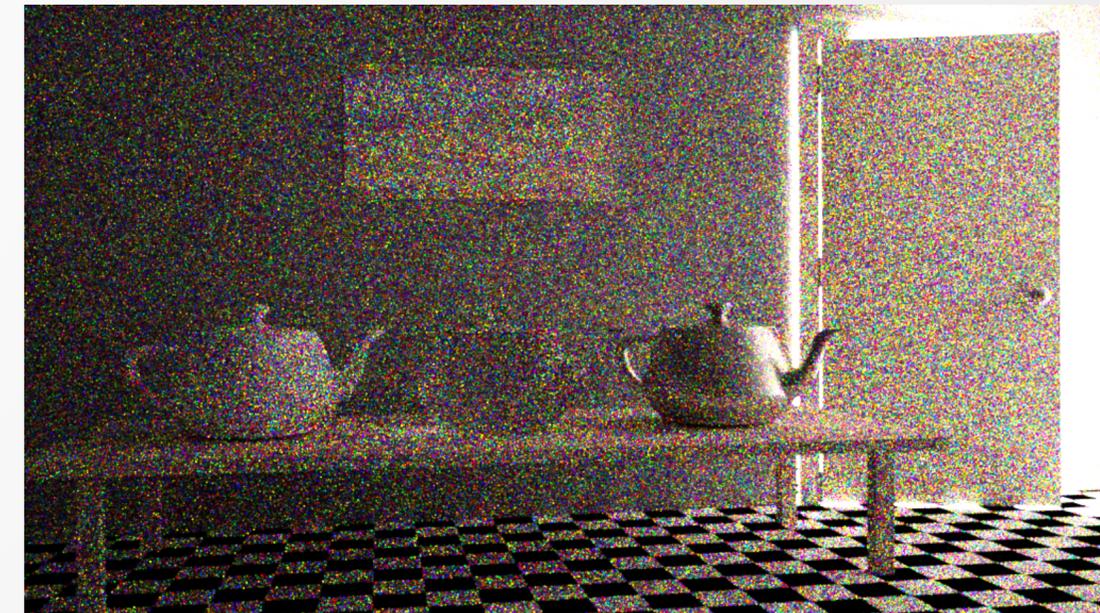


path tracing



7921spp, RMSE 0.75

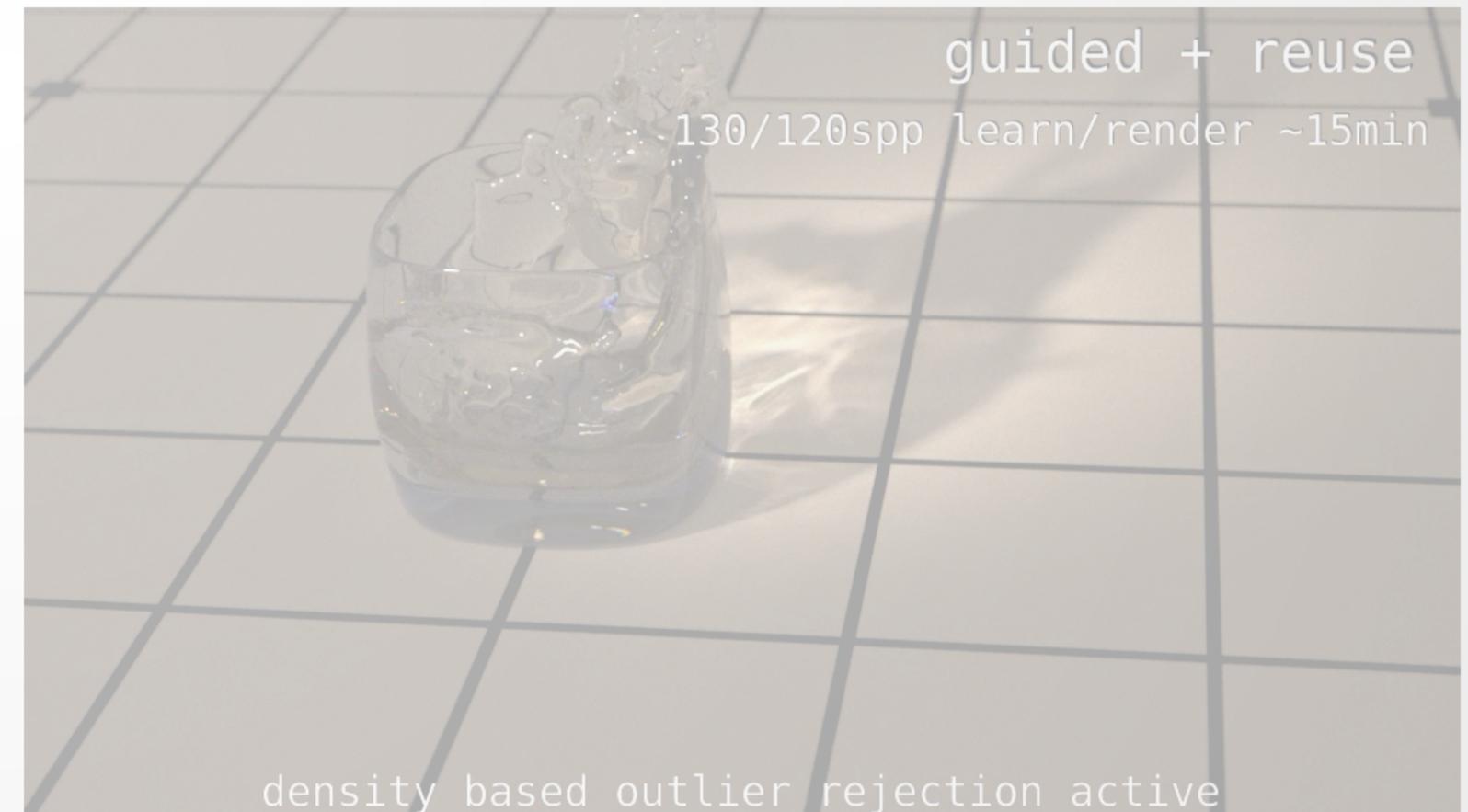
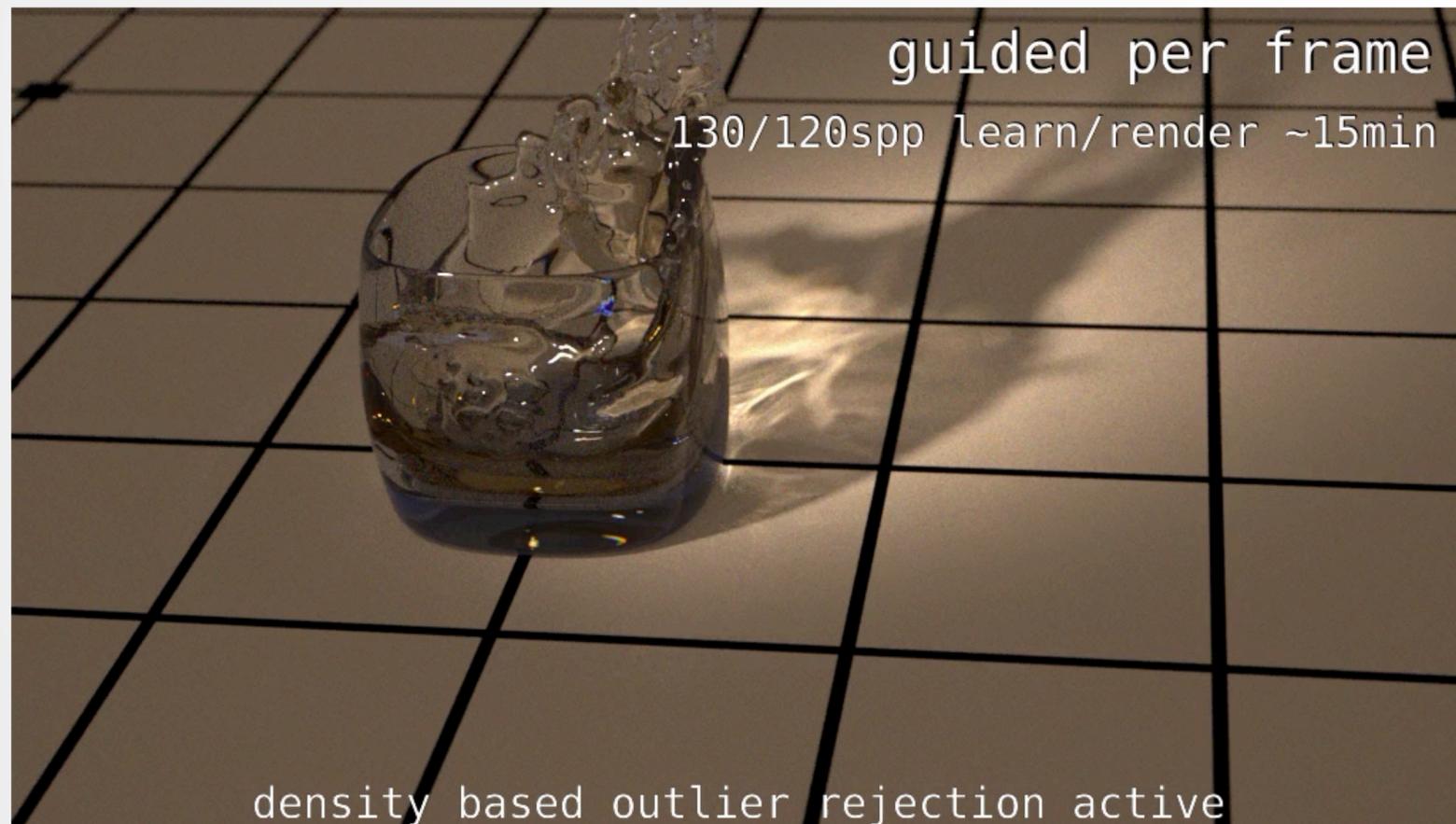
guided path tracing



4405spp, RMSE 1.30

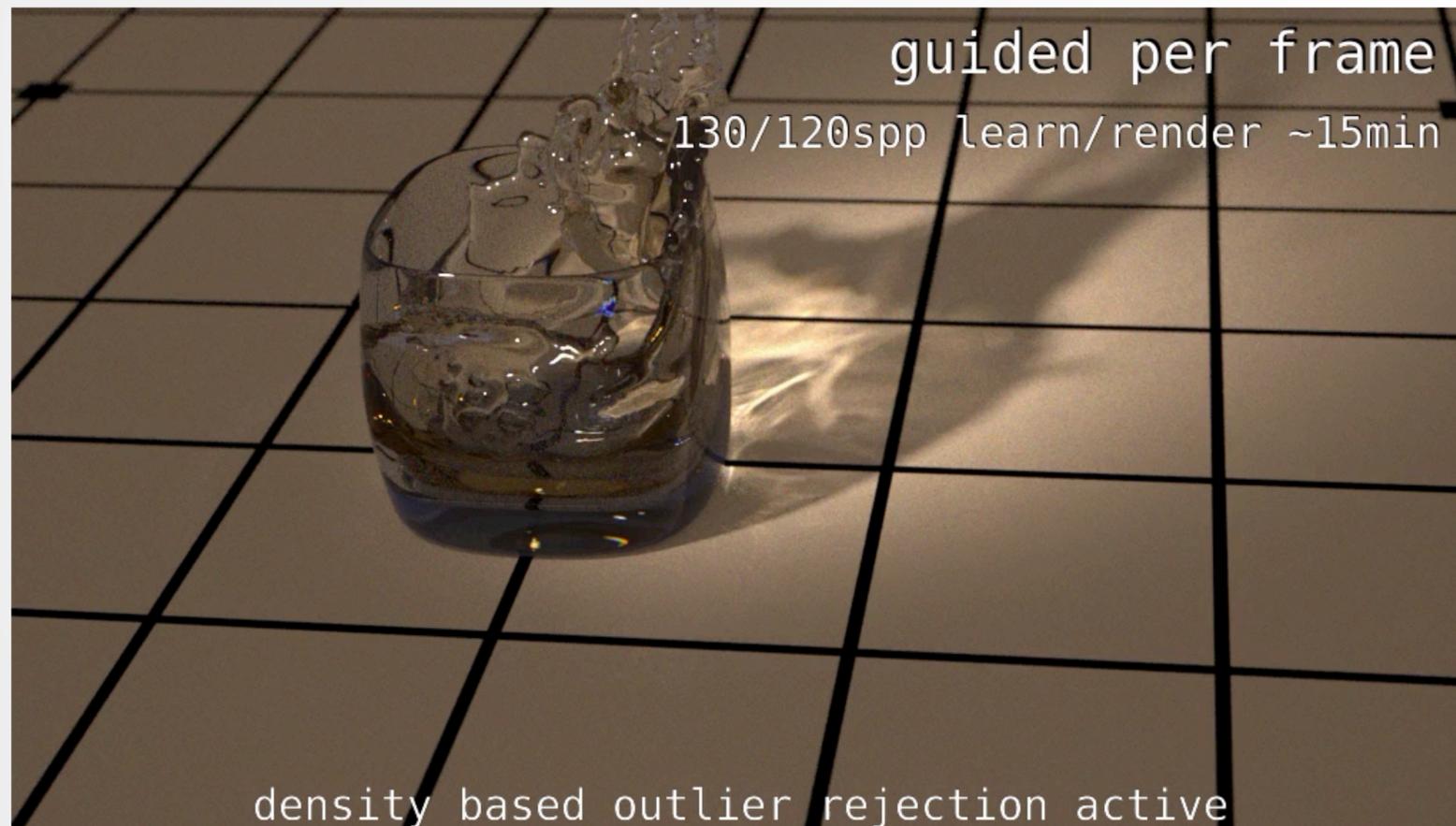
# Limitations & Future Work

- Temporal stability is challenging

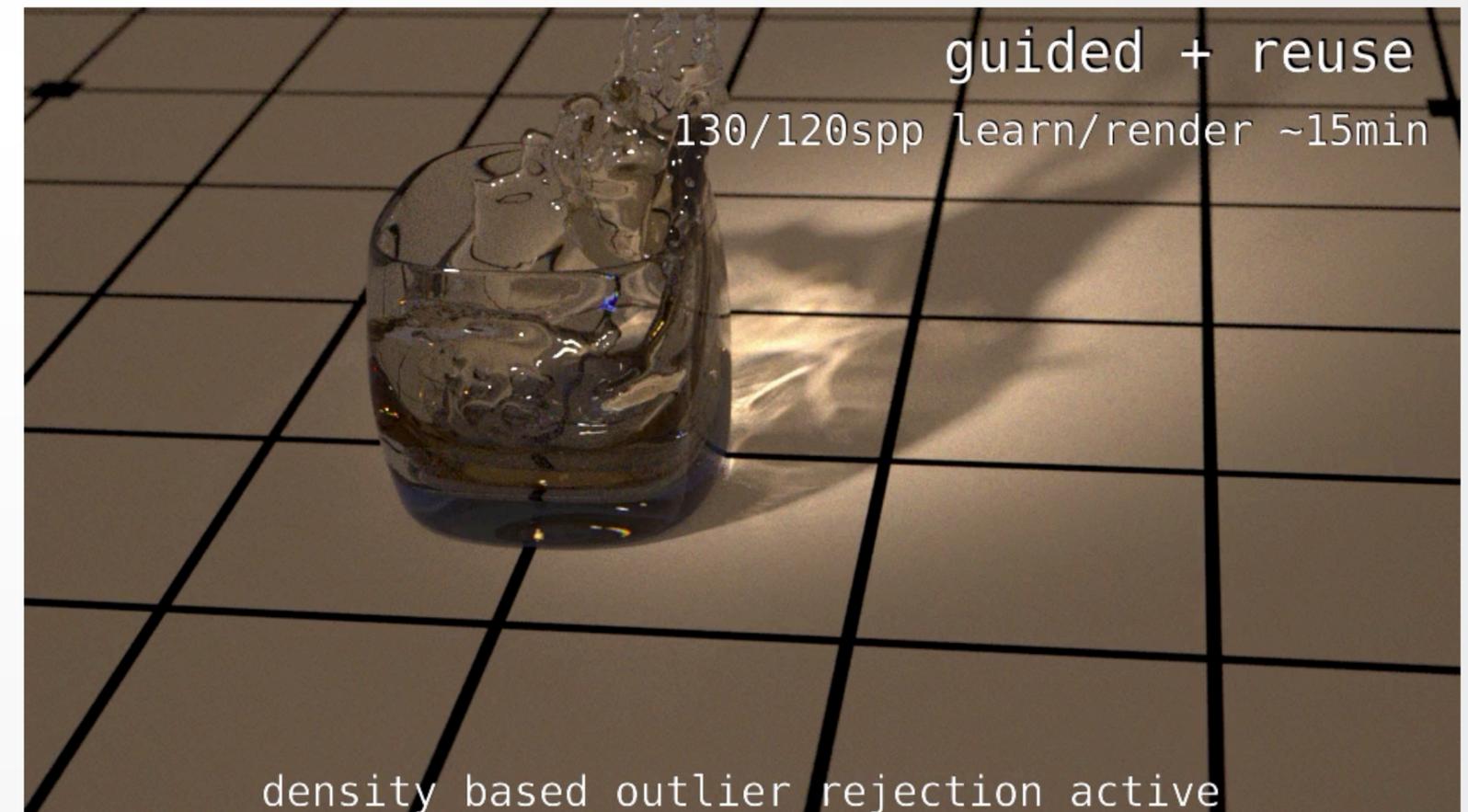


# Limitations & Future Work

- Temporal stability is challenging
- Improvement: Resample guide paths from previous frame



**independent guide path cache**



**resampled guide path cache**

# Conclusion

- Data driven path sampling with local exploration behaviour
- Path construction using information of multiple existing paths
- Other Monte Carlo samplers possible as the unguided sampler
- Similarities to Sequential Monte Carlo
- Guide paths could be hand picked (artist) or from Markov Chain without detailed balance



Sponsored by



# Thank you!



**SIGGRAPH**  
ASIA 2018  
T O K Y O

CONFERENCE 4 - 7 December 2018  
EXHIBITION 5 - 7 December 2018  
Tokyo International Forum, Japan  
[SA2018.SIGGRAPH.ORG](http://SA2018.SIGGRAPH.ORG)



# Discarded Ideas

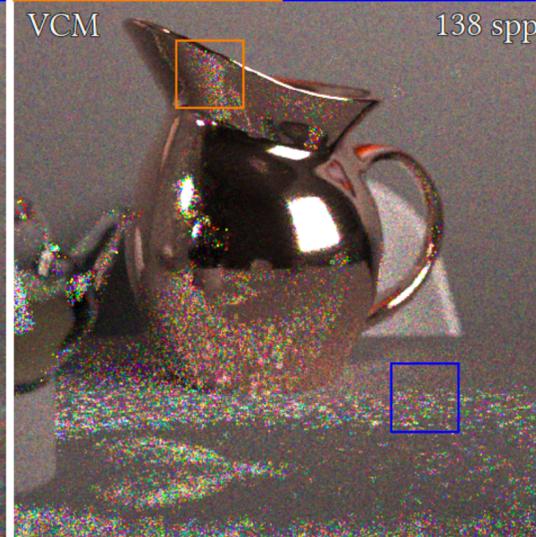
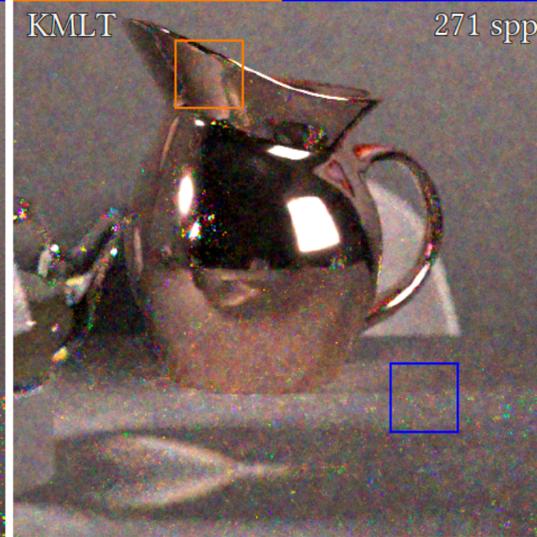
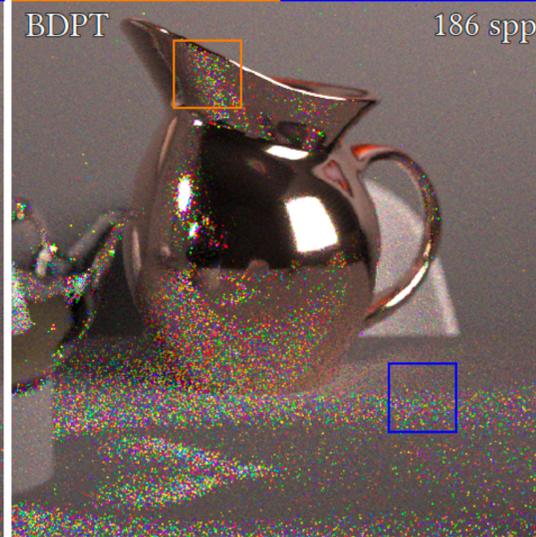
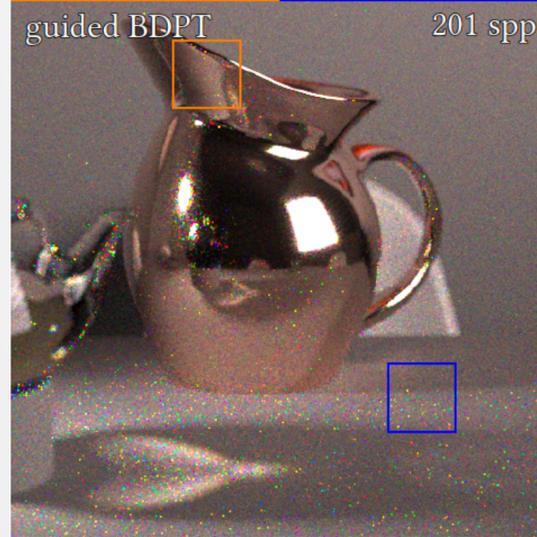
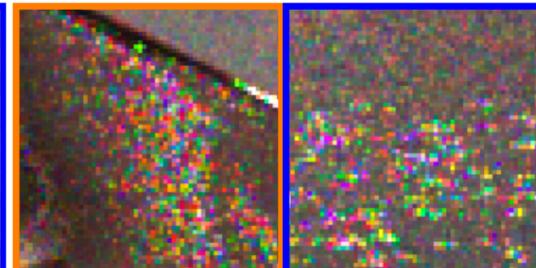
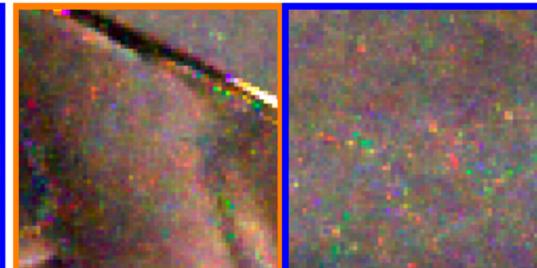
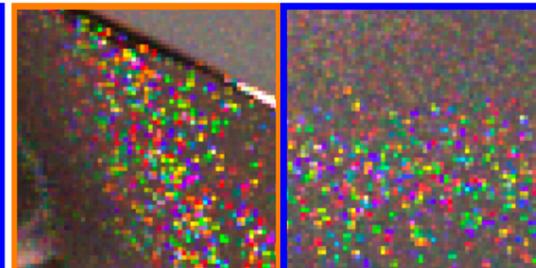
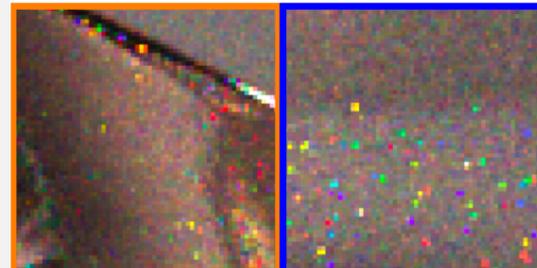
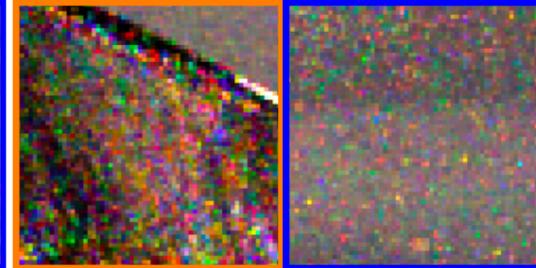
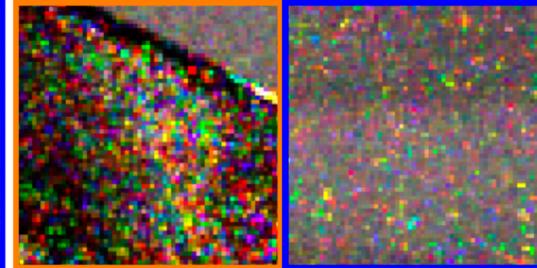
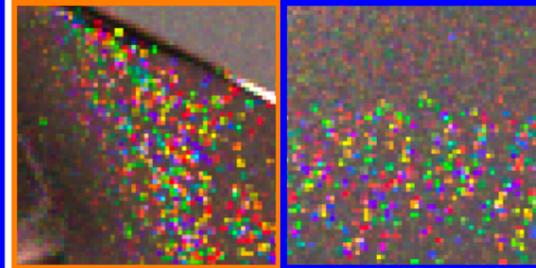
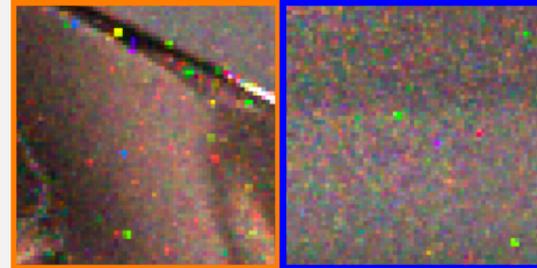
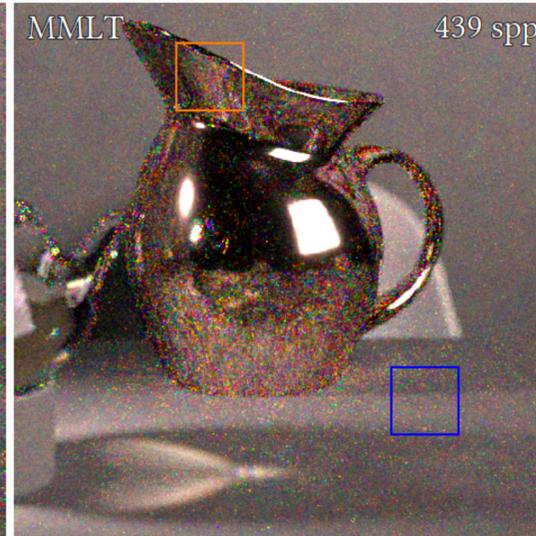
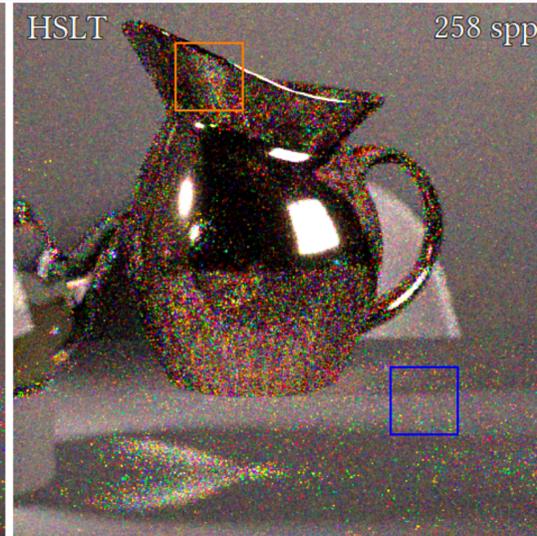
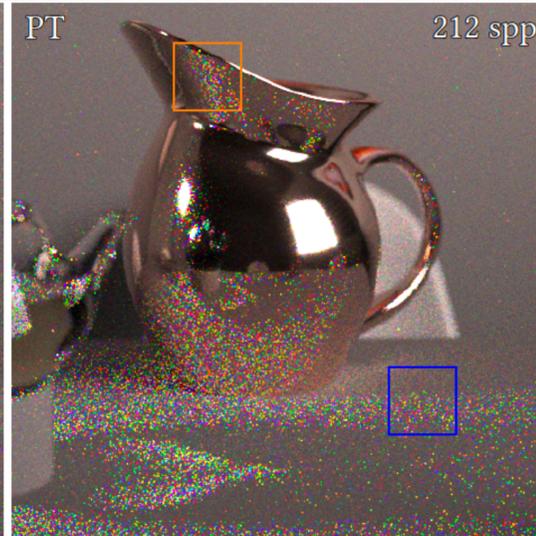
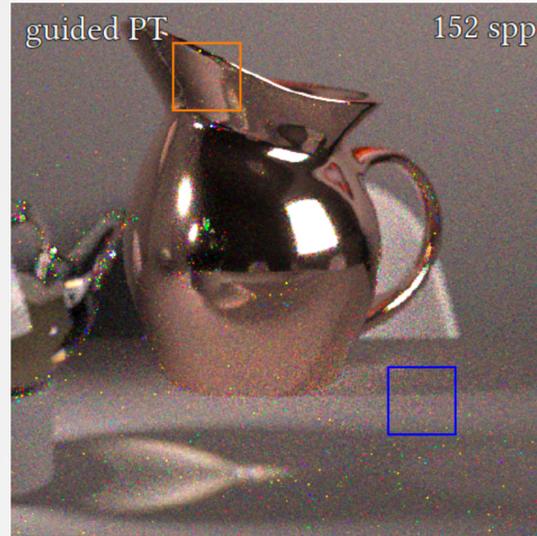
- Constant Kernel
- Repeated 3D search for NN
- Metropolis Hastings to resample guide paths
- Relaxation of guide paths (photon map-style)

**guided PT**

**PT**

**HSLT**

**MMLT**



**guided BDPT**

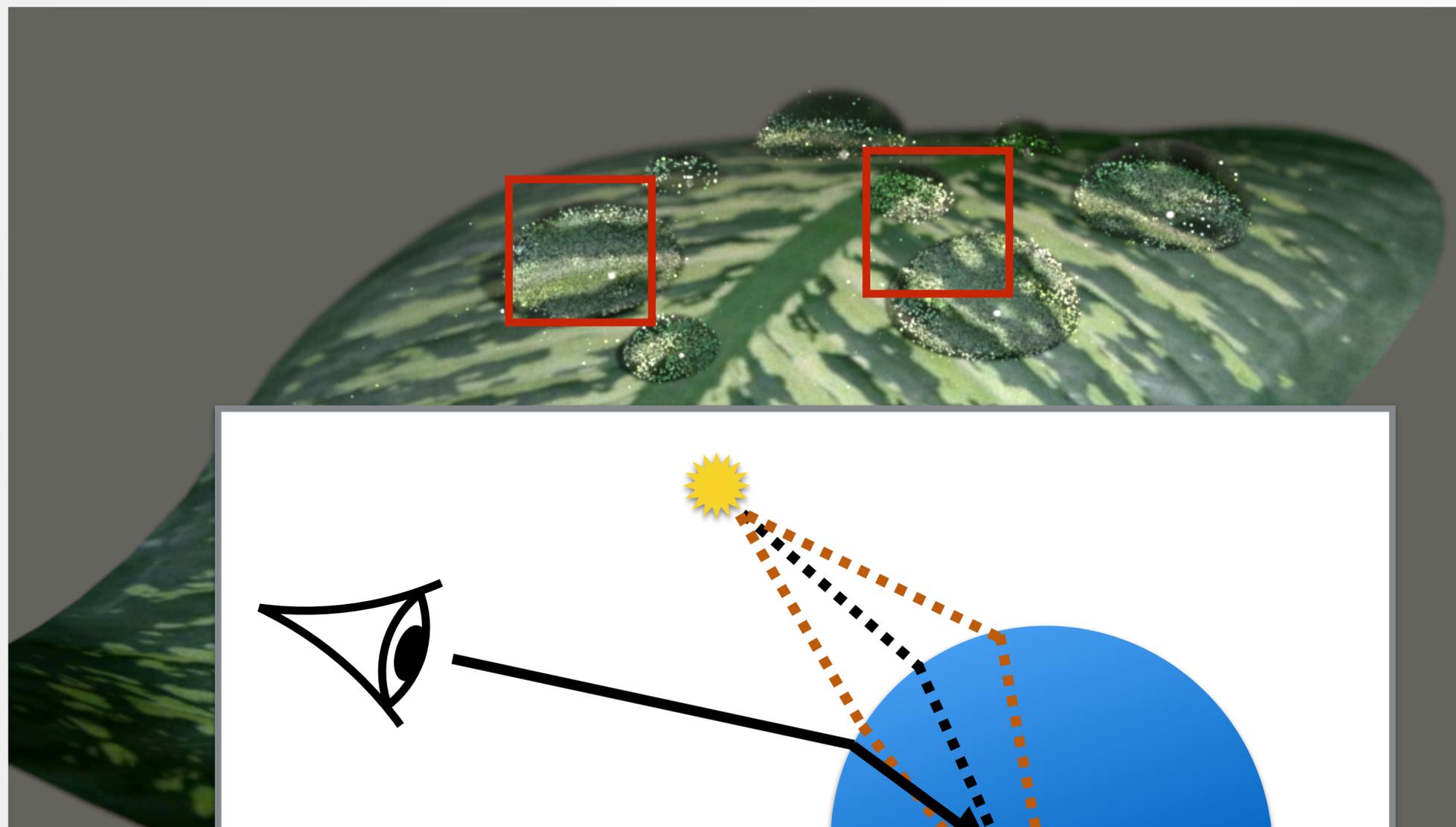
**BDPT**

**KMLT**

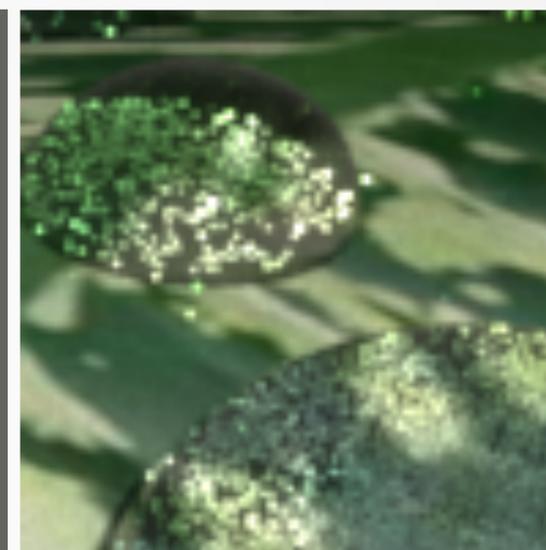
**VCM**

# Recent Guiding Methods

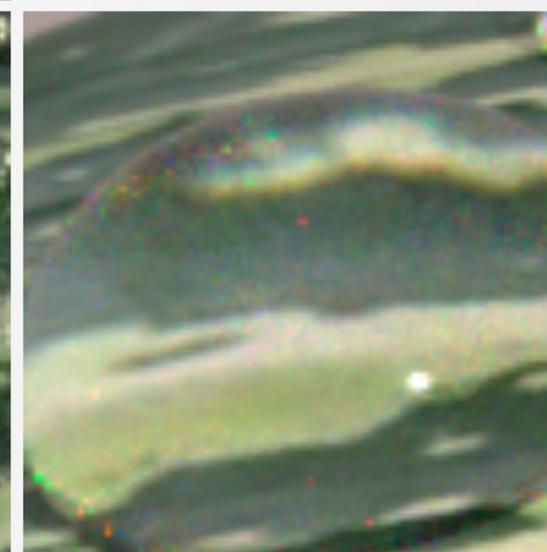
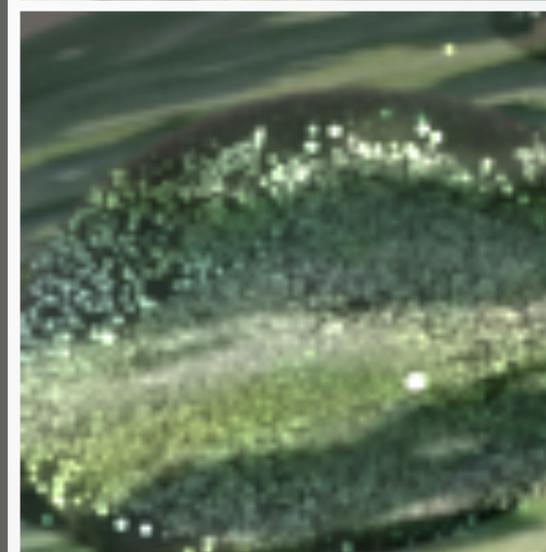
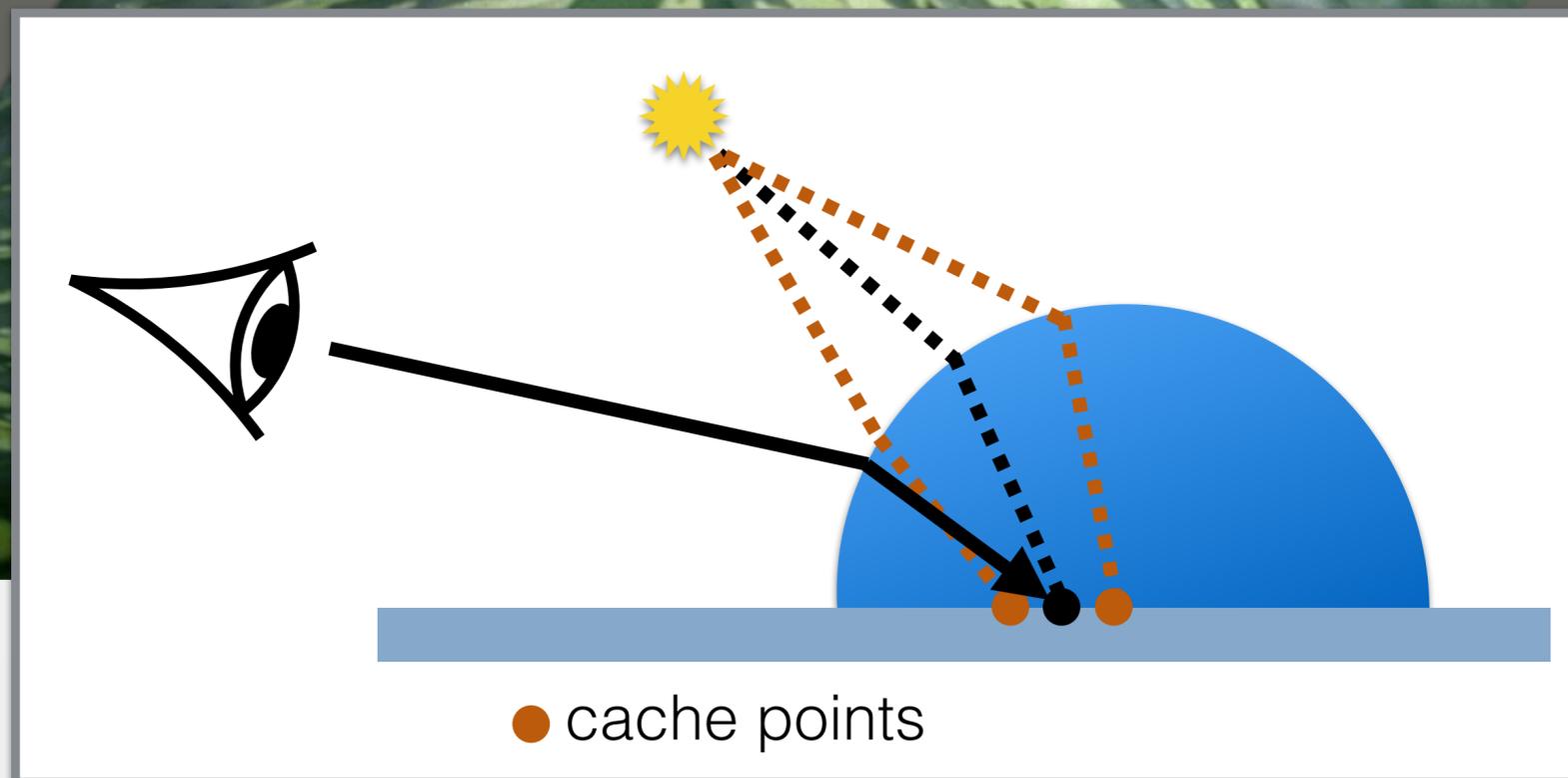
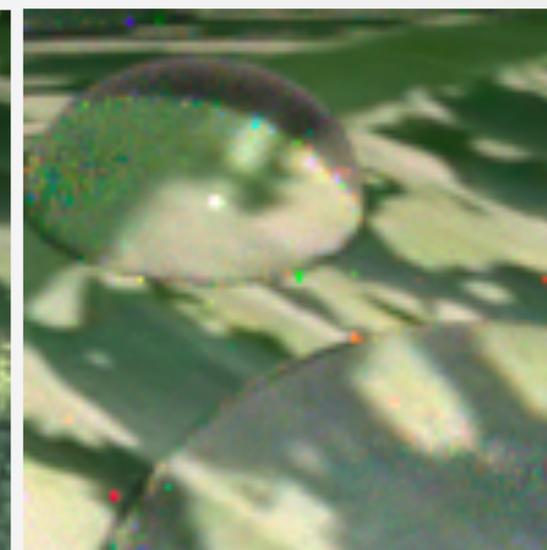
Vorba et al. [2014]



Vorba et al. [2014]

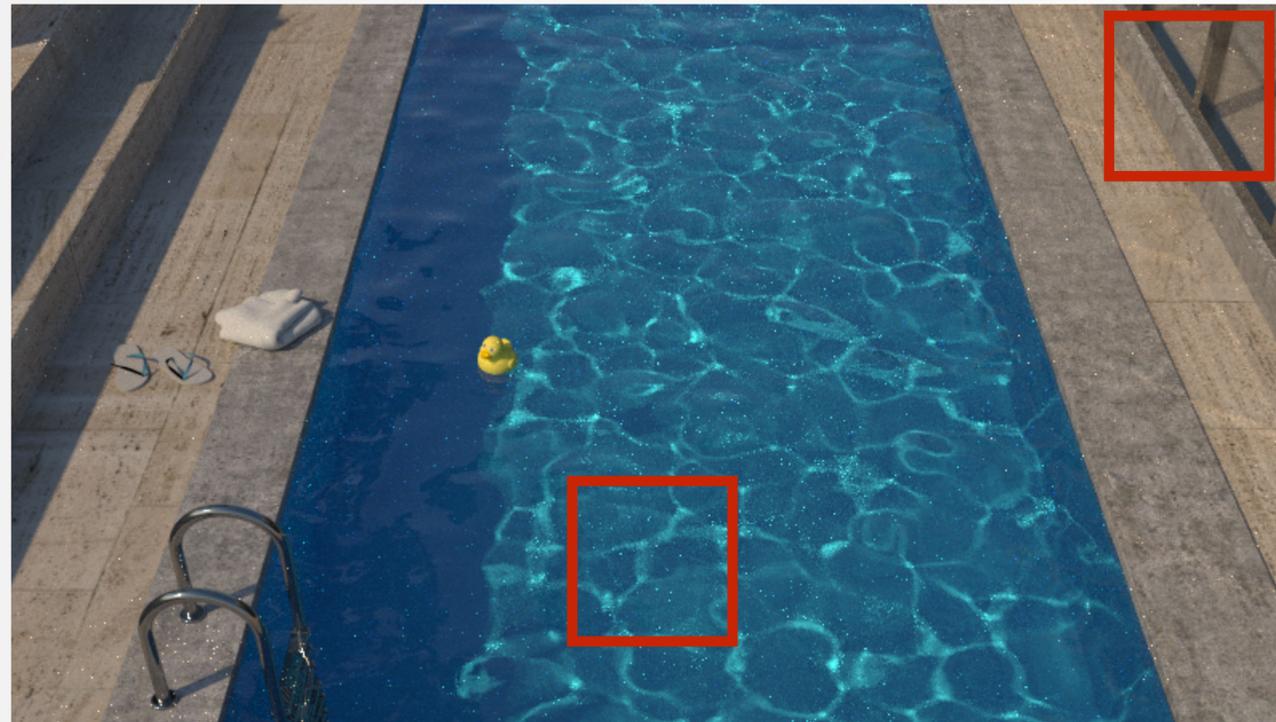


ours

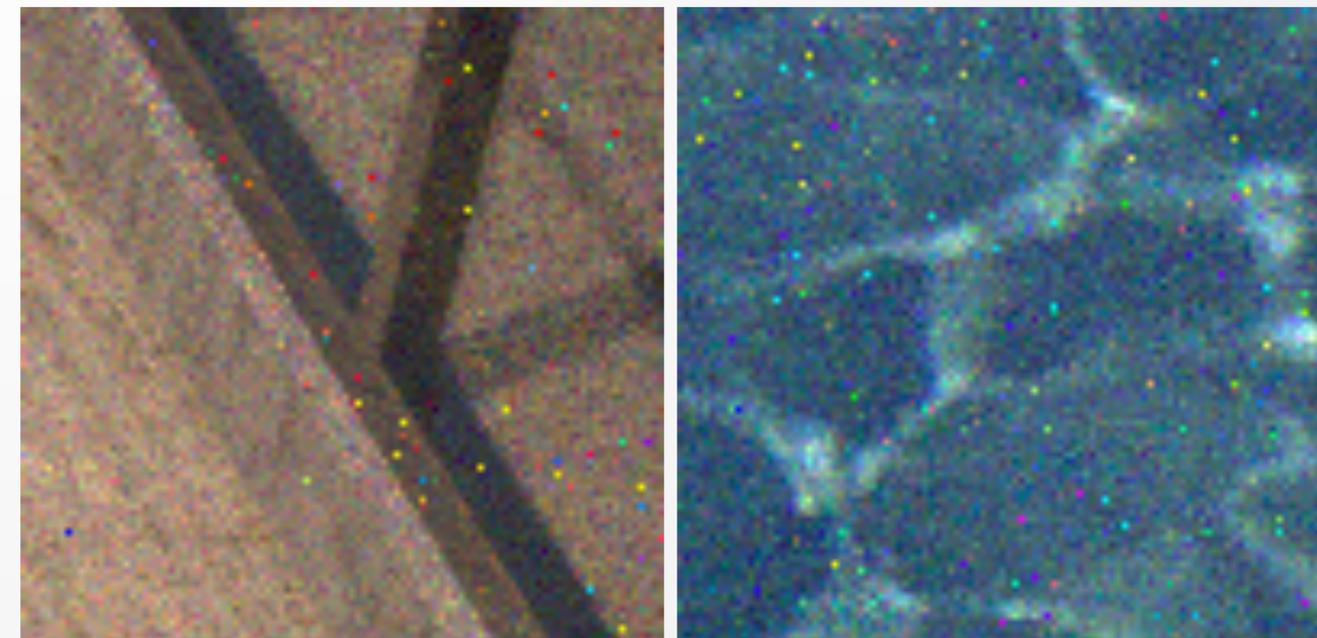
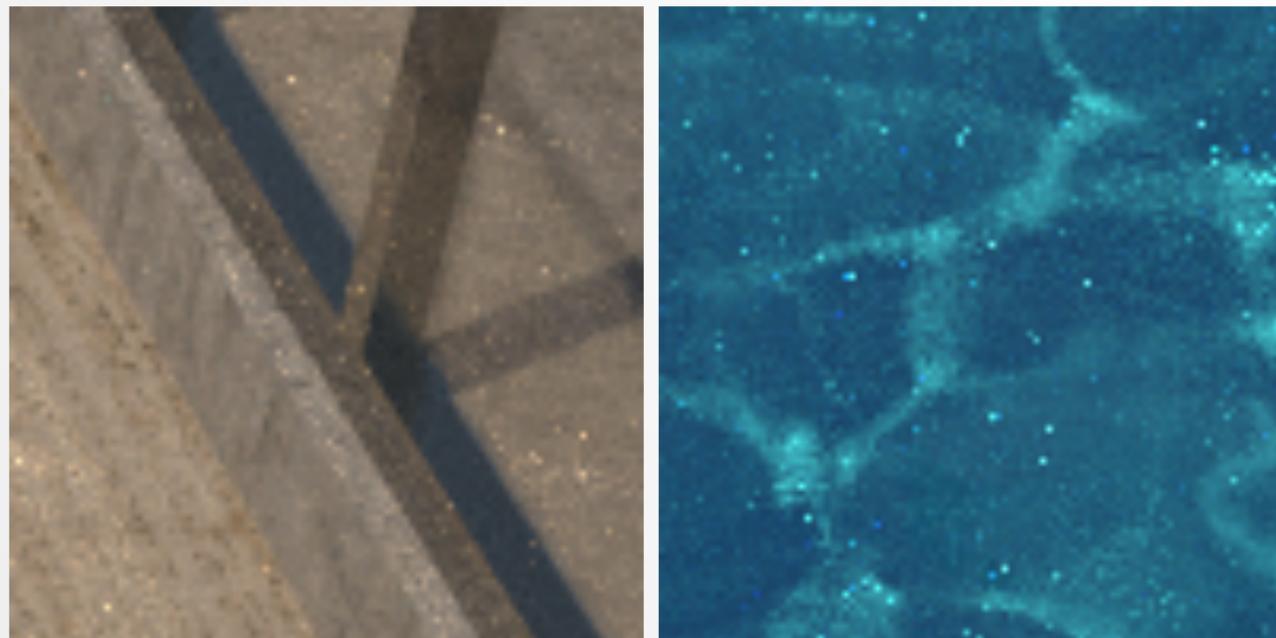
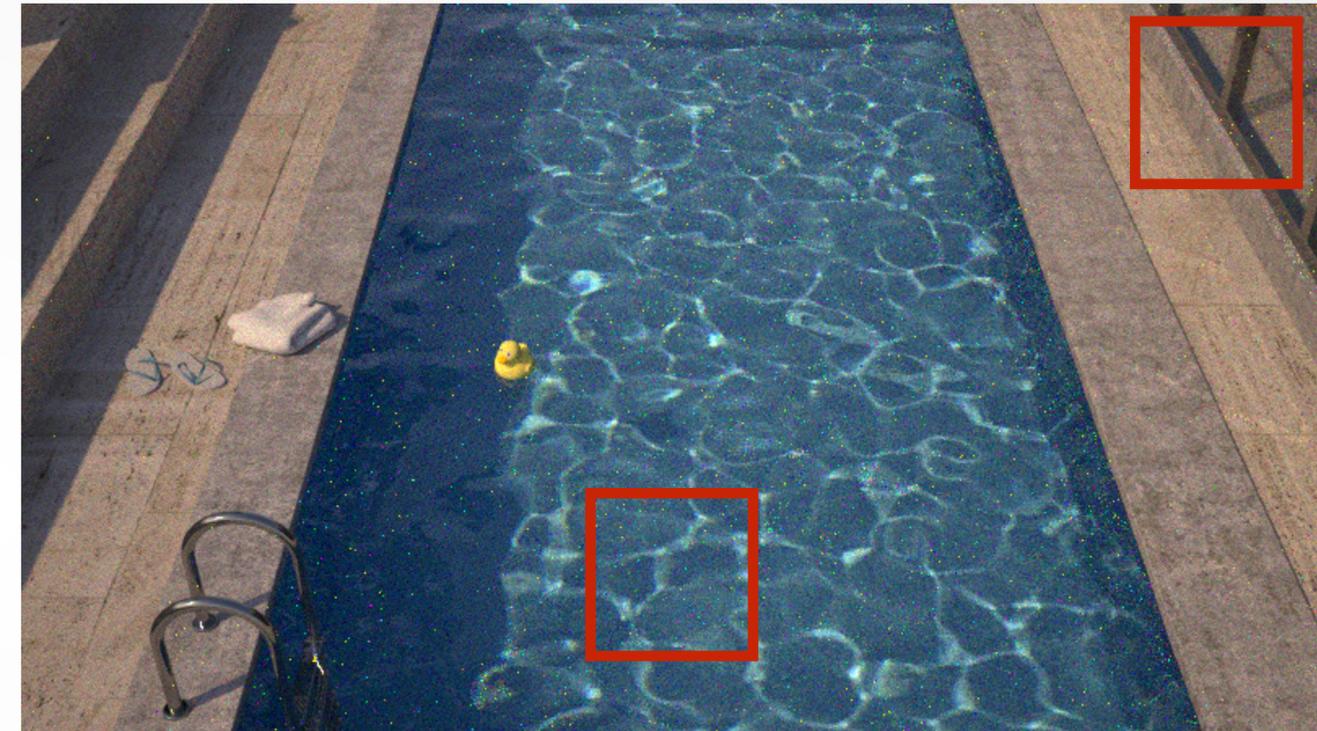


# Recent Guiding Methods

Müller et al. [2017] 256spp

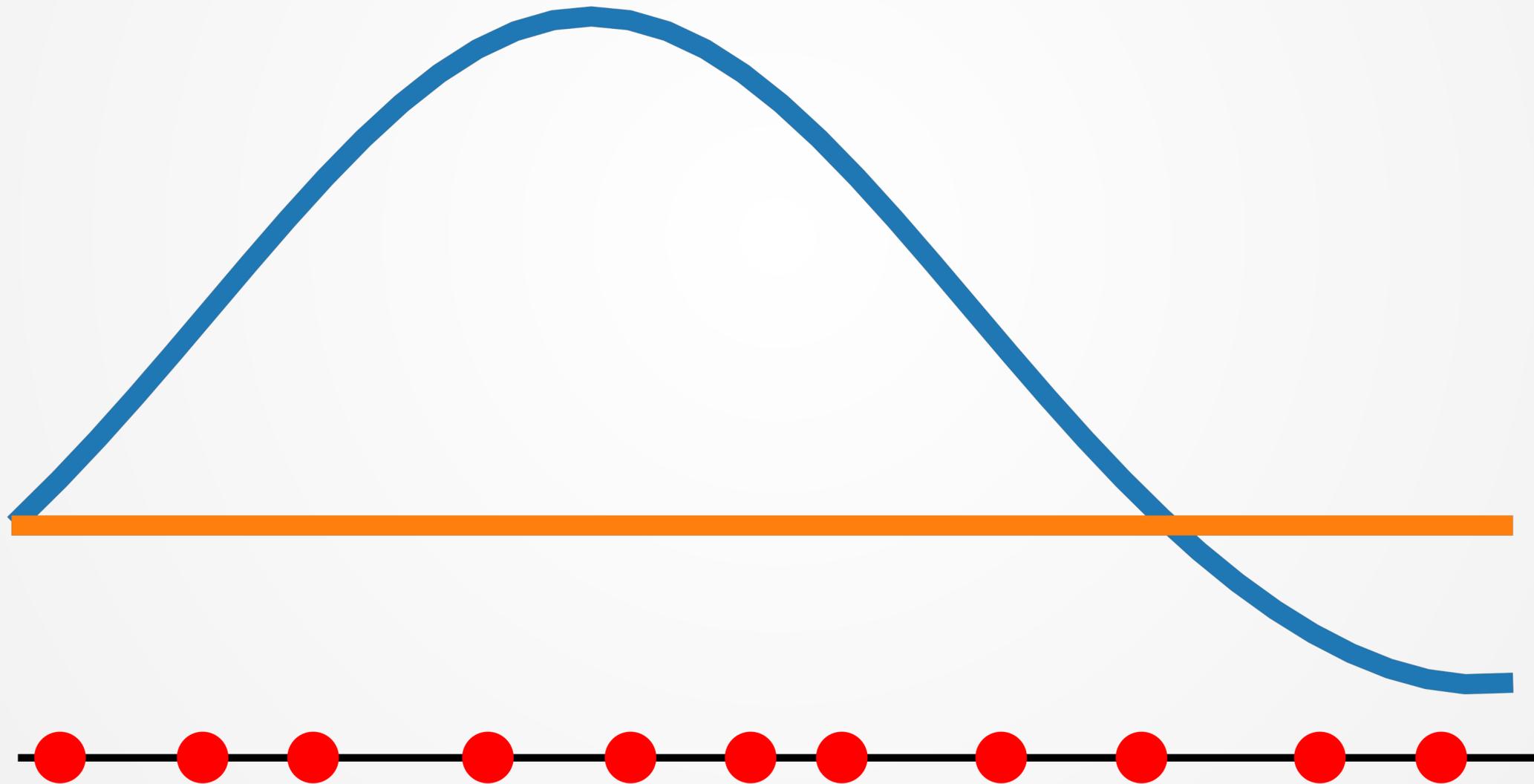


ours 260spp



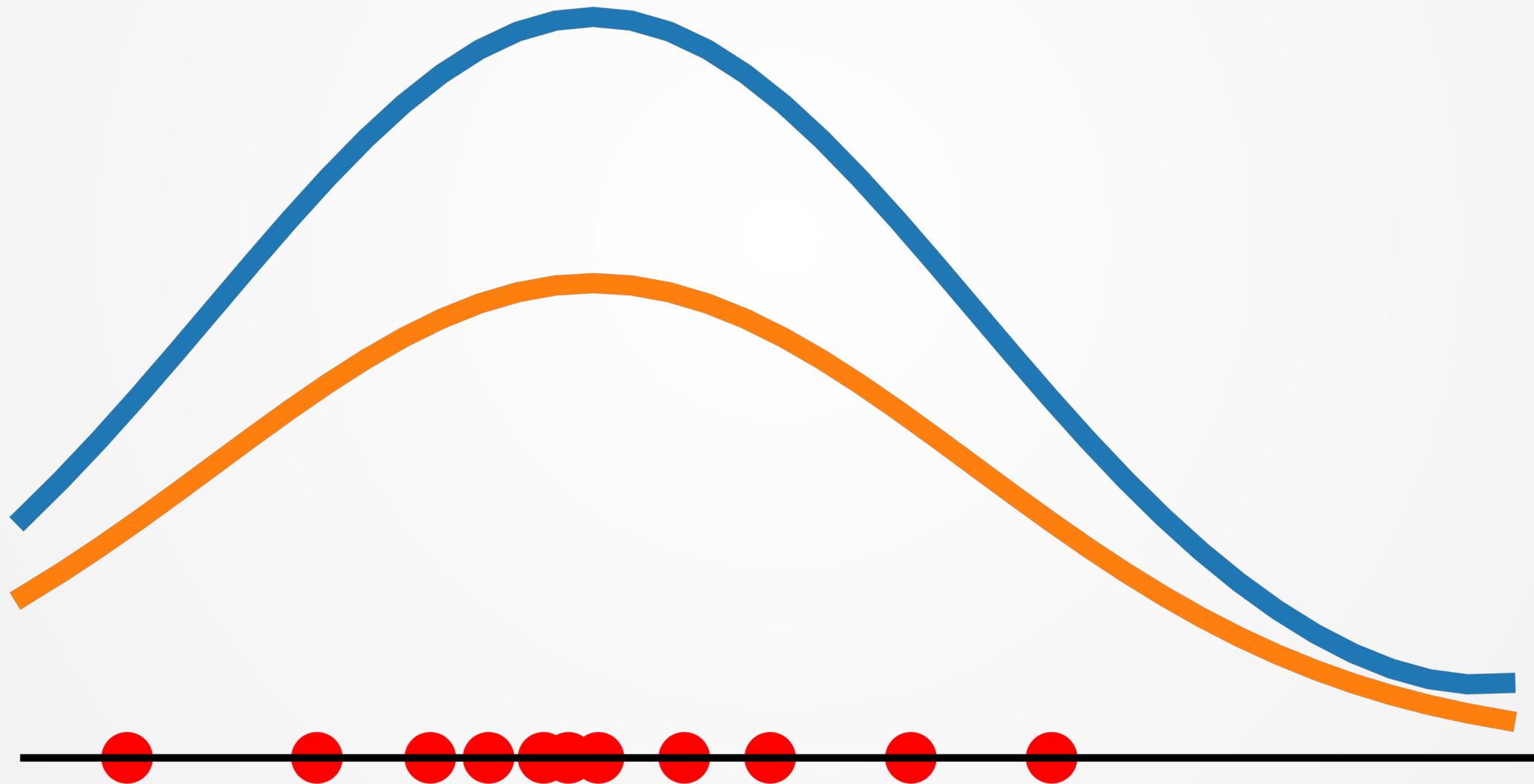
# Illustration in 1D

- Uniform sampling



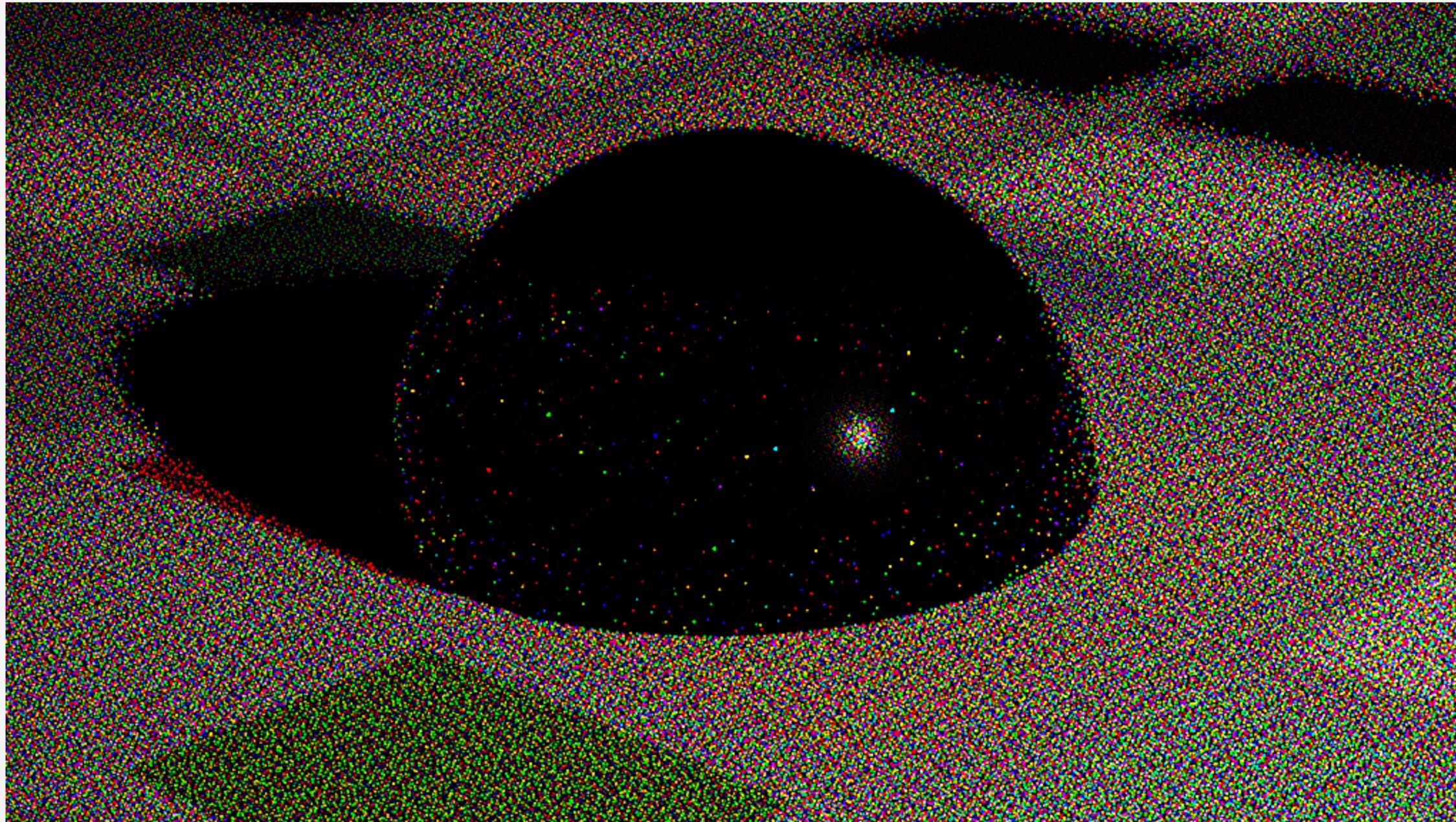
# Illustration in 1D

- Importance sampling



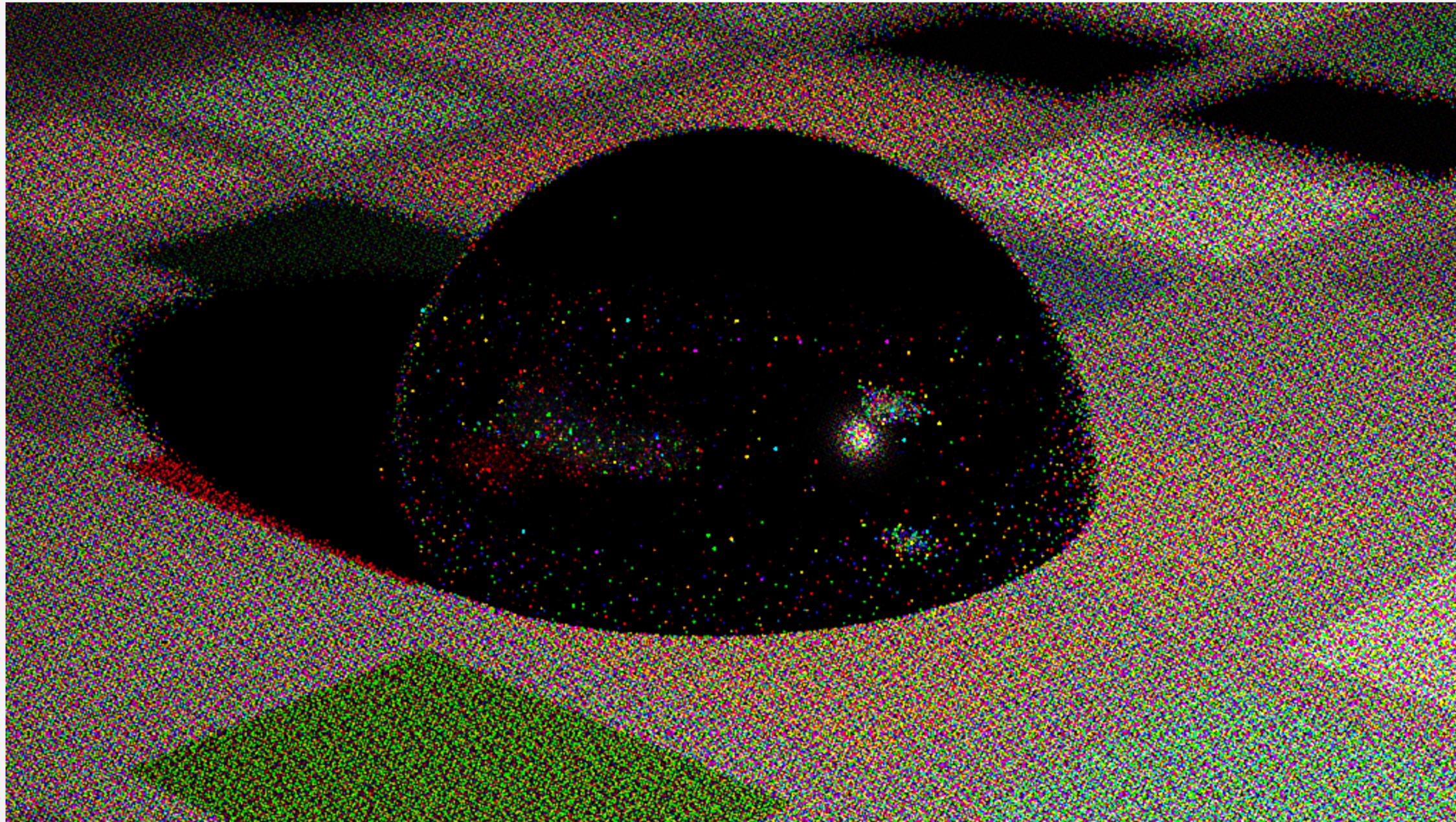
# Guiding Behaviour

Guided path tracing - iteration 1



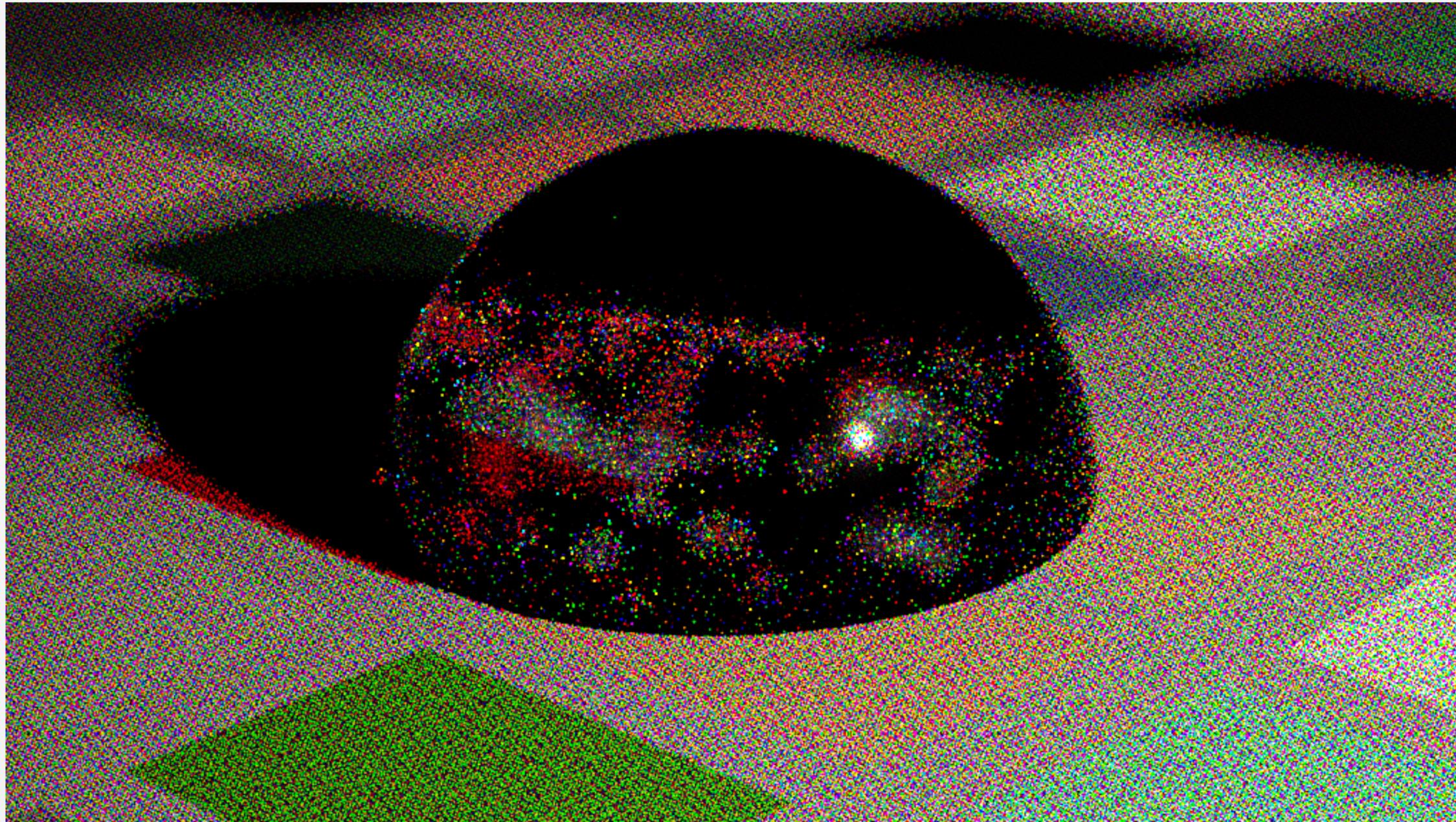
# Guiding Behaviour

Guided path tracing - iteration 2



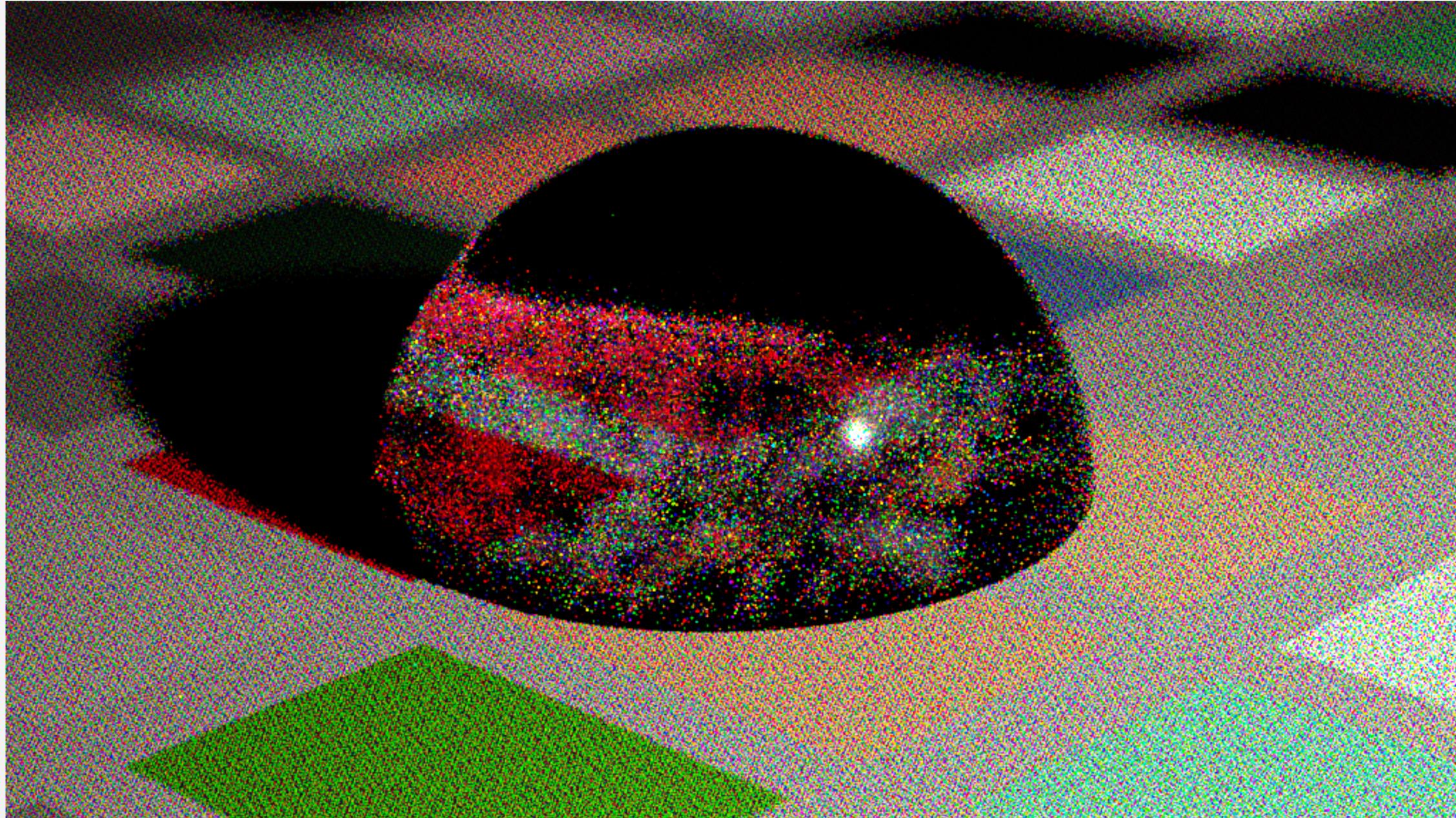
# Guiding Behaviour

Guided path tracing - iteration 3



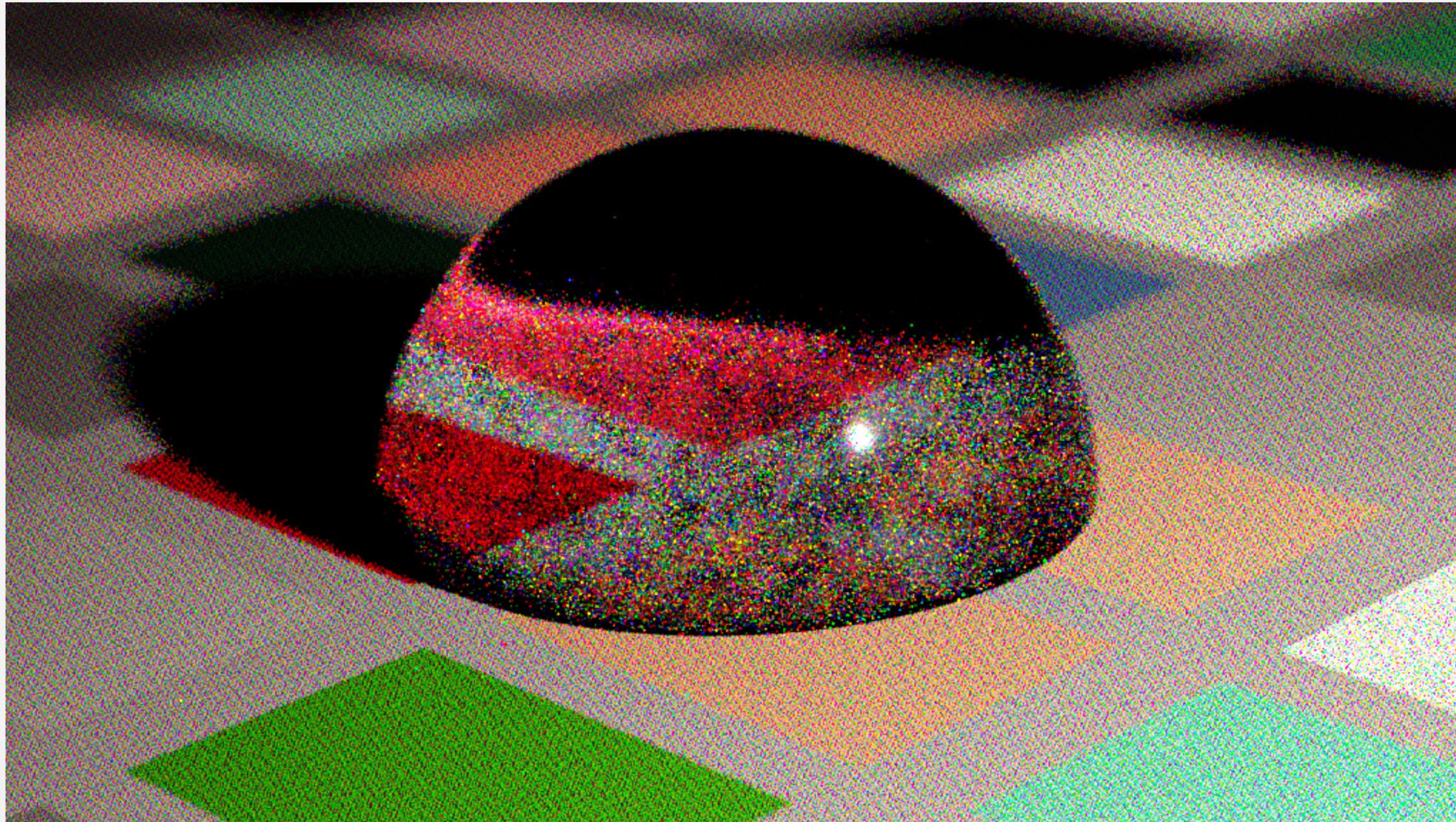
# Guiding Behaviour

Guided path tracing - iteration 4



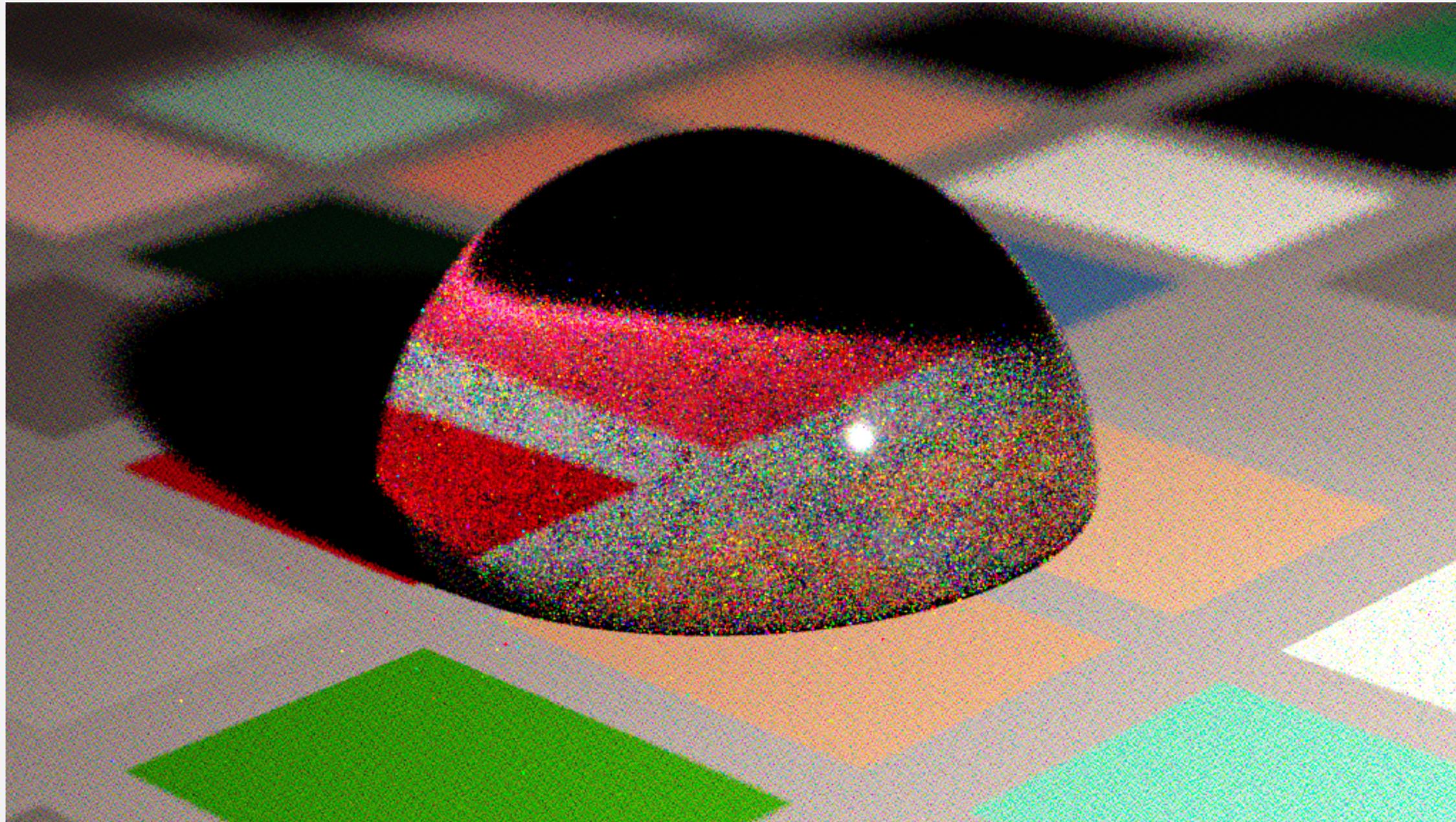
# Guiding Behaviour

Guided path tracing - iteration 8

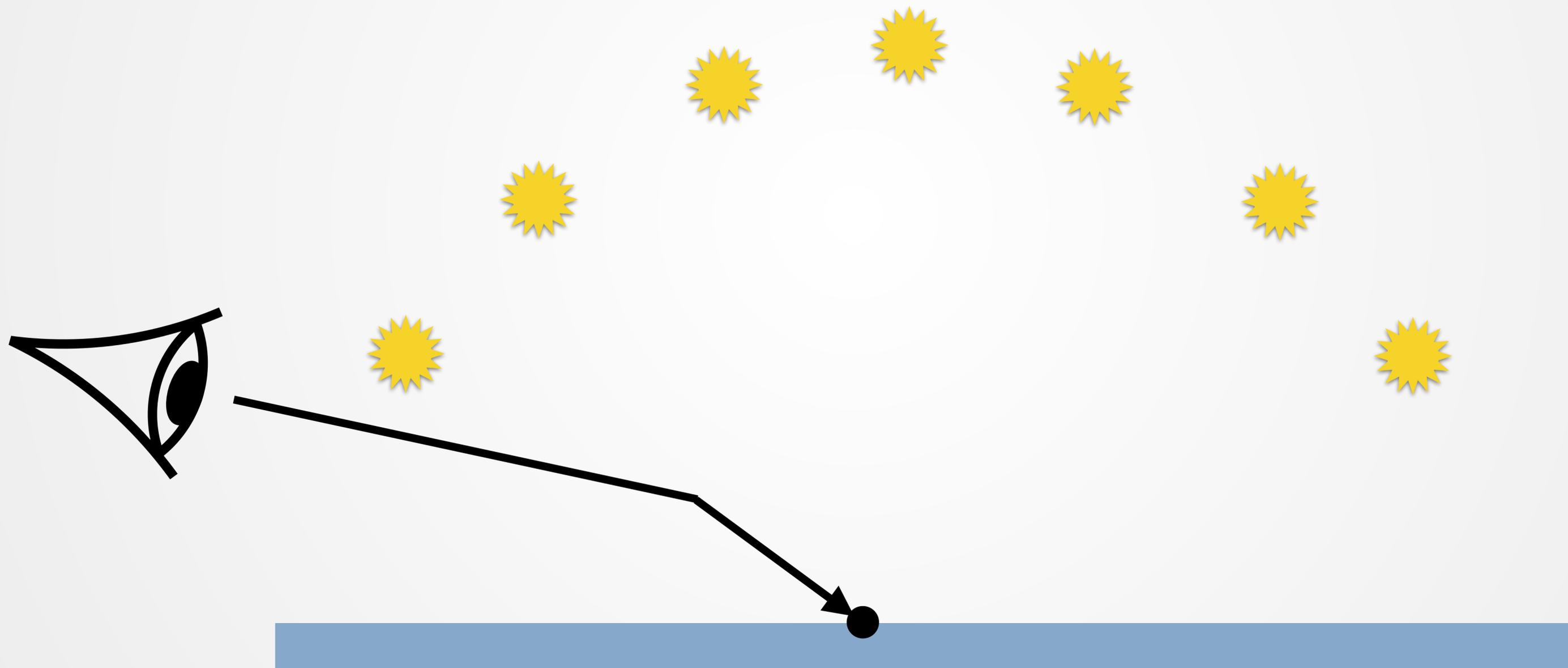


# Guiding Behaviour

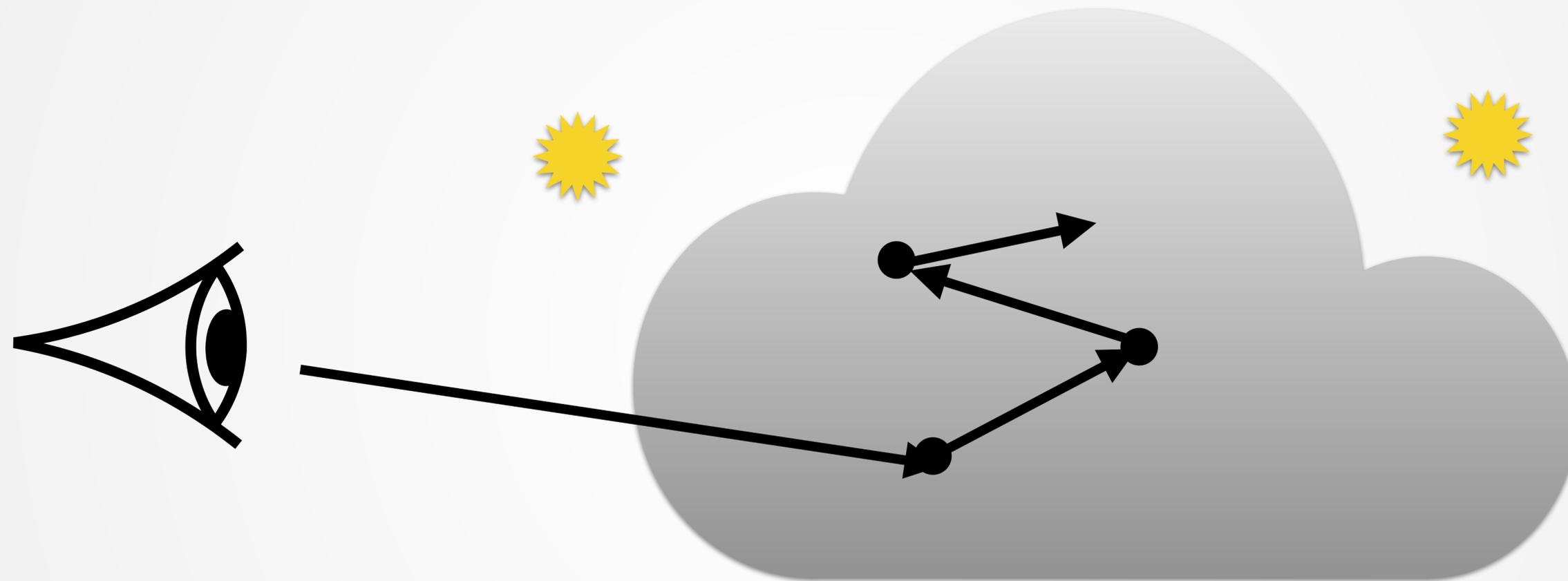
Guided path tracing - iteration 16



# Recent related guiding methods



# Recent related guiding methods

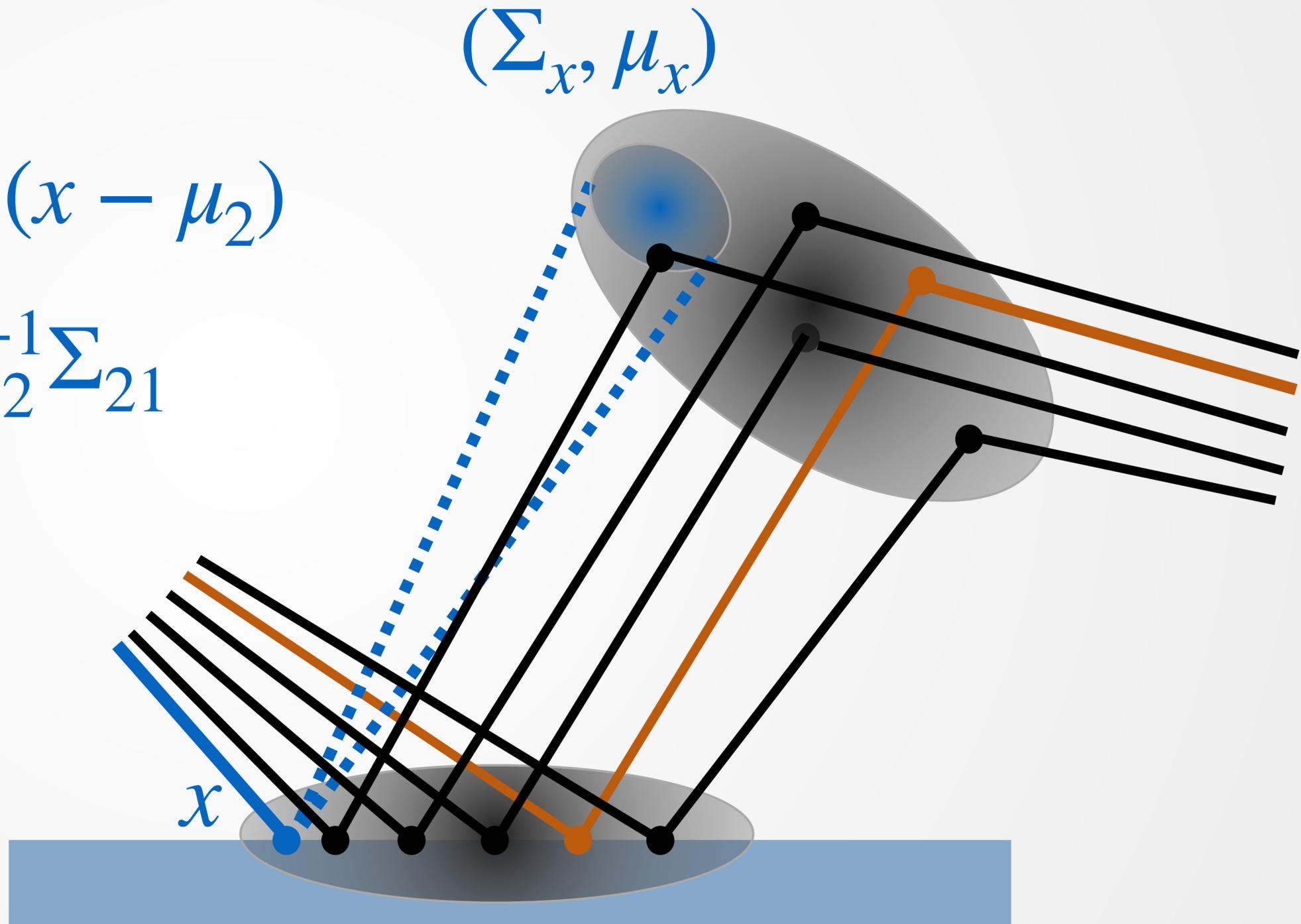




# Conditional Gaussians

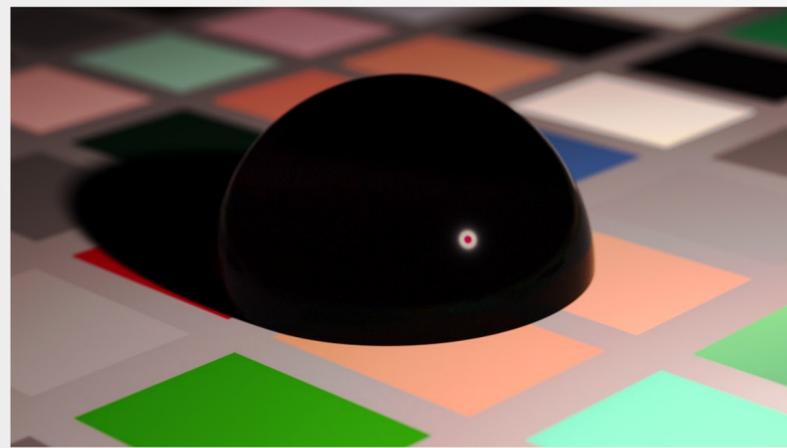
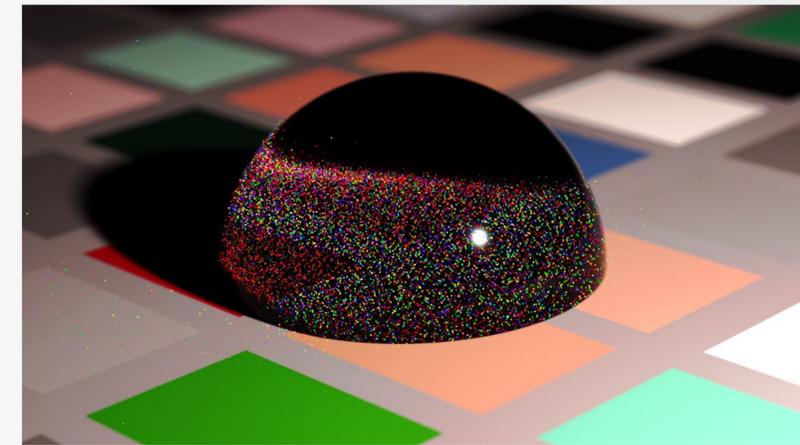
$$\mu_x = \mu_1 + \Sigma_{12} \Sigma_{22}^{-1} (x - \mu_2)$$

$$\Sigma_x = \Sigma_{11} - \Sigma_{12} \Sigma_{22}^{-1} \Sigma_{21}$$



# Selecting Guide Paths

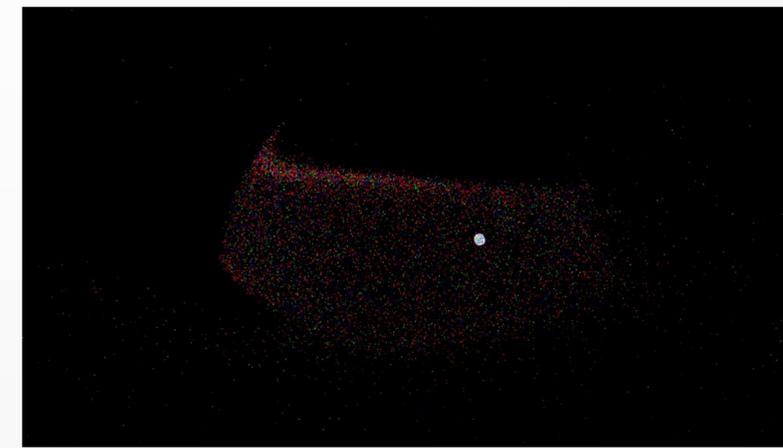
- DBOR: DeCoro et al. [2010] / Zirr et al. [2018]
- Framebuffer cascade with histogram
- Samples split according to throughput



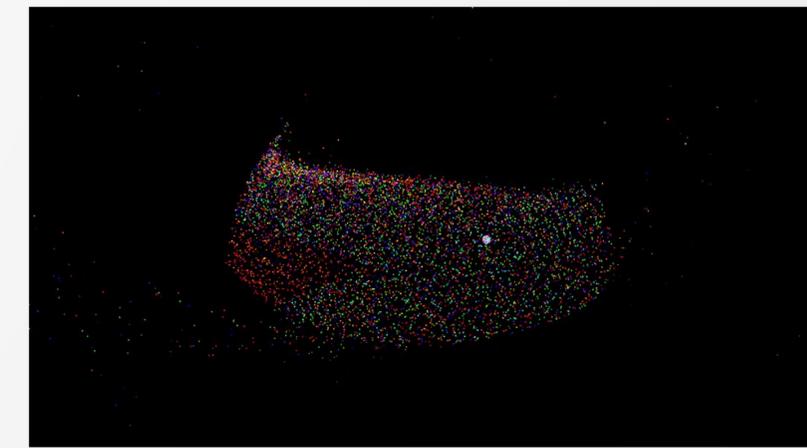
$C \in [0, 8^1]$



$C \in [8^1, 8^2]$



$C \in [8^2, 8^3]$



$C \in [8^3, \infty)$

# Remaining outliers

- Either: stop adding, clear the framebuffer and restart rendering.
  - Outliers possible because of yet unexplored lighting features or gaps between guide paths.
- Or: keep adding, don't clear the framebuffer
  - Outliers will remain in the framebuffer and won't converge away in reasonable time.

# Dining Room - 30min

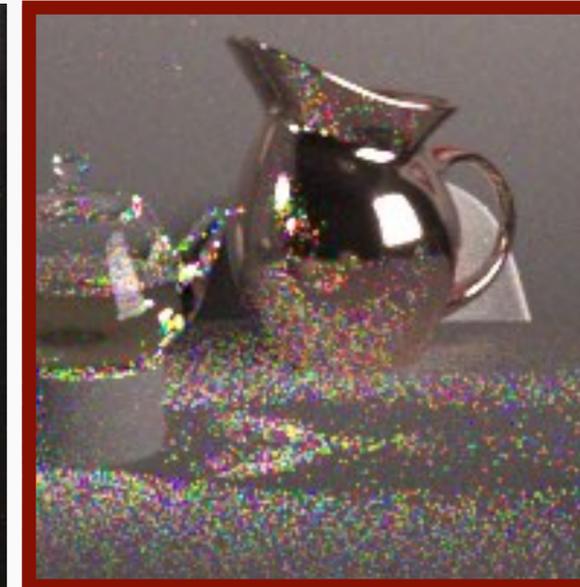
reference



# Dining Room - 30min

path tracing

RMSE 0.0435

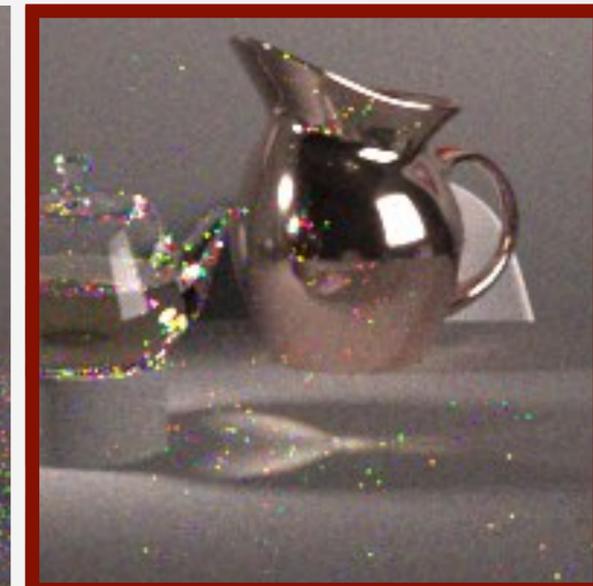
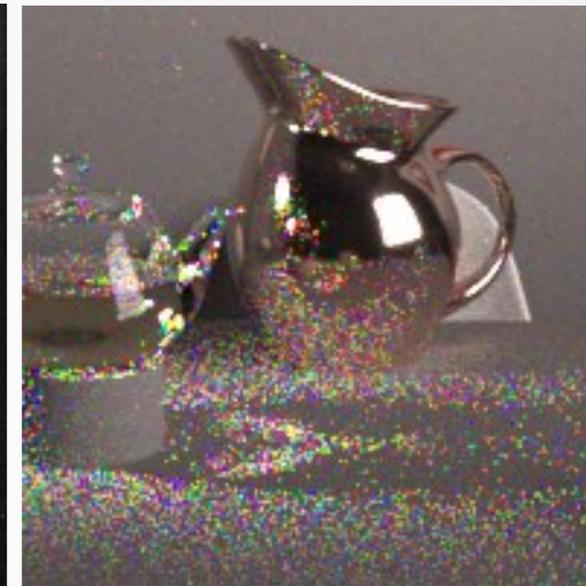


# Dining Room - 30min

guided path tracing

RMSE 0.0435

RMSE 0.0345

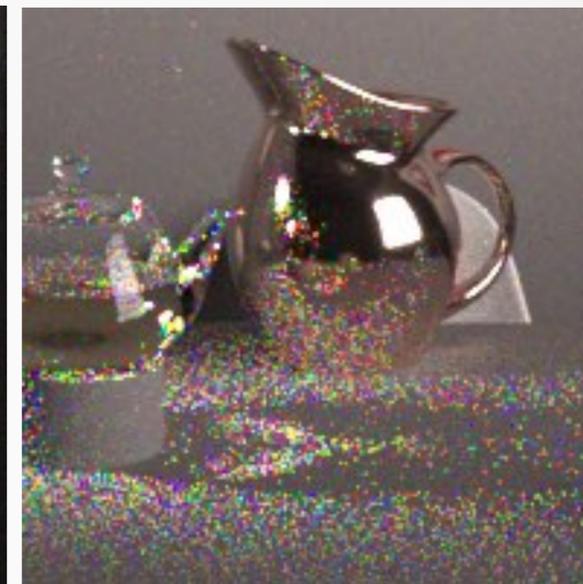


# Dining Room - 30min

guided path tracing + DBOR

RMSE 0.0435

RMSE 0.0345



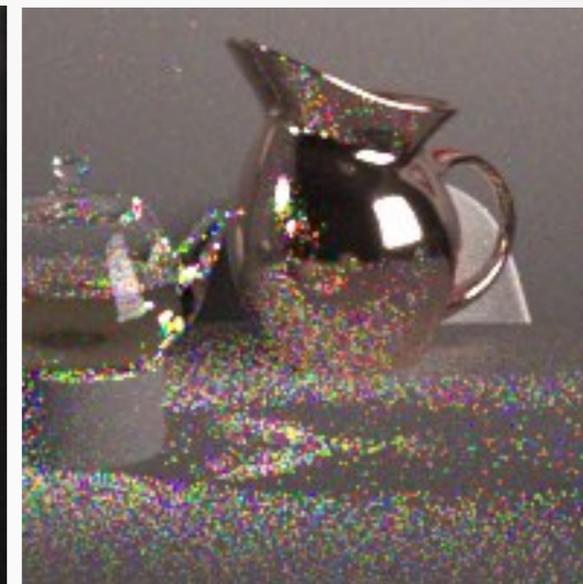
RMSE 0.0231

# Dining Room - 30min

path tracing + DBOR

RMSE 0.0435

RMSE 0.0345



RMSE 0.1170

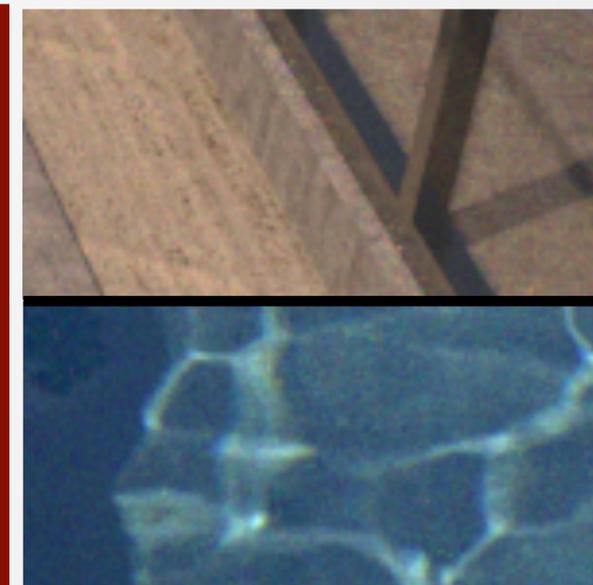
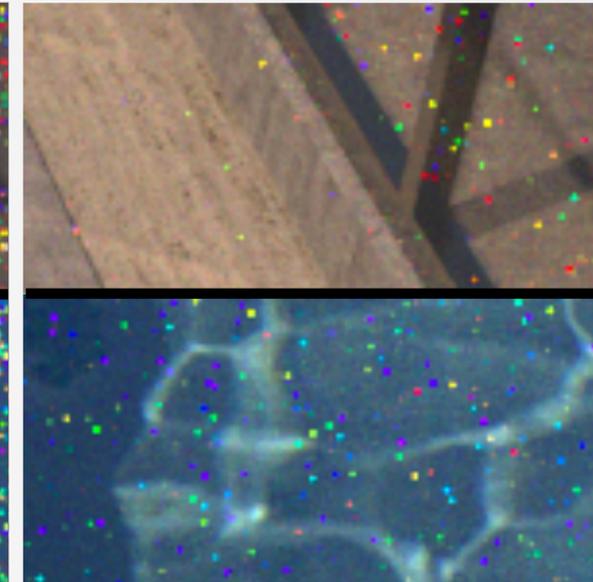
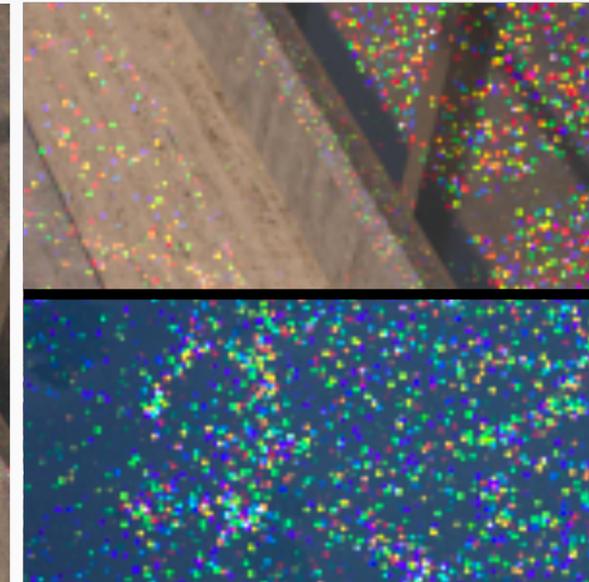
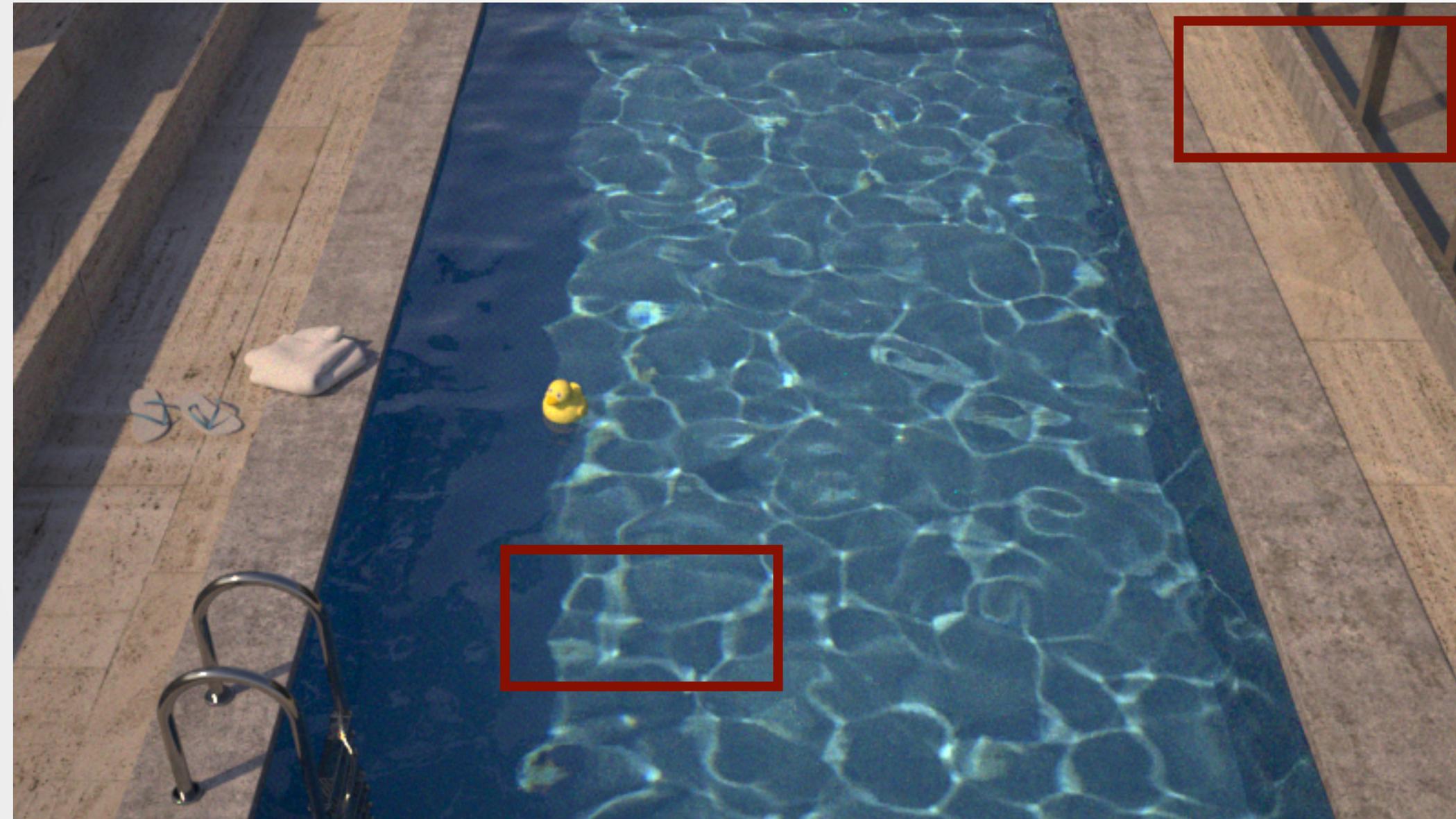
RMSE 0.0231

# Pool - 30min

guided path tracing + DBOR

RMSE 0.2550

RMSE 0.3162



RMSE 0.1238

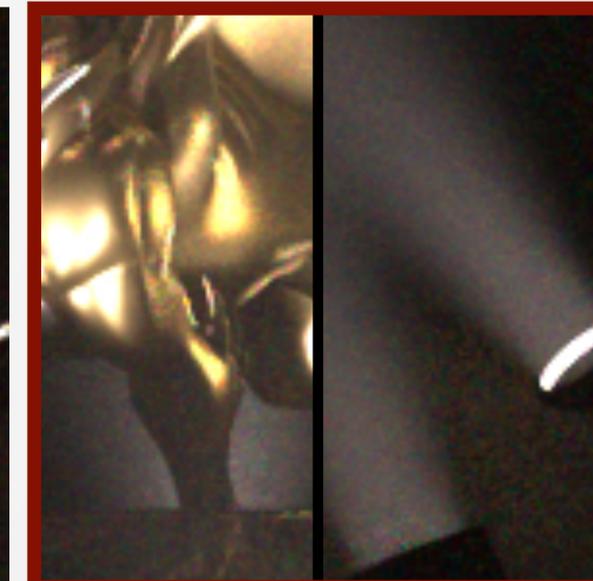
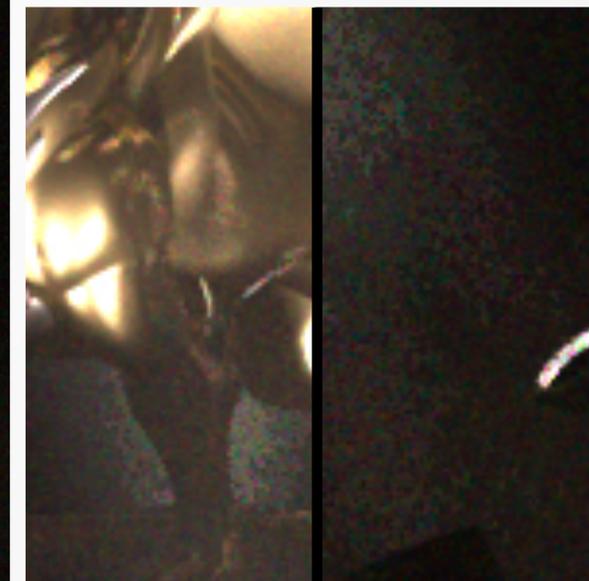
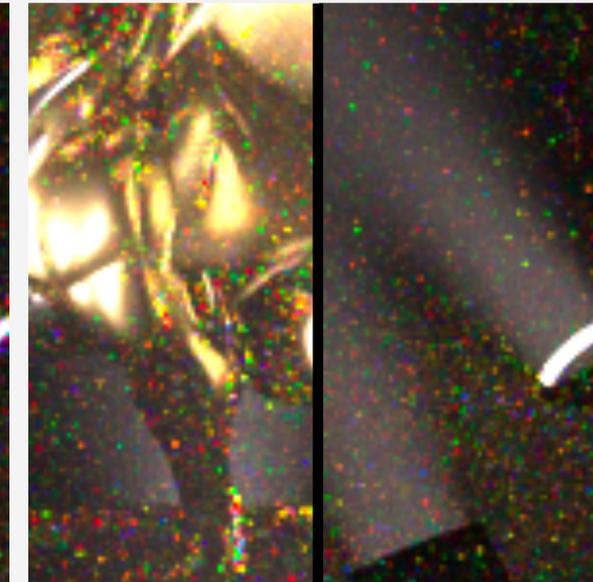
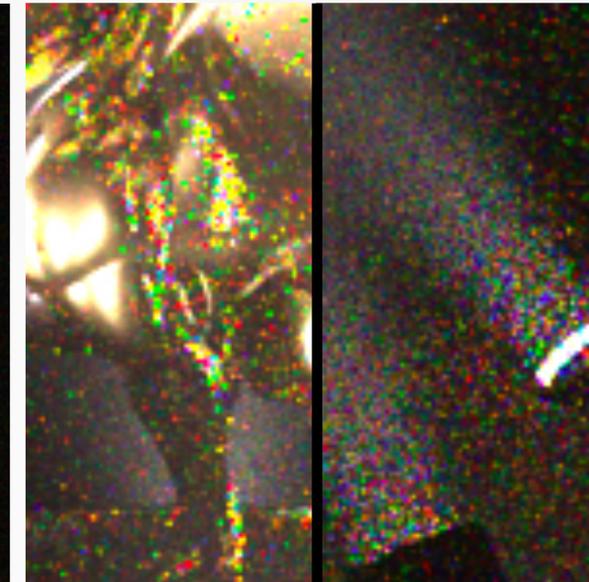
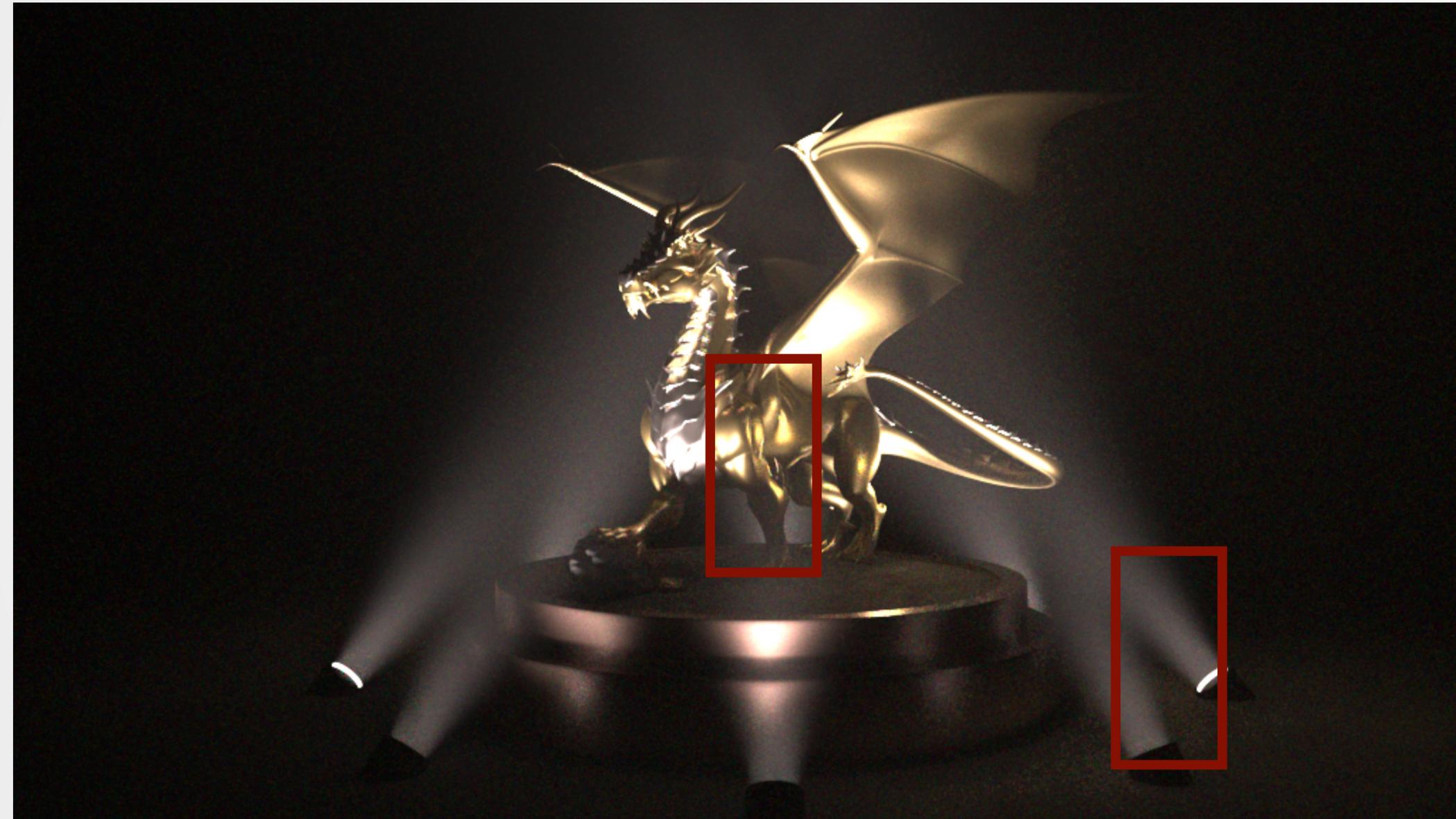
RMSE 0.0499

# Dragon - 10h

guided path tracing + DBOR

RMSE 0.5012

RMSE 0.2121



RMSE 0.6143

RMSE 0.2198

# Dining Room - 30min

reference



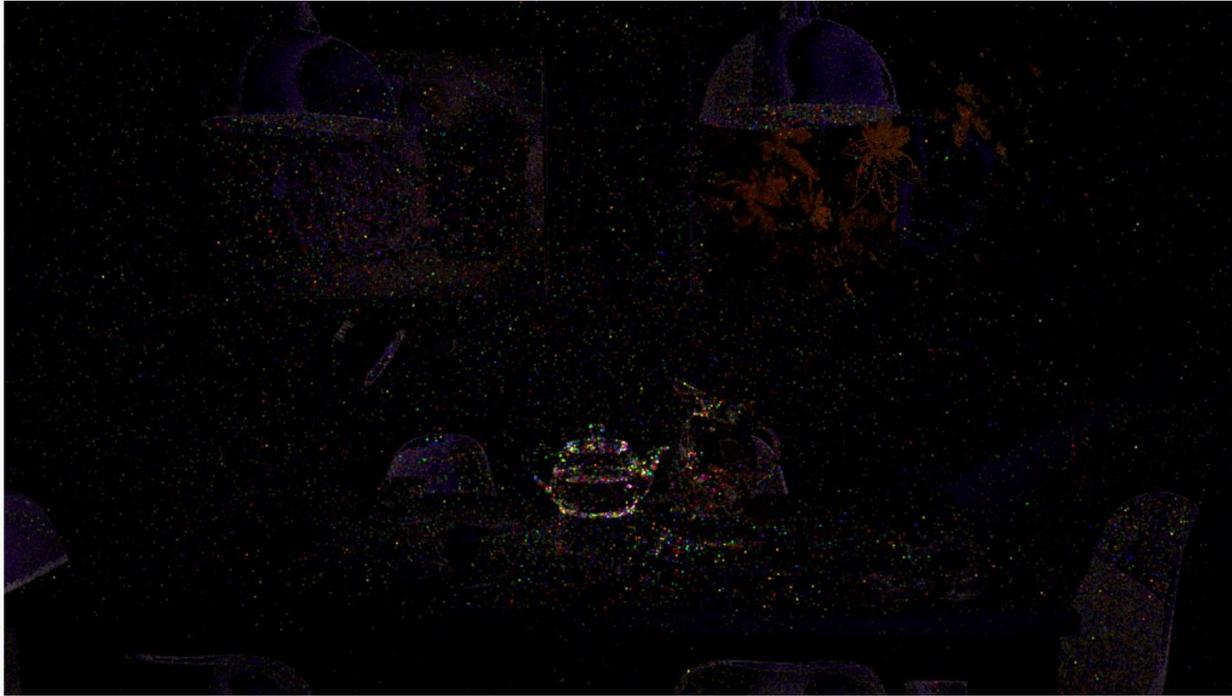
ours



path tracing



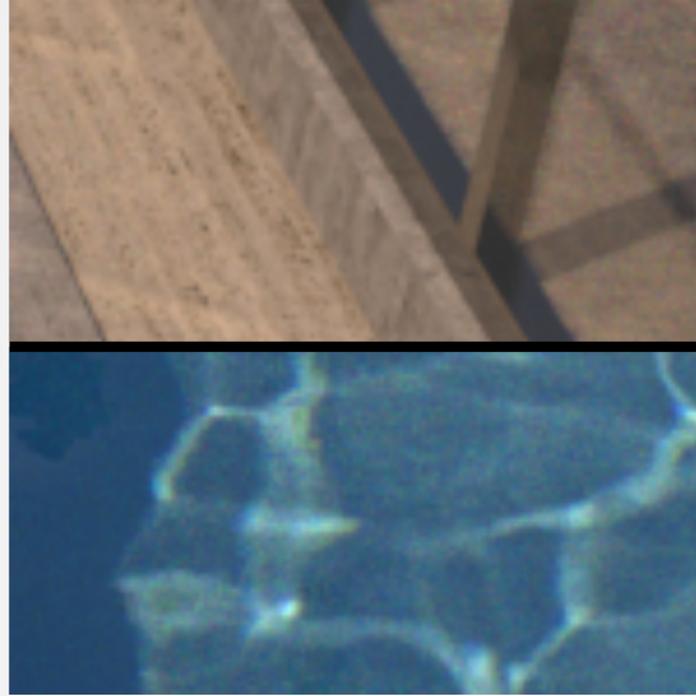
guided path tracing



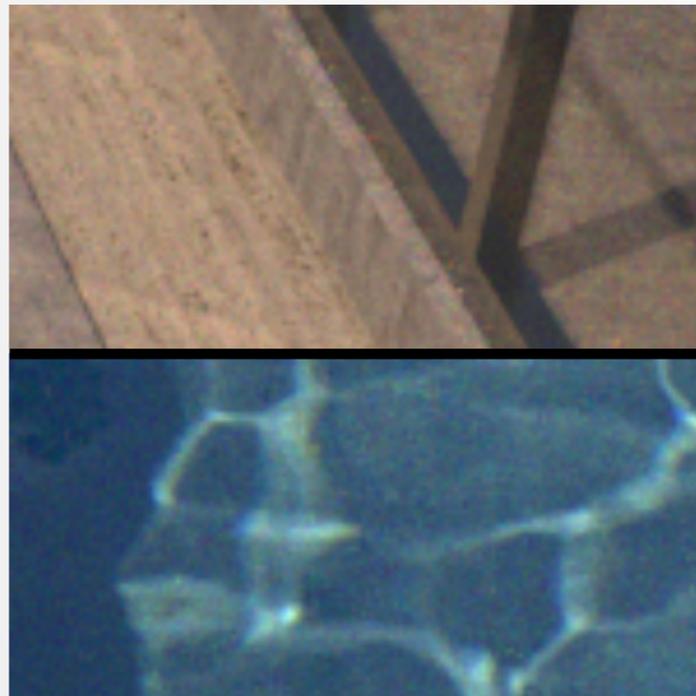
removed by DBOR

# Pool - 30min

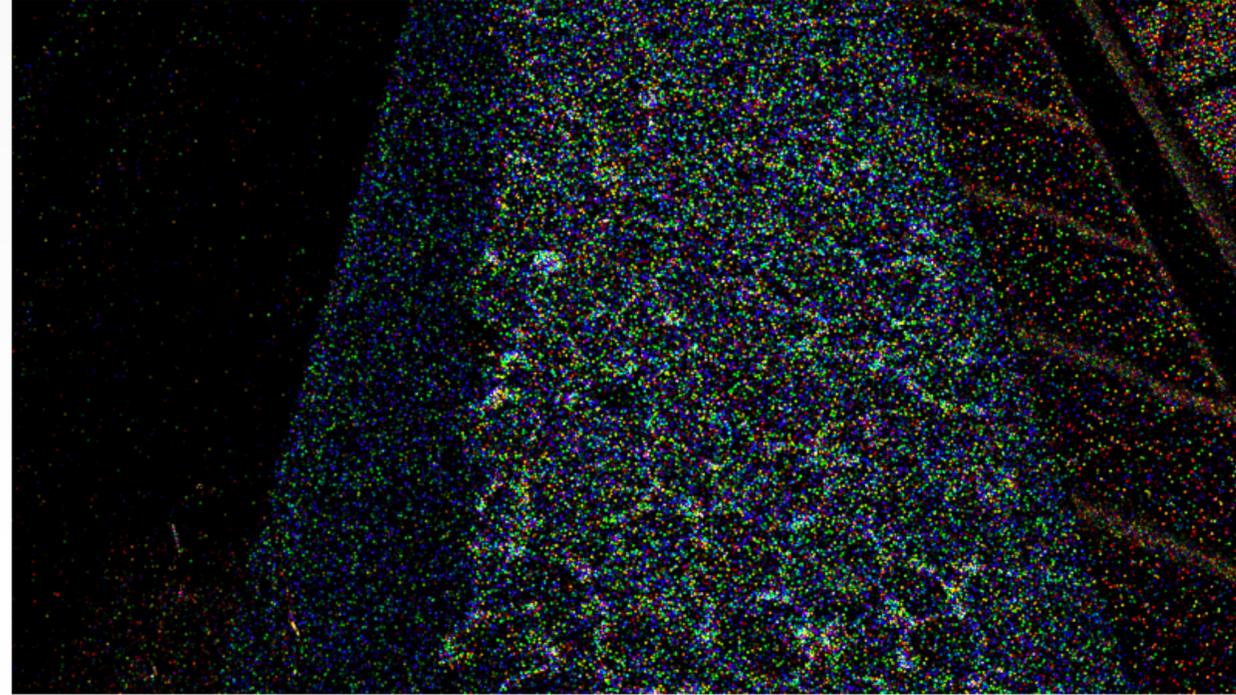
reference



ours

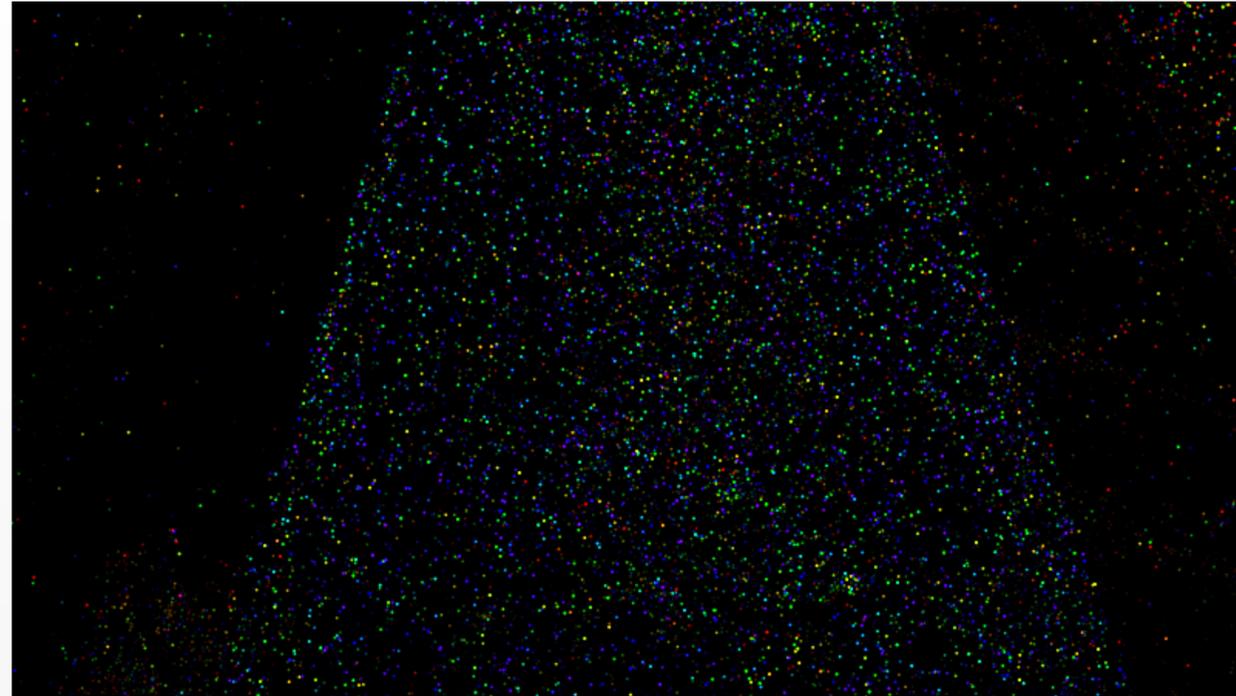


removed by DBOR



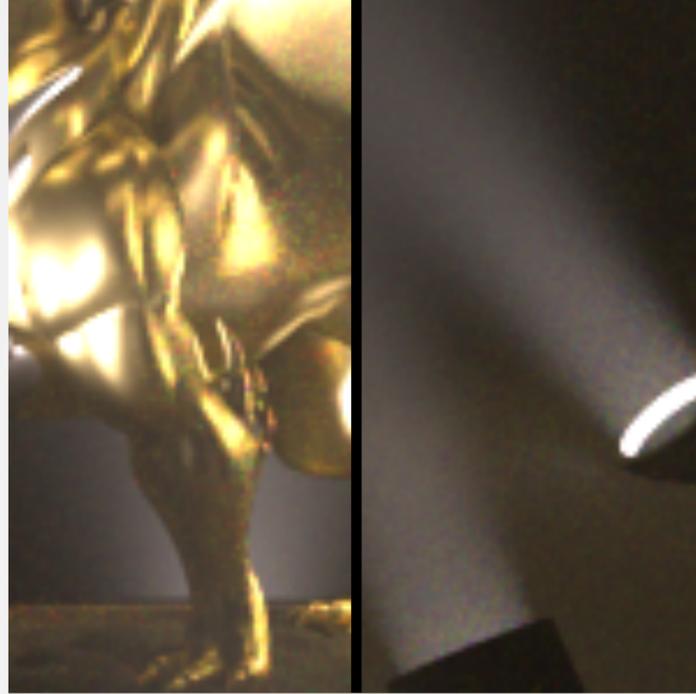
path tracing

guided path tracing

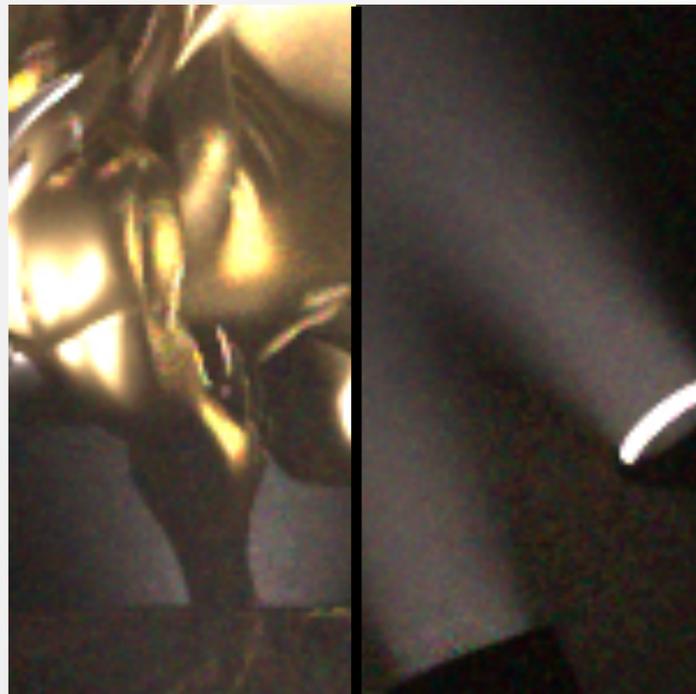


# Dragon - 10h

reference

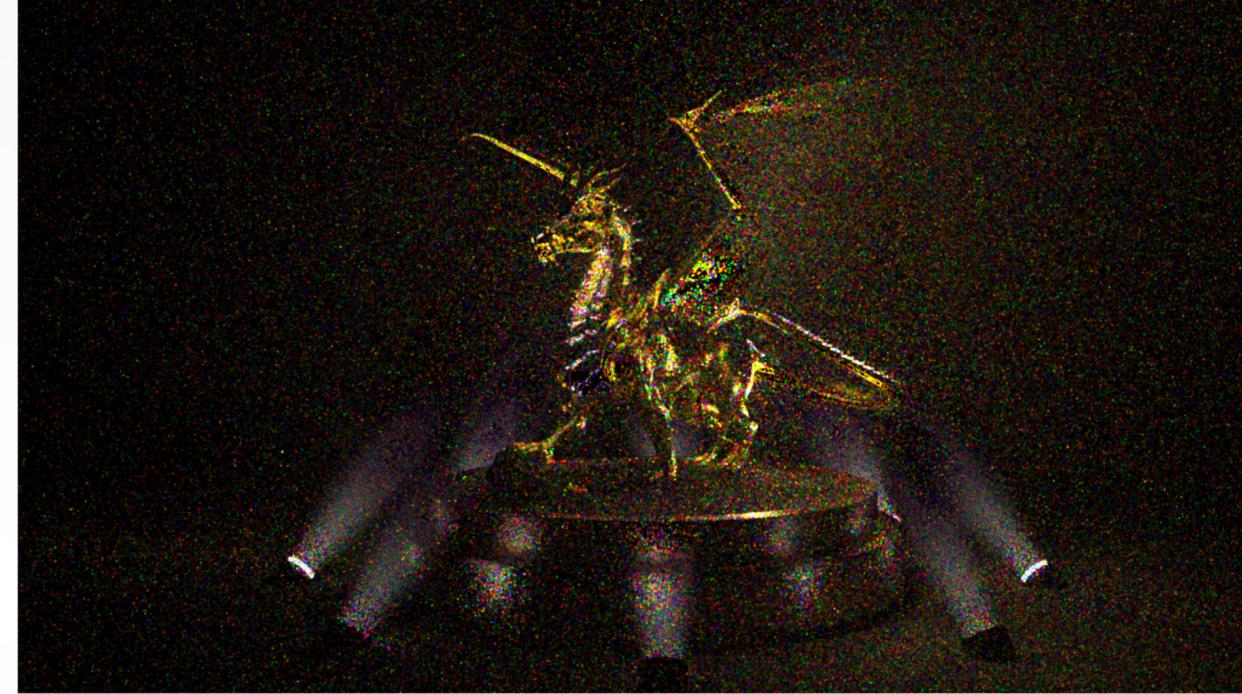


ours



removed by DBOR

path tracing

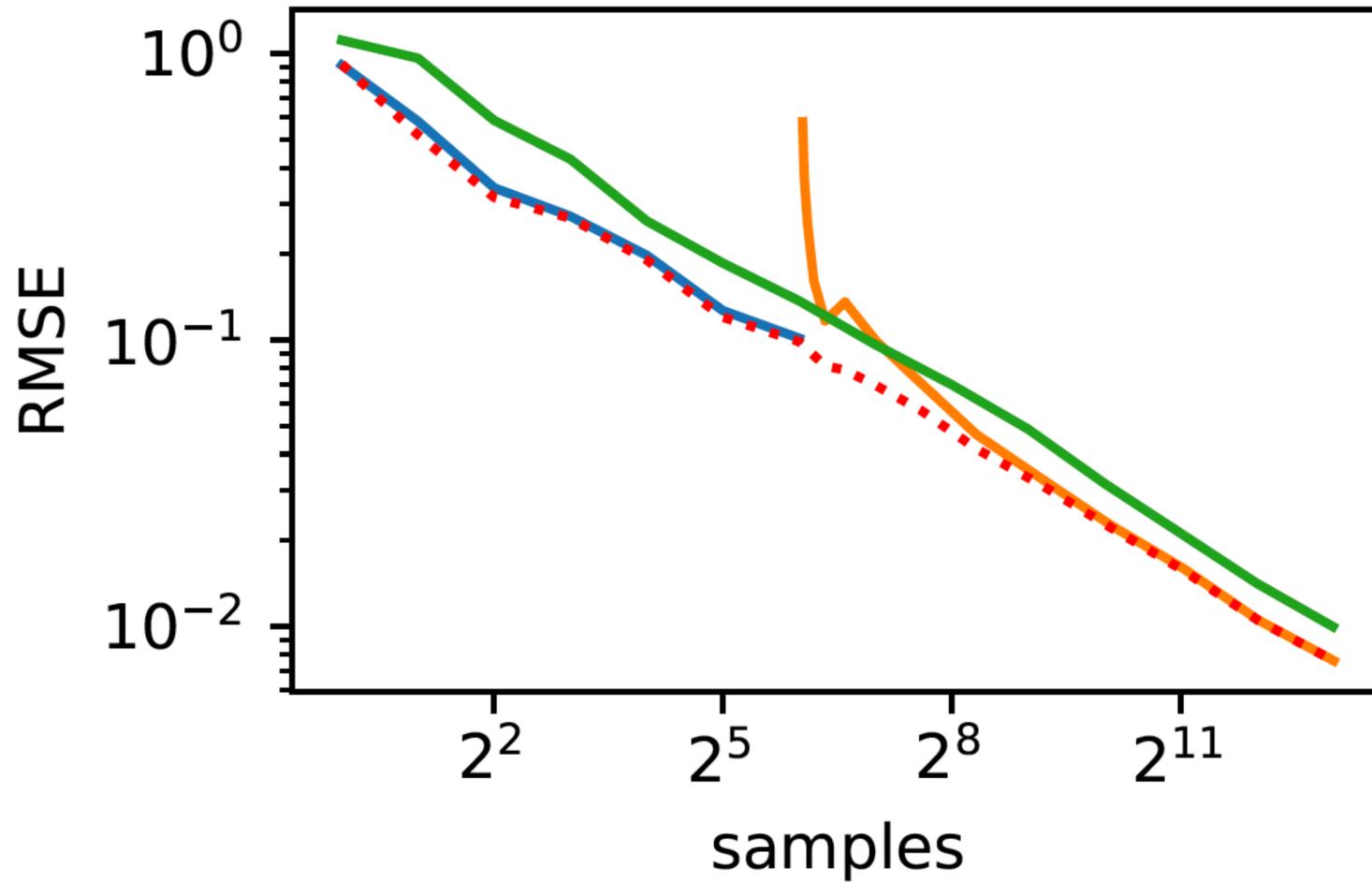


guided path tracing

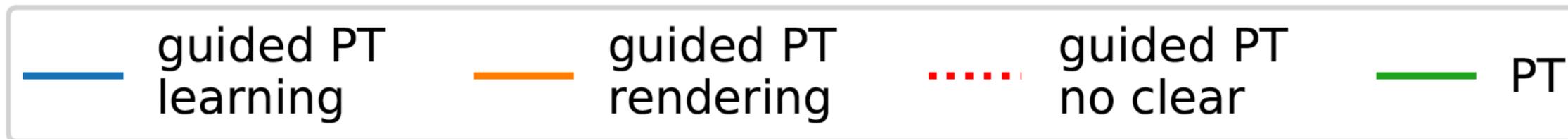
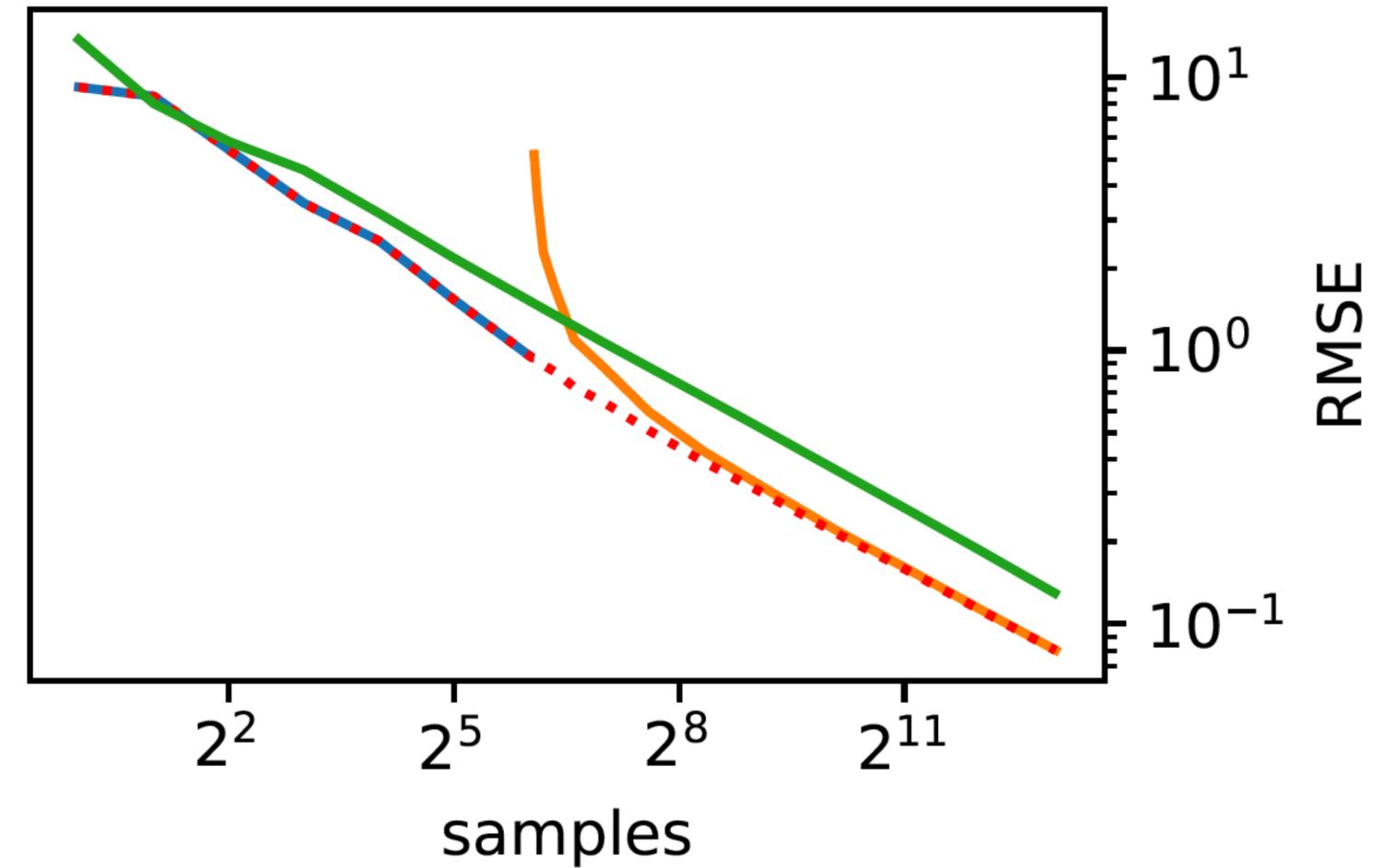


# Convergence

## Dining Room

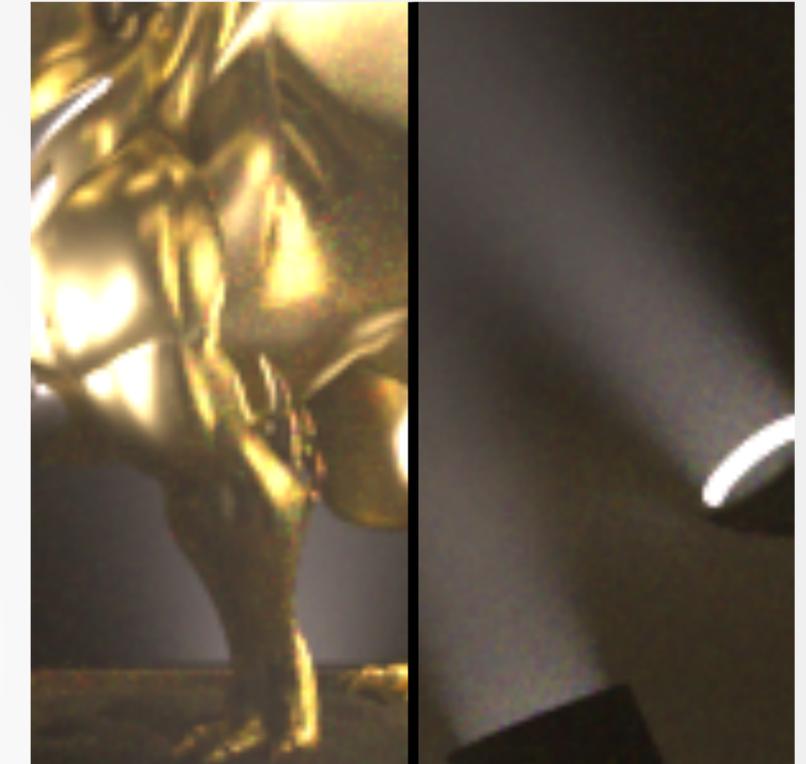
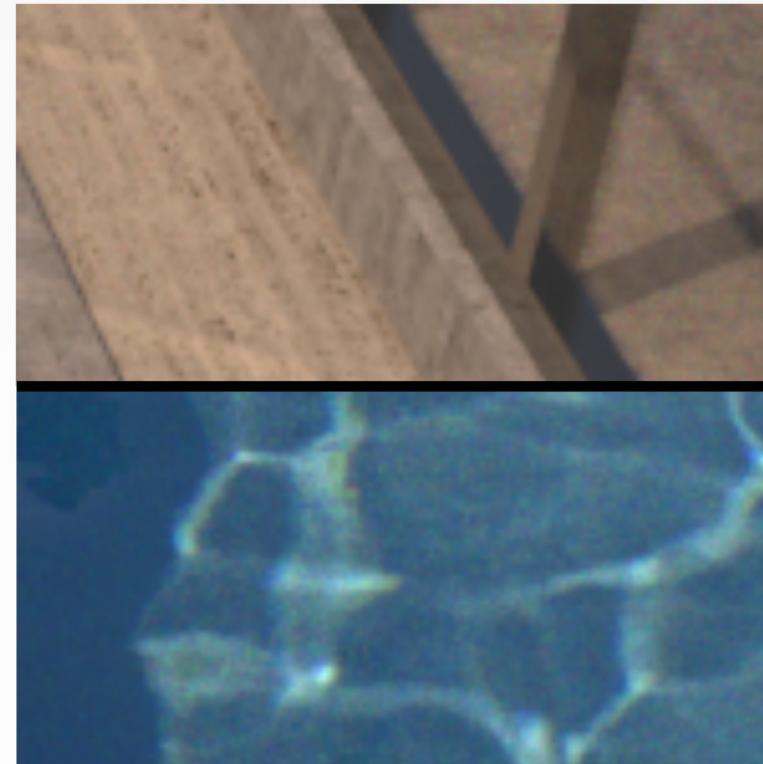


## Swimming Pool

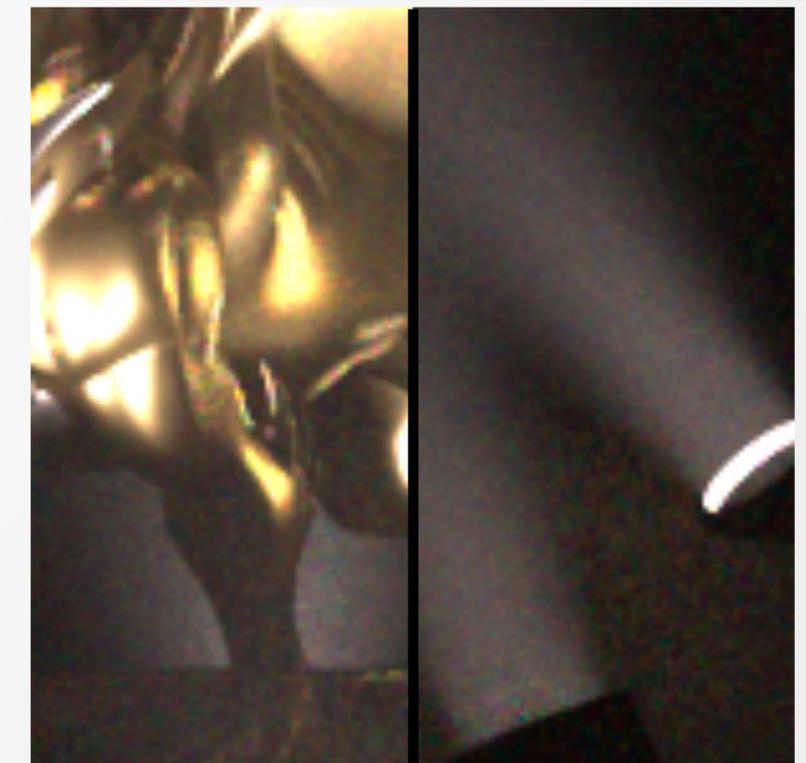
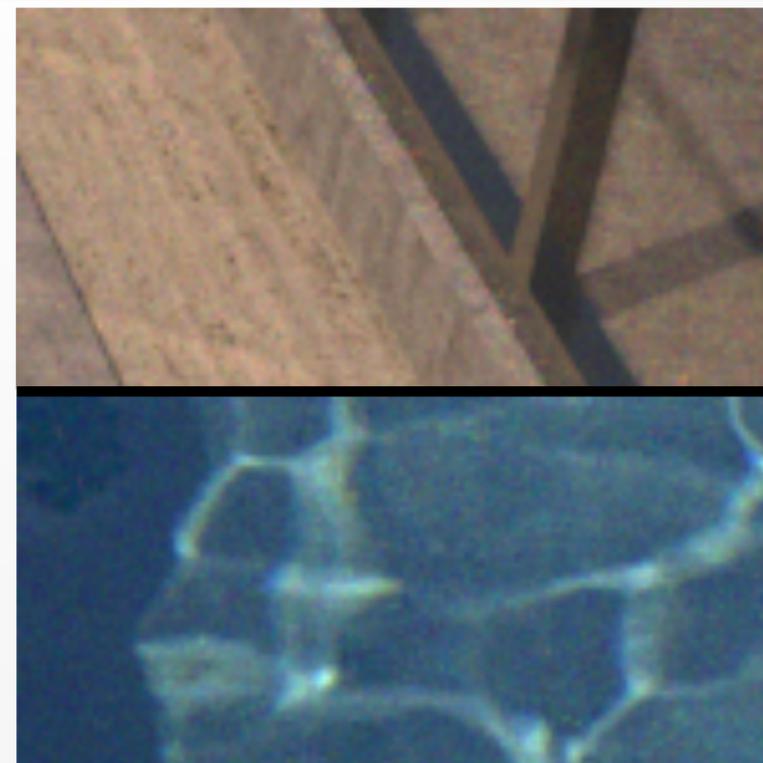


# Difference

**Reference**

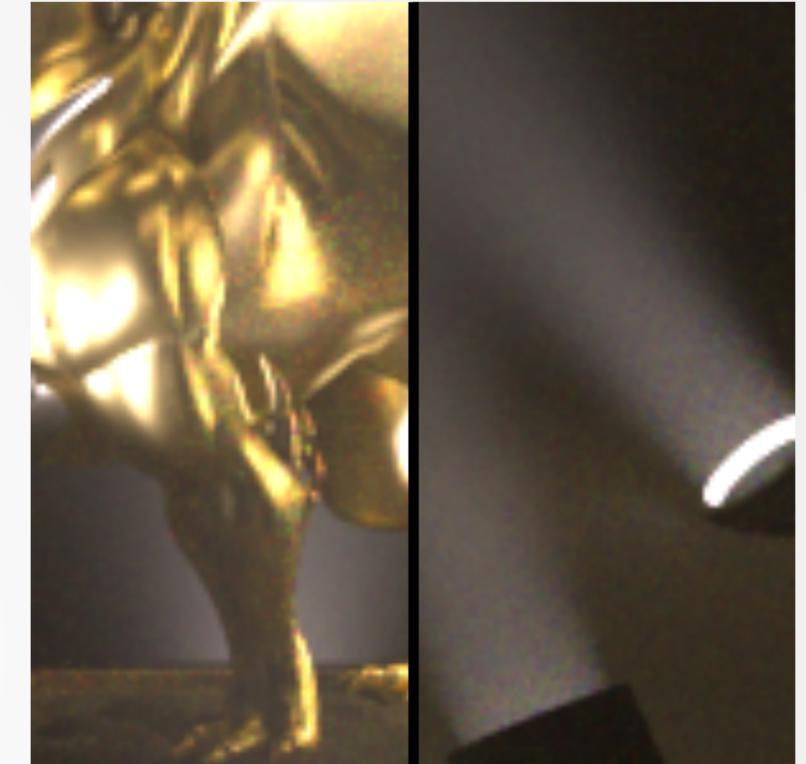
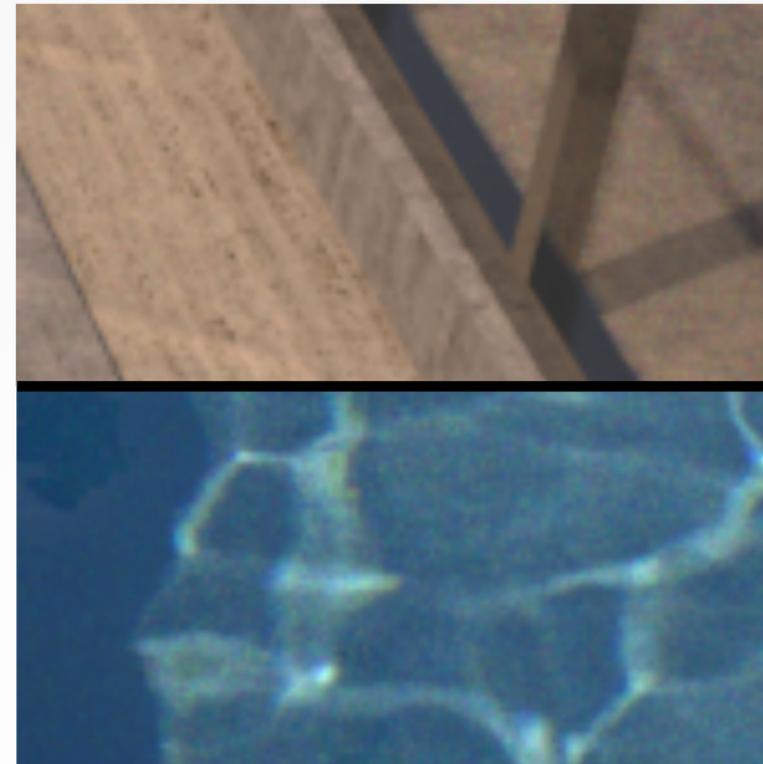


**Guided path  
tracing  
+  
DBOR**



# Difference

**Scene**



---

**Learning time**

**3min**

**3min**

**3min**

---

**Number of  
guide paths**

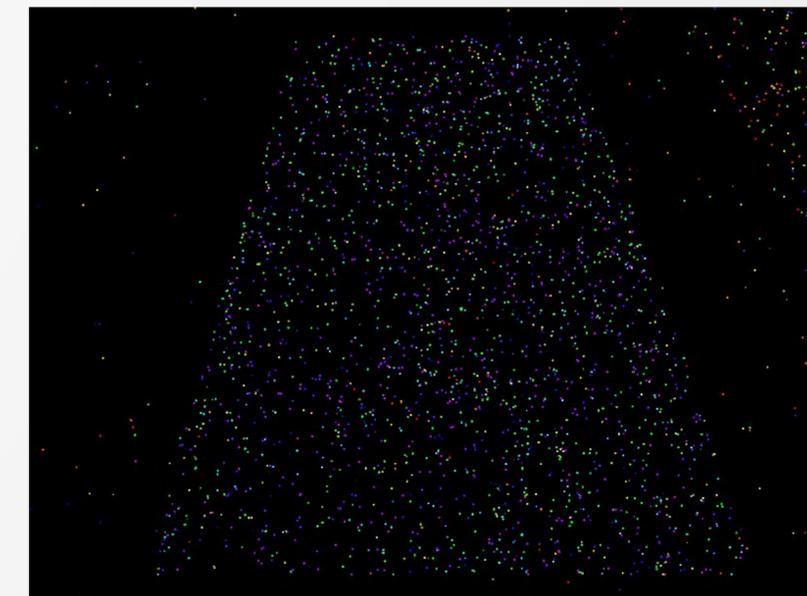
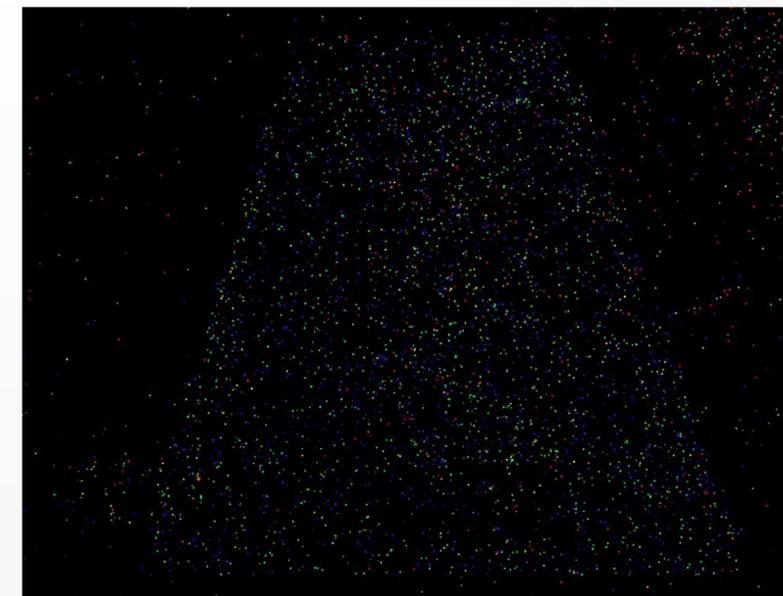
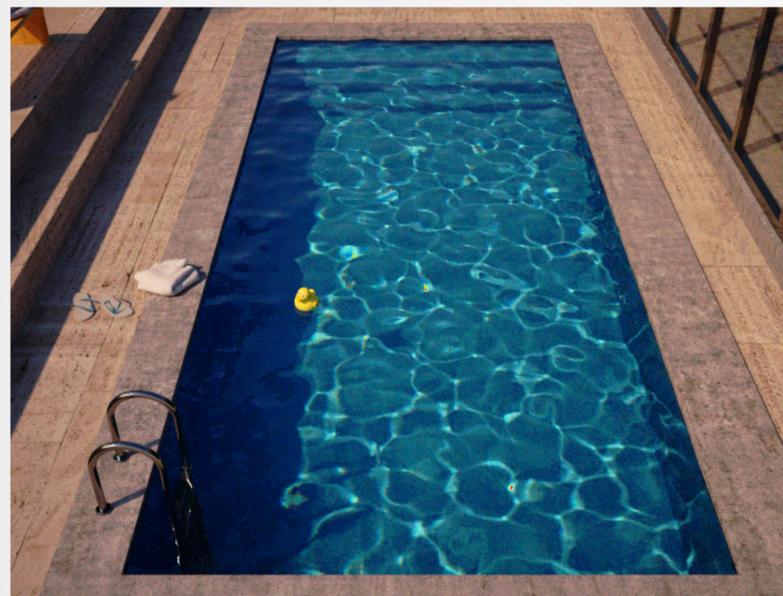
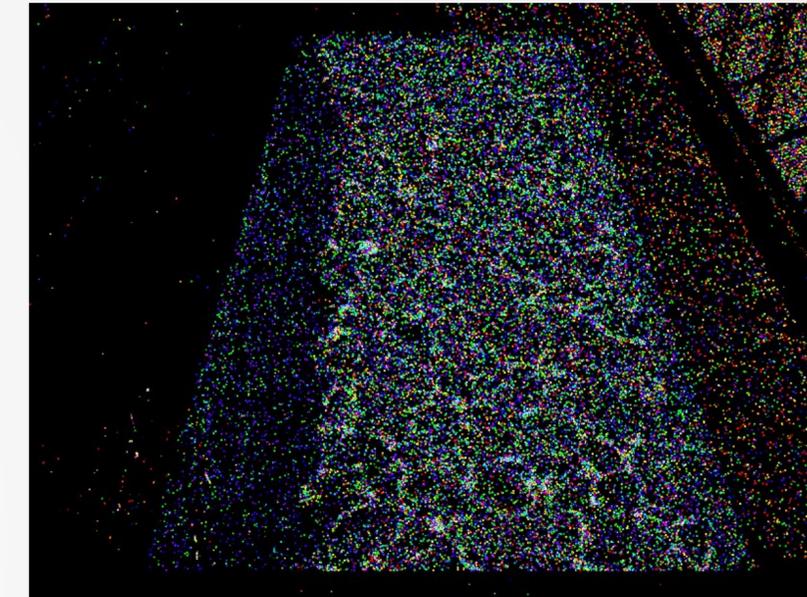
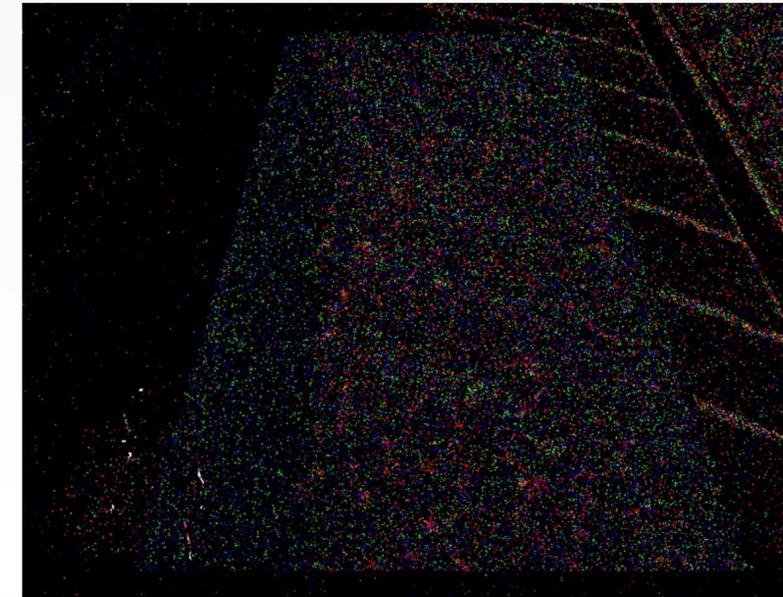
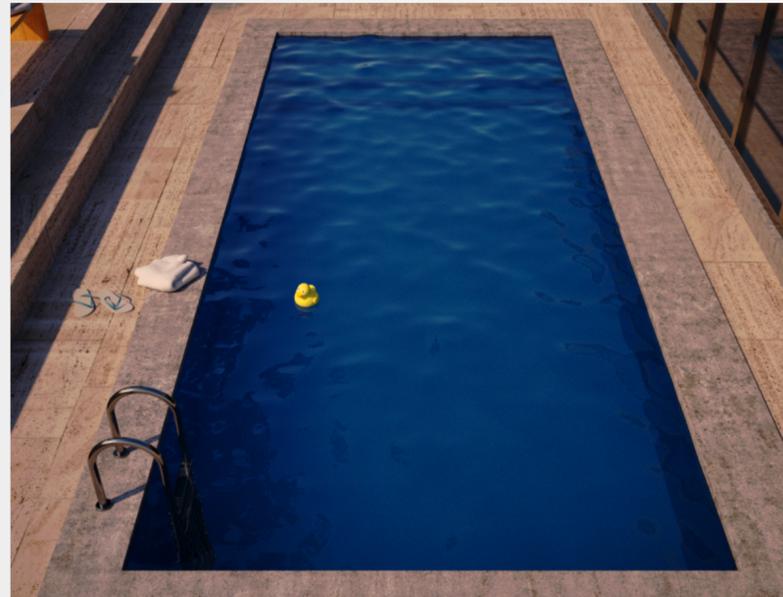
**33k**

**104k ( $\approx$ 300MB)**

**69k**

# Pool DBOR Cascade

path tracing



guided path tracing

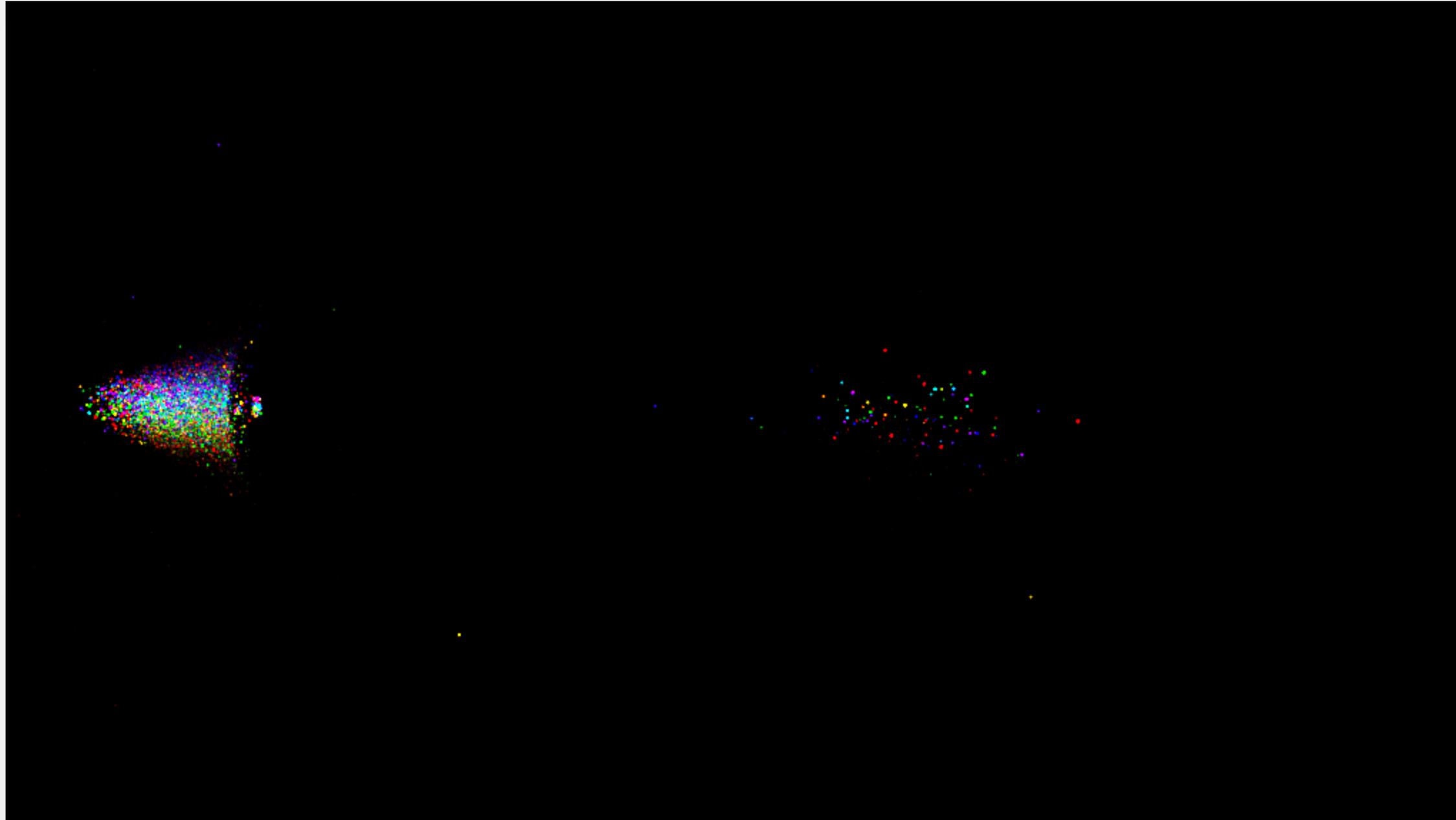
# Guiding Behaviour

Guided path tracing - iteration 1



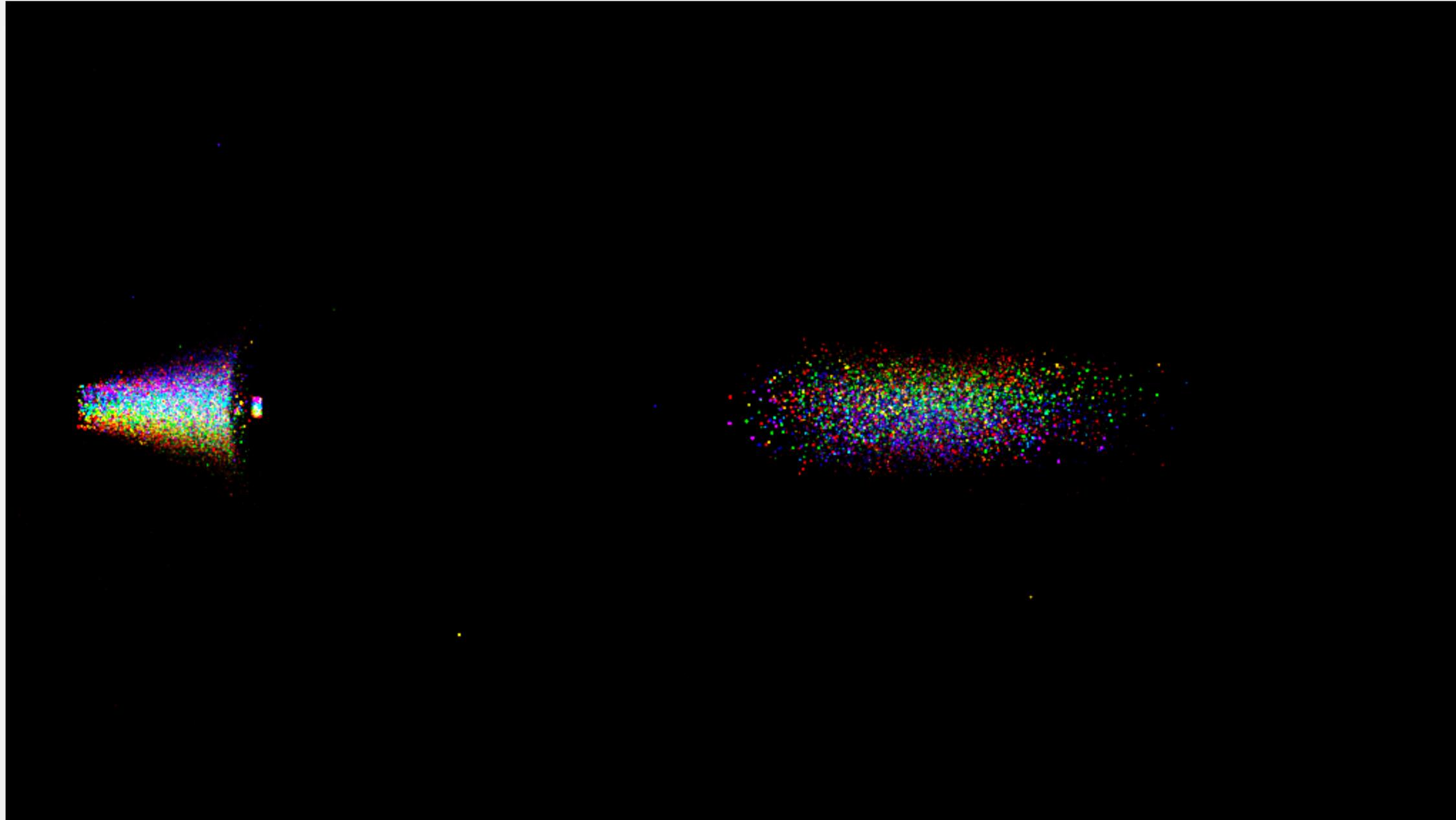
# Guiding Behaviour

Guided path tracing - iteration 2



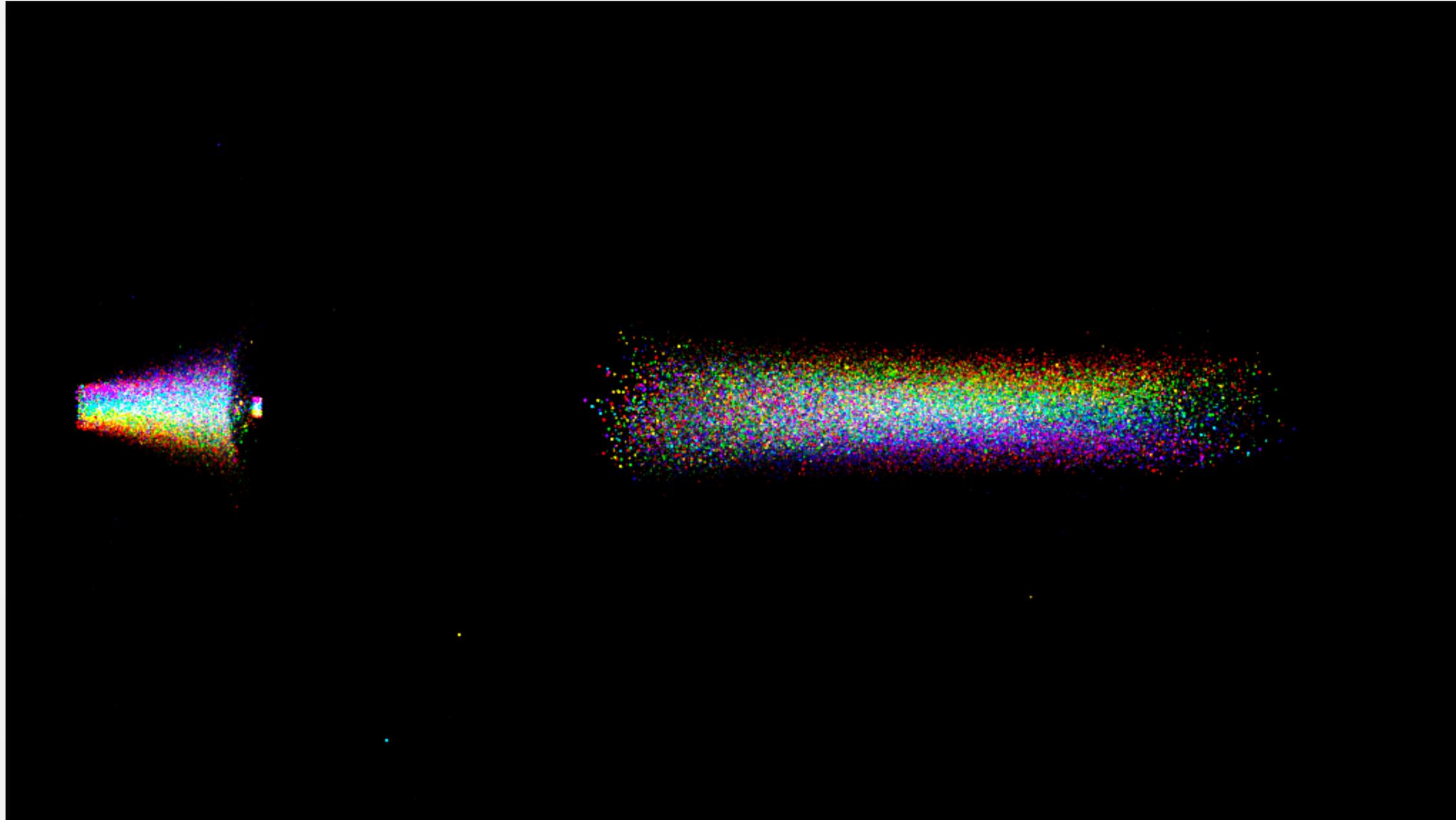
# Guiding Behaviour

Guided path tracing - iteration 3



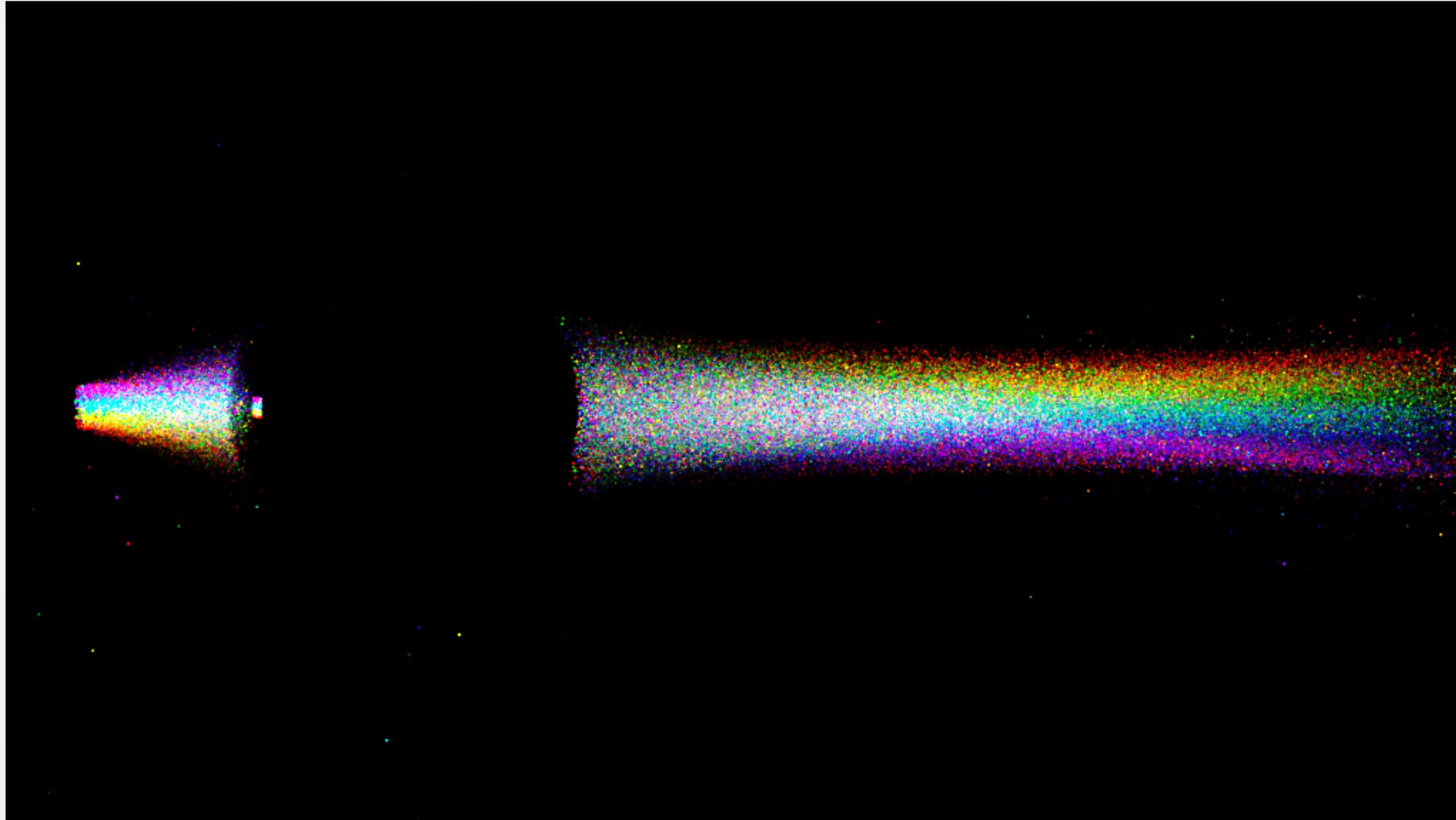
# Guiding Behaviour

Guided path tracing - iteration 4



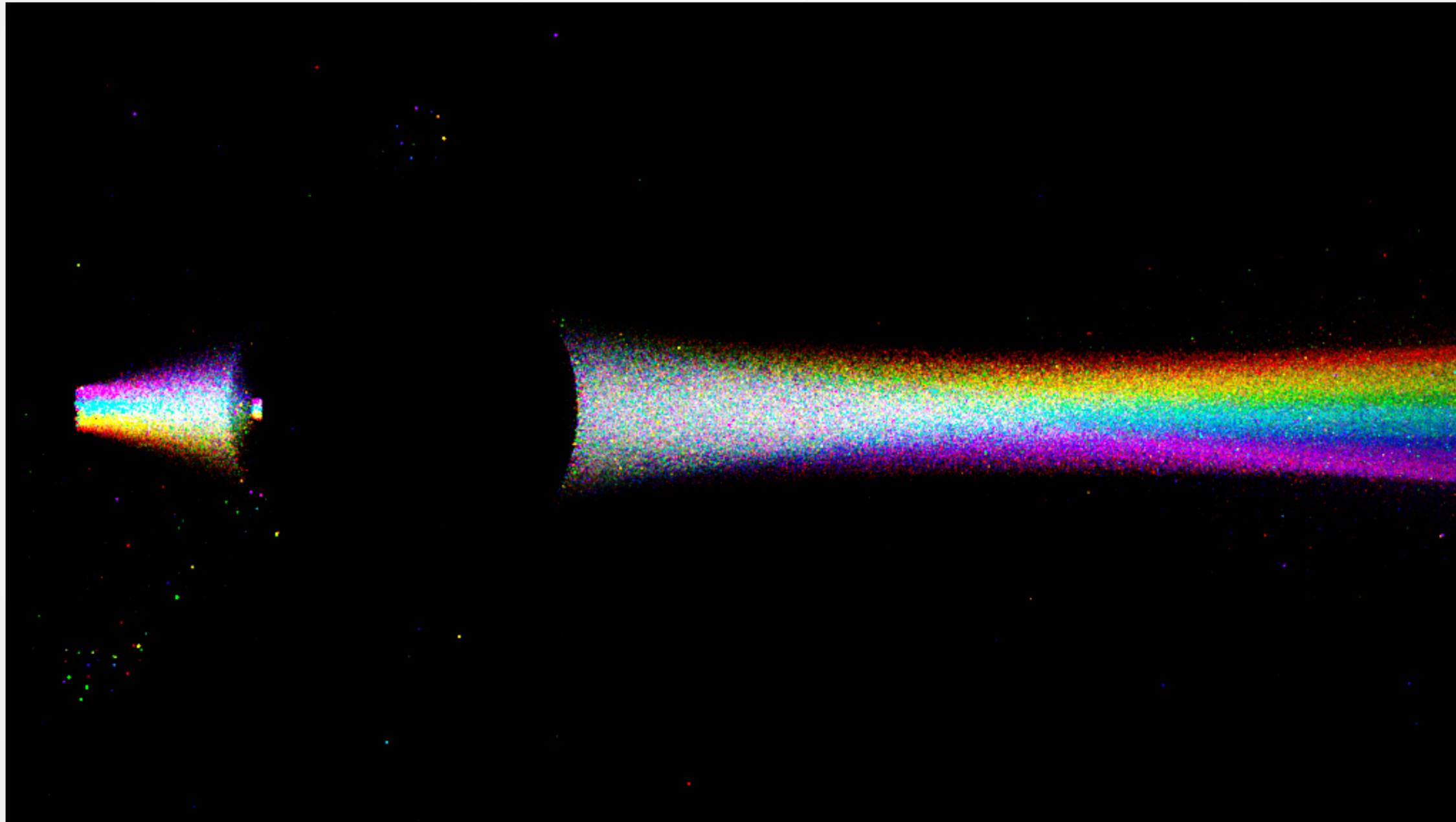
# Guiding Behaviour

Guided path tracing - iteration 8



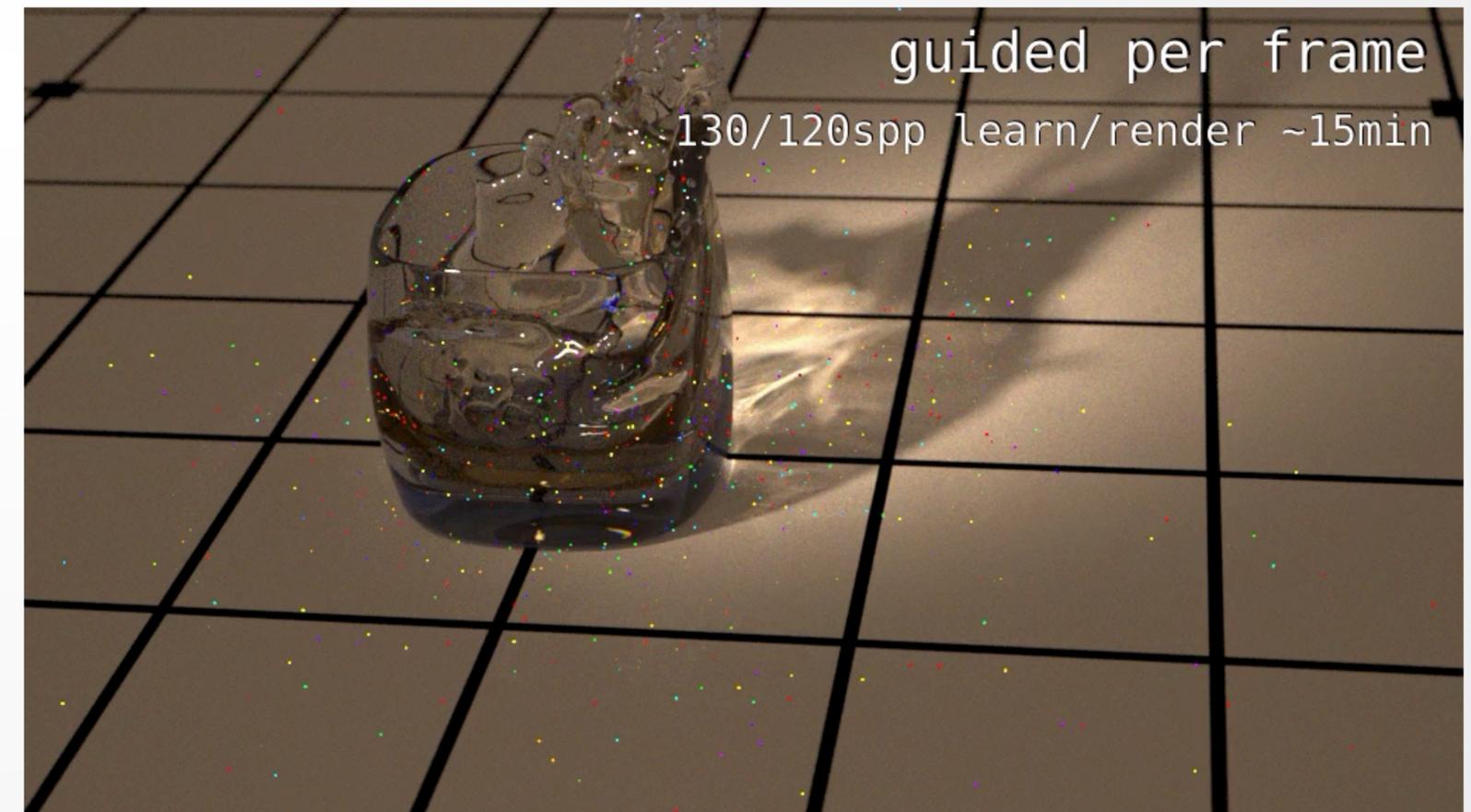
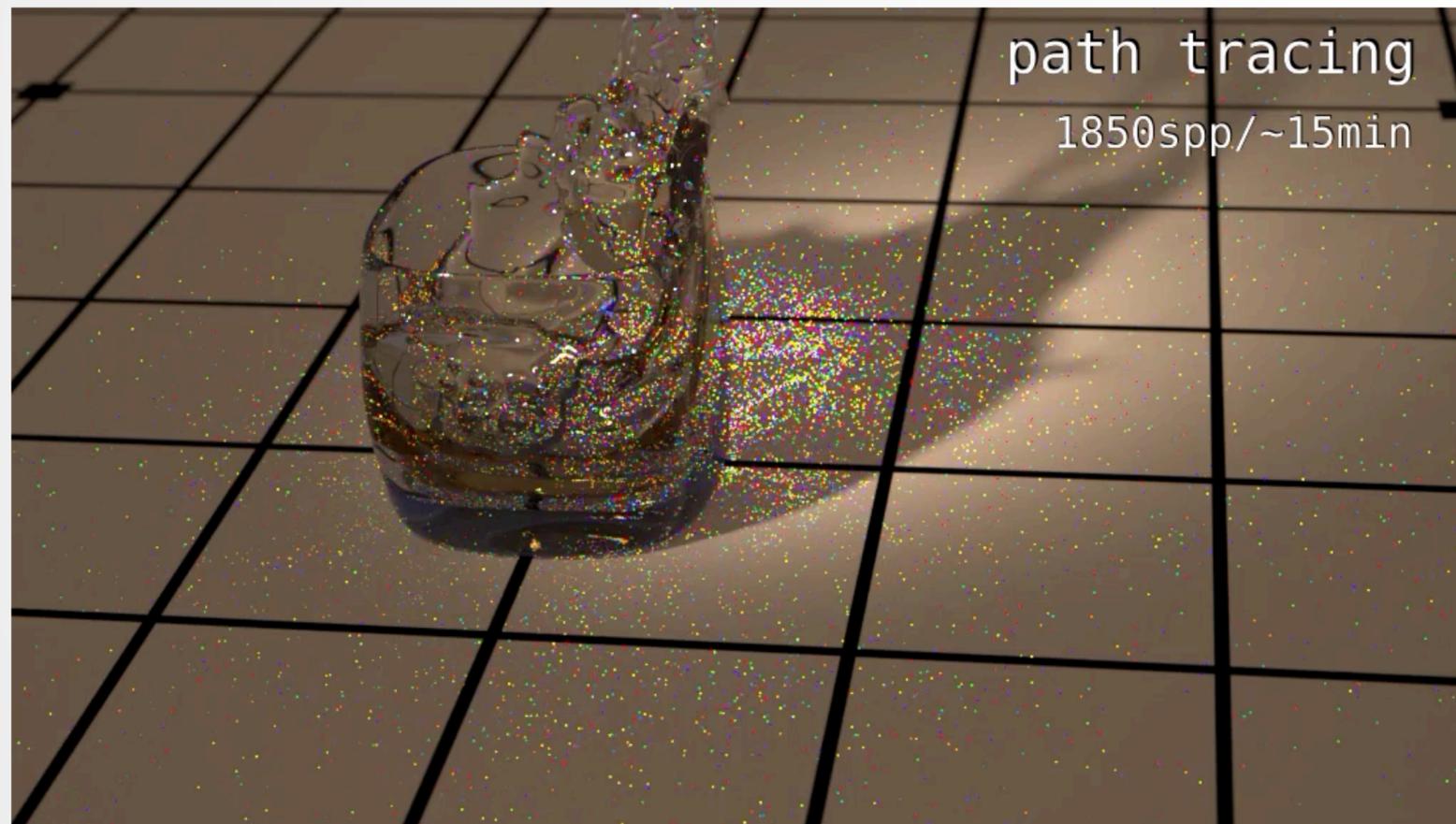
# Guiding Behaviour

Guided path tracing - iteration 16



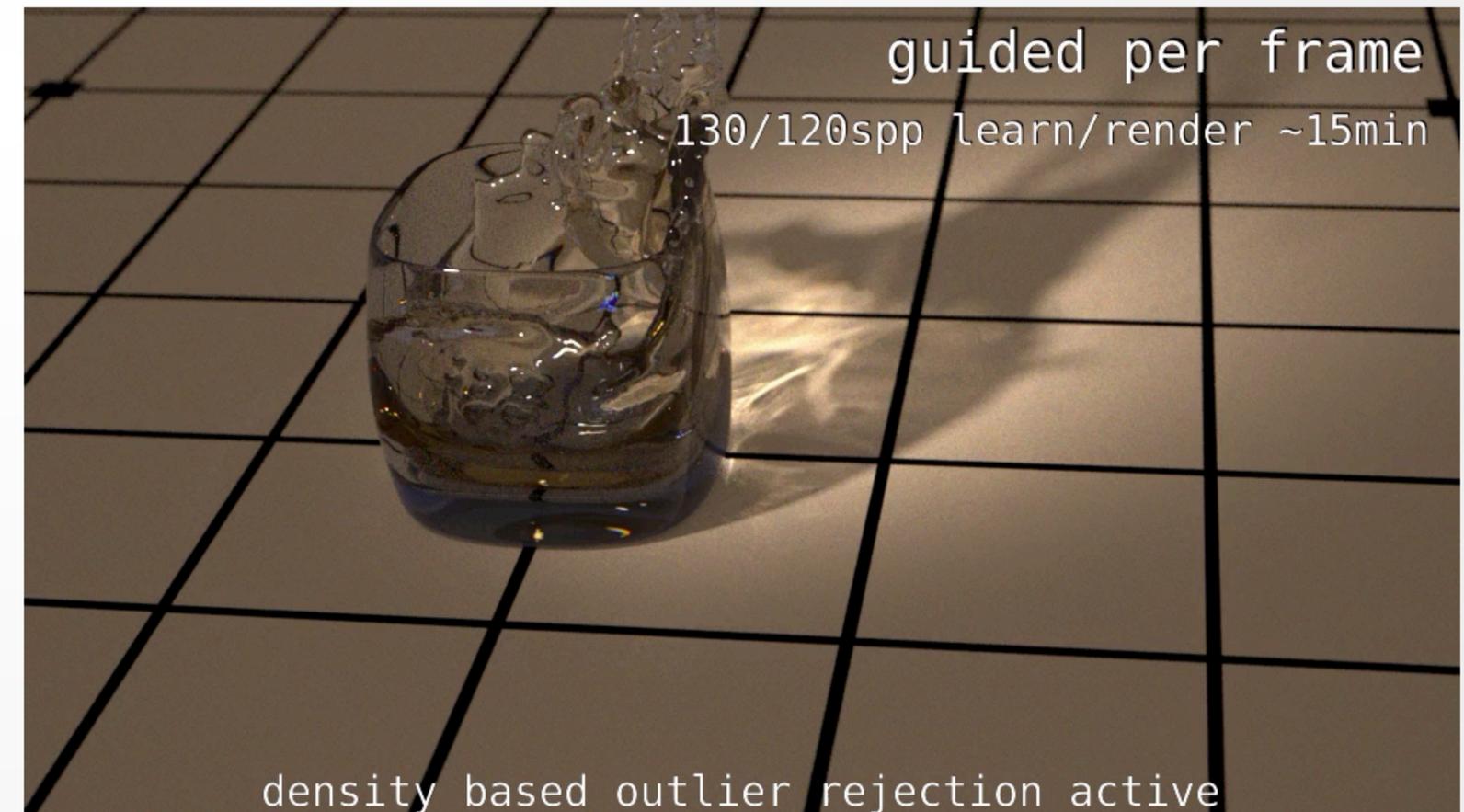
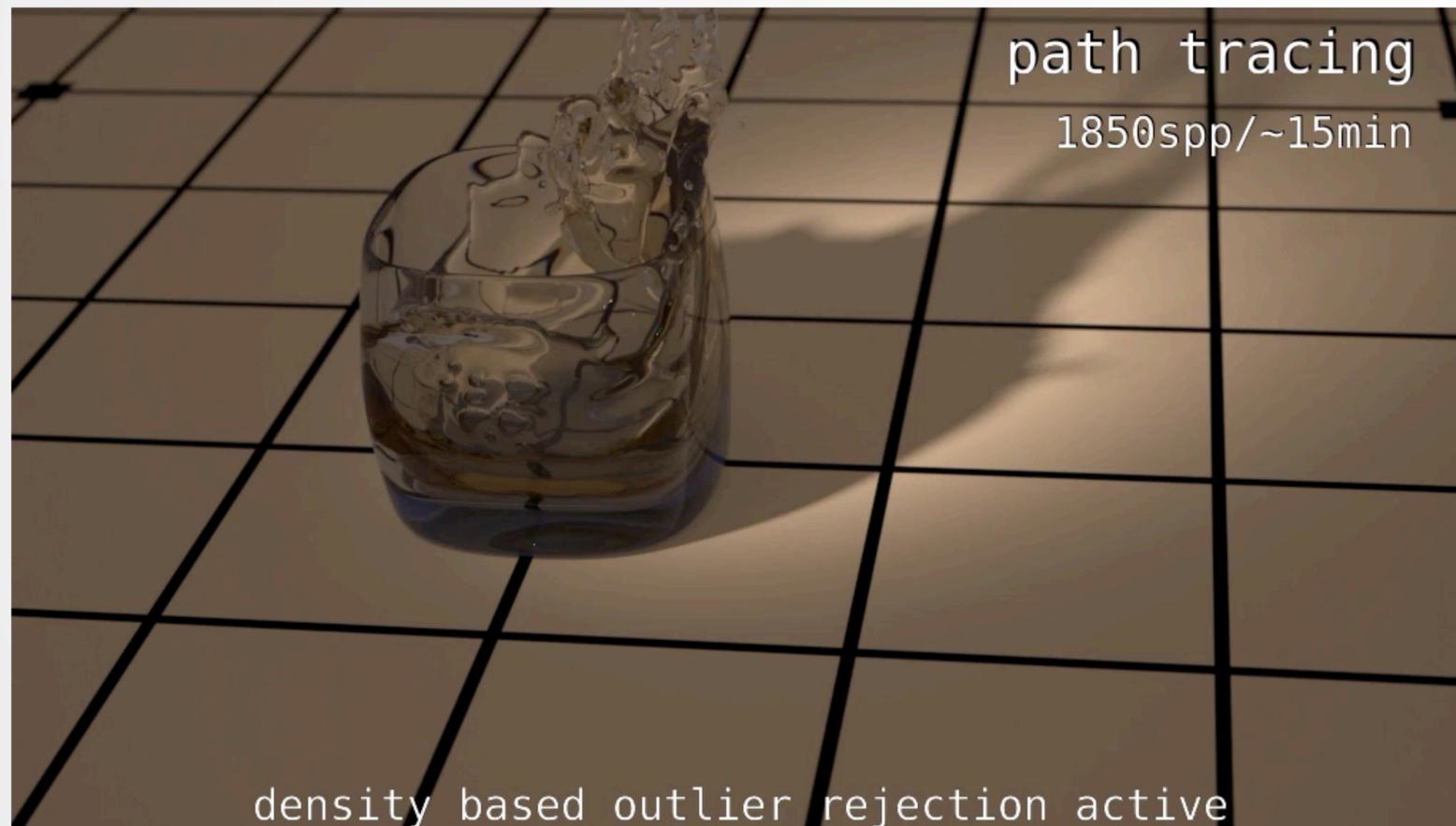
# Limitations & Future Work

- Temporal stability is challenging



# Limitations & Future Work

- Temporal stability is challenging



# Guide path sampling

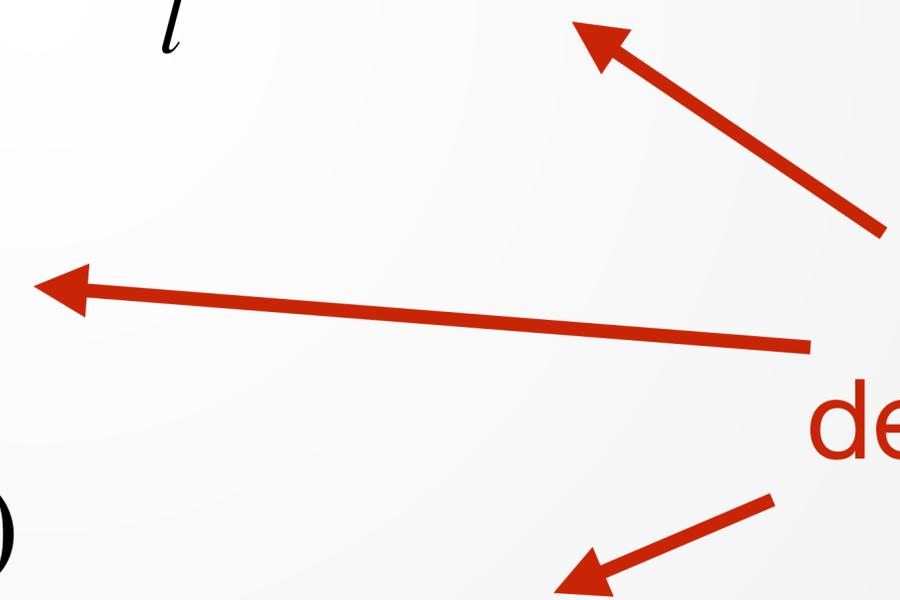
- Pick guide path  $X_j$  randomly using weights  $w_j$

- Then in iteration  $k$ : 
$$p_g^k(X) = \sum_l w_j^k p_g^k(X | X_l)$$

- Choosing 
$$w_j^k = \frac{C^k(X_j)}{\sum_l C^k(X_l)}$$

with 
$$C^k(X_i) = \frac{f(X_i)}{\alpha p_u(X_i) + (1 - \alpha) p_g^k(X_i)}$$

circular  
dependency



# Guide path sampling

- Pick guide path  $X_j$  randomly using weights  $w_j$

- Then in iteration  $k$ : 
$$p_g^k(X) = \sum_l w_j^k p_g^k(X | X_l)$$

- Therefore 
$$w_j^k = \frac{C^{k-1}(X_j)}{\sum_l C^{k-1}(X_l)}$$

$$\text{with } C^k(X_i) = \frac{f(X_i)}{\alpha p_u(X_i) + (1 - \alpha) p_g^k(X_i)}$$

oscillation

# Guide path sampling

- Pick guide path  $X_j$  randomly using weights  $w_j$

- Then in iteration  $k$ : 
$$p_g^k(X) = \sum_l w_j^k p_g^k(X | X_l)$$

- Therefore 
$$w_j^k = t \cdot \frac{C^{k-1}(X_j)}{\sum_l C^{k-1}(X_l)} + (1 - t) \cdot w_j^{k-1}$$

$$\text{with } C^k(X_i) = \frac{f(X_i)}{\alpha p_u(X_i) + (1 - \alpha) p_g^k(X_i)}$$