Computer graphics III – Photon mapping

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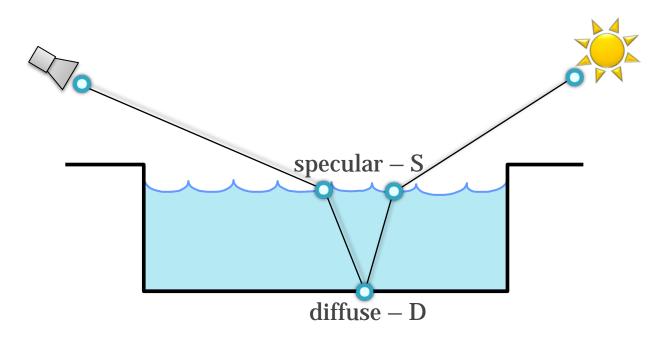


Reference solution

Bidirectional path tracing

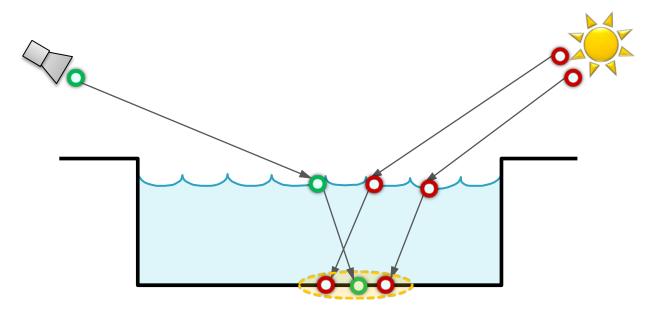
Insufficient path sampling techniques

Some paths sampled with zero (or very small) probability

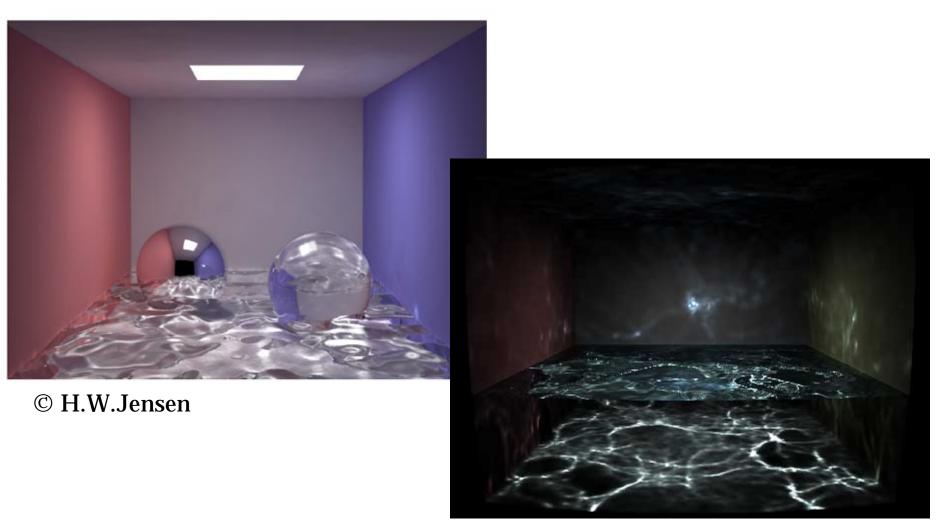


Photon mapping (Density estimation)

- 1. Many fwd walks + store particles ("photon map")
- 2. Radiance estimate: (Kernel) **density estimation**



Photon mapping – SDS paths



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Photon mapping overview

- Paths are followed both from the light sources and from the camera
- Similar to bidirectional path tracing
 - But the sub-path connection strategy significantly differs
- Reuse of light sub-paths for all pixels
 - Photon map = "light sub-path cache"
 - **Essential for good performance**
- For the same quality often faster than pure MC techniques
- Biased!
 - But can be made consistent (i.e. converges as the photon count increases, cf. progressive photon mapping)

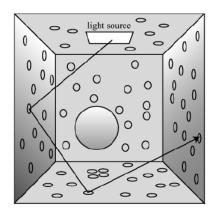
Calculation steps

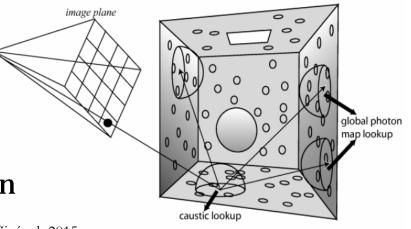
1. Photon tracing

- "Photons" emitted from light sources,
- traced through the scene (a la light tracing),
- and stored in a photon map

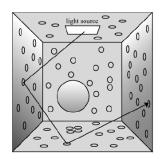
2. Rendering with photon maps

- Similar to distributed path tracing
- Recursion replaced by a photon map lookup
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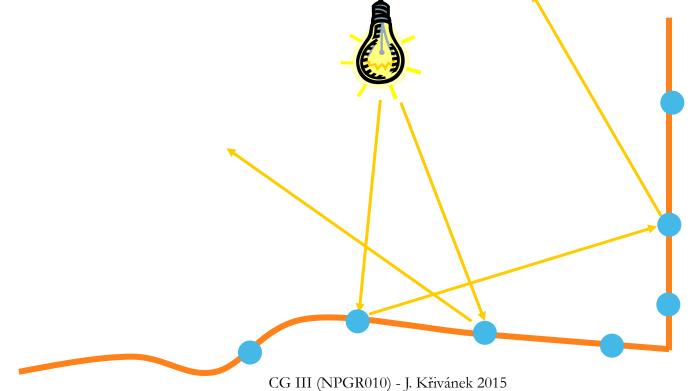




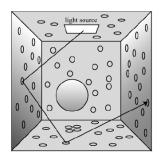
Phase 1: Photon tracing



- **1. Emission** of photons from light sources
- **2. Tracing** of photon paths
- Storage into the "photon map" (=photon list)



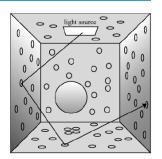
Photon emission



Goal

- All emitted photons carry the same (or similar) flux (so that the variance of photon map radiance estimates is low)
- **1. Emission** of a single photon (i.e. of a single sub-path)
 - 1. Choose the light source
 - Randomly with a probability proportional to its total flux
 - **2.** Choose the photon origin
 - The light position for point sources
 - Randomly chosen position for area sources
 - **3.** Choose the photon direction
 - Randomly according to the emission distribution of the source

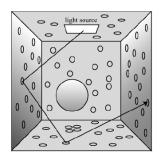
Photon emission



Flux of the emitted photon:

 $\Phi_{p,0} = \frac{1}{N} \frac{L_e(\mathbf{x}_0, \omega_0) |\cos \theta_0|}{P_l p(\mathbf{x}_0, \omega_0)}$ Total number of emitted photon paths
(Discrete) probability of choosing the light source *l*

Photon emission

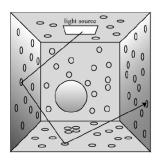


"Ideal" sampling

$$p(\mathbf{x},\omega) = \frac{L_{e}(\mathbf{x},\omega) \left|\cos\theta\right|}{\int\limits_{A_{light}} \int\limits_{H(\mathbf{x})} L_{e}(\mathbf{x},\omega) \left|\cos\theta\right| d\omega dA} = \frac{L_{e}(\mathbf{x},\omega) \left|\cos\theta\right|}{\Phi_{l}}$$
$$P_{l} = \frac{\Phi_{l}}{\sum_{i \in lights}} = \frac{\Phi_{l}}{\Phi_{total}}$$

• All emitted photons carry the same flux: $\Phi_{p,0} = \frac{\Phi_{\text{total}}}{N}$

Tracing of photon paths

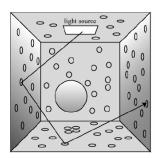


- Similar to light tracing
- Photon-surface intersection:
 - **1. Store "photon"** into a photon map
 - photon = (position, incident direction, flux)
 - 2. Generate reflected direction
 - BRDF importance sampling
 - 3. Update photon flux
 - (next slide)
 - 4. **Russian roulette** randomized absorption (termination)
 - (next slide)

Objective

• Keep the photon flux close to its original value

Photon tracing



3. Update photon flux

$$\Phi_{p,j+1}^{tentative} = \Phi_{p,j} \frac{f_r(\mathbf{x}, \omega_0 \to \omega_i) \left| \cos \theta_0 \right|}{p(\omega_0)}$$

4. **Russian roulette** – randomized photon absorption

$$q_{p,j+1} = \min\left\{1, \frac{\max_{r,g,b}[\Phi_{p,j+1}^{tentative}]]}{\max_{r,g,b}[\Phi_{p,j}]}\right\}$$

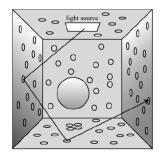
$$\Phi_{p,j+1} = \frac{\Phi_{p,j+1}^{tentative}}{q_{p,j+1}}$$

Survival probability

Updated photon flux on survival

The above strategy keeps the photon flux roughly constant
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Photon tracing



Attention to light refraction

- Recall: When tracing paths from the camera, we need to update radiance according to the 2nd power of the relative IOR
- But photon do not carry radiance but flux no flux change upon refraction

Photon map

Storage of photons into a photon map

Upon each interaction of a photon with a <u>diffuse (or</u> <u>moderately glossy, but not mirror</u>) surface (even on absorption)

Photon map

- A simple linear list of photons during photon tracing
- After photon tracing, we build a *kD*-tree for faster search

Photon

- position:
- incident direction:
- energy (flux):

$$\mathbf{x}_p = (x, y, z)$$

$$\omega_p = (\theta, \phi)$$

$$\Phi_p = (r, g, b)$$

Number of photons: $10^6 - 10^7$ sufficient in many scenes

Photon map

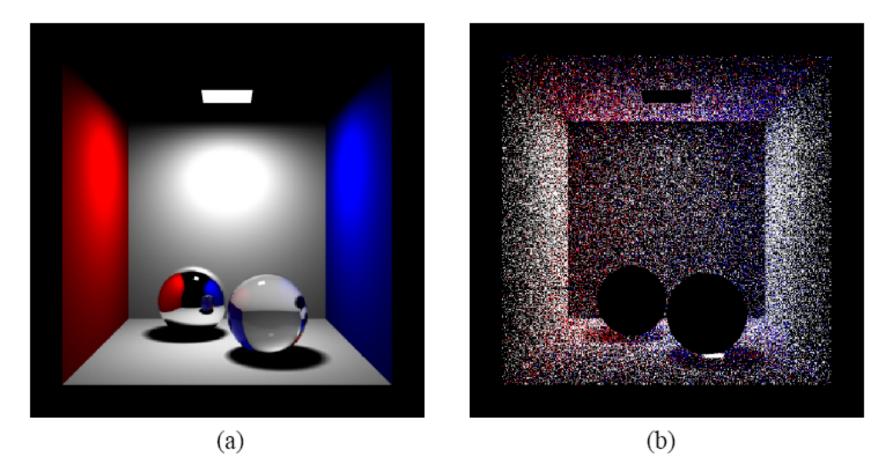
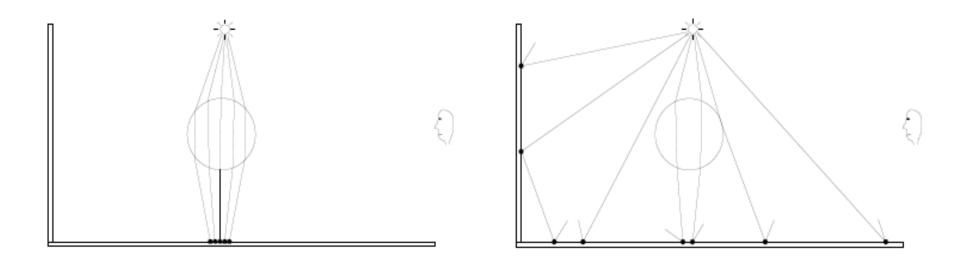


Figure 2.4: "Cornell box" with glass and chrome spheres: (a) ray traced image (direct illumination and specular reflection and transmission), (b) the photons in the corresponding photon map. _{CG III (NPGR010) - J. Křivánek 2015}

Photons represent the equilibrium radiance in the scene



Two photon maps



Caustics map

Global map

Two photon maps

1. Global map: L[S|D]*D

Contains even direct illumination

Caustics map: LS+D

- Contains indirect illumination only
- Is a subset of the global map
- Different use of the two maps in image rendering
 - It's more advantageous to keep them separate

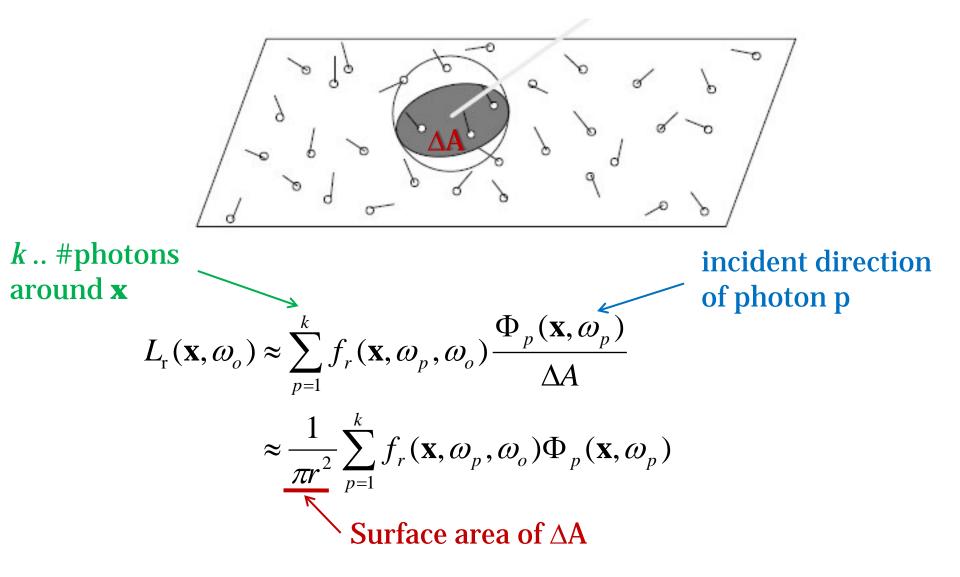
Light path grammar

- E ... eye, L ... light, D ... diffuse, S ... specular
- G ... glossy (often included in D)

Getting the photon maps ready for rendering

- During photon tracing, photons are simply appended into a linear list
- After that, we build a spatial search acceleration structure
 - **In rendering we need to quickly locate** *k* **nearest photons**
 - kD-tree or hashed uniform grid

Radiance estimate from a photon map

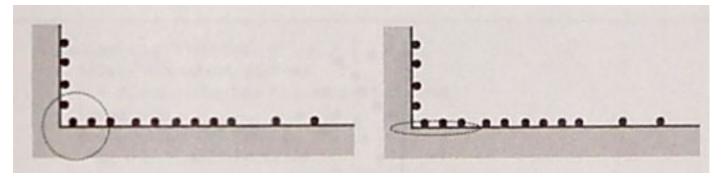


Radiance estimate from a photon map

```
RadianceEstimate(x, wo):
  Color L = (0, 0, 0);
  int k = locateNearestPhotons(x, wo, n max, nearest, r);
  // 'nearest' is an array of k nearest photons to x
  // r is the distance from x to the farthest of them
  if (k < 5) return L;
  for p = 1 to k do
  ł
     if( dot ( nearest[p].wi, N) <= 0 ) continue;
    L += fr(x, wo, nearest[p].wi) * nearest[p].flux;
  return L / (M_PI * r*r);
```

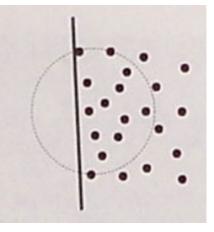
Radiance estimate – issues

Incorrect photons included in the search



- Incorrect estimate of the surface area ΔA
 - Next to a wall,

a caustic or geometry edge



© H.W.Jensen

Fast search of nearest phtons

- Needed for the radiance estimate
- Search of the nearest photons is an instance of

k-nearest neighbor search (k-NN)

*k***-D tree – Construction**

 Recursive space subdivision along the axis with maximum span

Subdivision

- Splitting plane can be in the spatial center (faster, ok) or through the median of photons
- When using the median split rule, the resulting tree is perfectly balanced and can be stored in a linear array
 - Descendants of the photon at index *i* are at indexes 2*i* a 2*i*+1

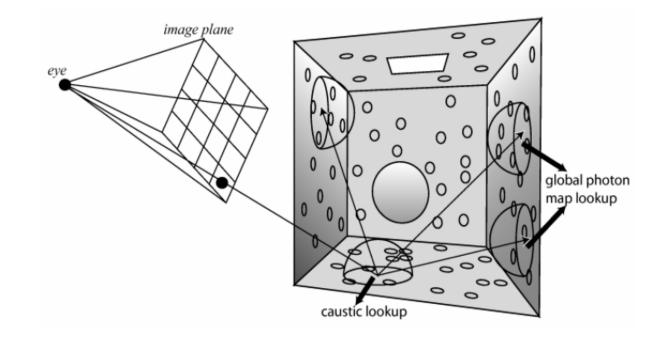
k-D tree – Nearest neighbor search

- Pruning of the search
 - Either: According to the distance to the already located *k*-th nearest photon (when searching *k* nearest)
 - Photons located so far are maintained in a max-heap
 - Or: According to the search radius *r* (when locating particles witin a fixed radius "range query")

Phase 2: Rendering with photon maps

Distributed ray tracing from the camera

- Recursion replaced by a photon map lookup
- For highly specular surfaces we still use recursion as in classic path tracing



Reflected radiance calculation

Reflected radiance: this is what we want to calculate

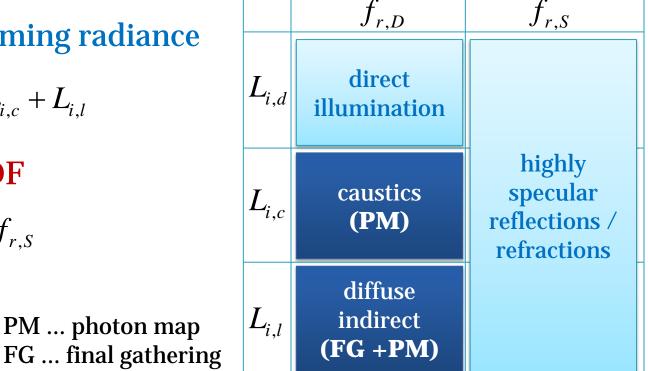
$$L_r(\mathbf{x}, \omega_o) = \int_{\Omega} L_i(\mathbf{x}, \omega_i) f_r(\mathbf{x}, \omega_i \to \omega_o) \cos \theta_i \, \mathrm{d}\omega_i$$

Split the incoming radiance

$$L_{i} = L_{i,d} + L_{i,c} + L_{i,l}$$

Split the BRDF

$$f_r = f_{r,D} + f_{r,S}$$



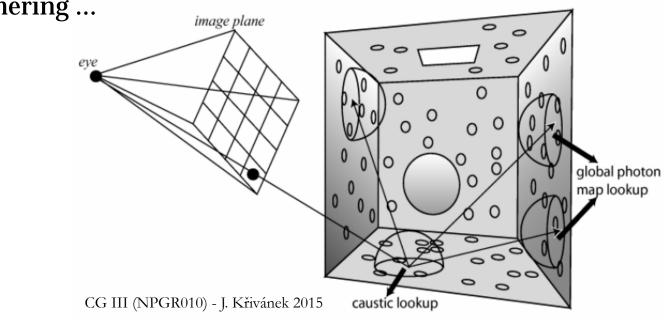
Reflected radiance calculation

When not using photon maps

- Direct illumination
 - As usual: light source area sampling + shadow rays
- **Ideal mirror reflections / refractions**
 - As usual: deterministic secondary rays
- With photon maps
 ...

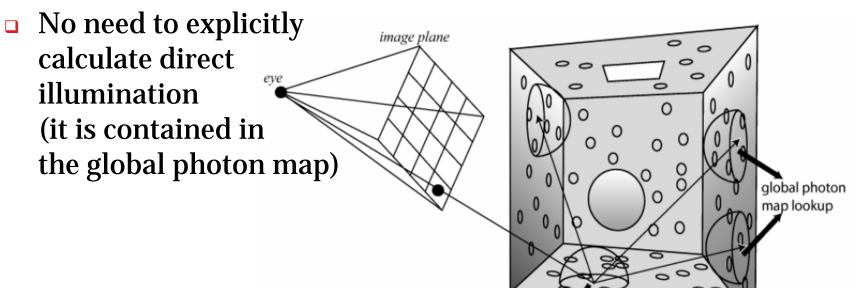
Illumination calculation for a primary ray (or after a mirror reflection)

- Using the photon map
 - Caustics
 - Radiance estimate from the caustic photon map
 - Indirect illumination on diffuse or moderately glossy surfaces
 - Final gathering ...



Final gathering (FG)

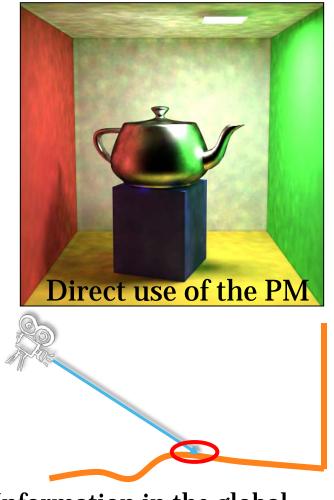
- Indirect illumination on diffuse and moderately glossy surfaces
- One level of recursion as in distributed ray tracing (i.e. path tracing with massive splitting)
- For the intersection of secondary rays, use radiance estimate from the global photon map



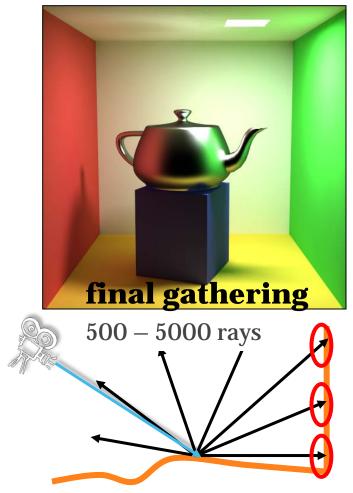
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caustic lookup

Why do we need final gathering?



Information in the global photon map is too noisy for a direct use CG III (



Inaccuracy in the global photon map is "averaged out"

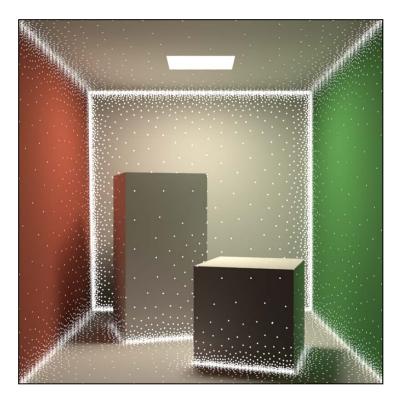
Why is there no final gathering for caustics?

 Caustics = light focusing => sufficient photon density (beware, it's just a heuristic, may not always work well)

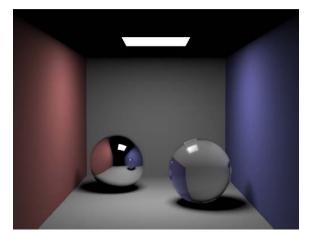


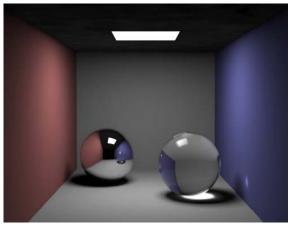
Accelerating final gathering

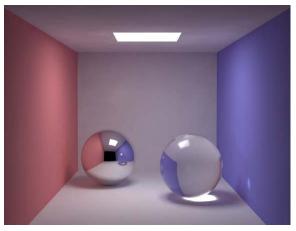
Irradiance caching (next time)



Results







přímé osvětlení (21 s)

kaustiky (45 s)

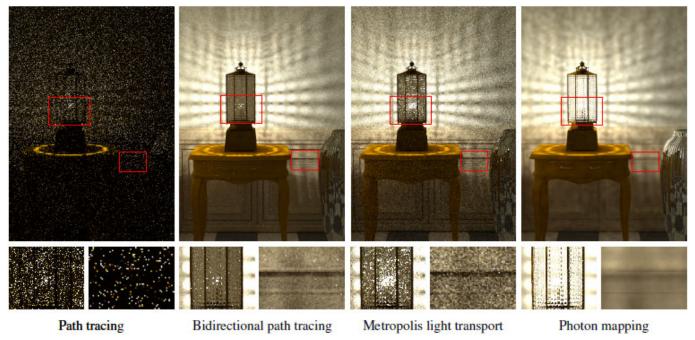
50 000 photons in the caustic map

GI (66 s)

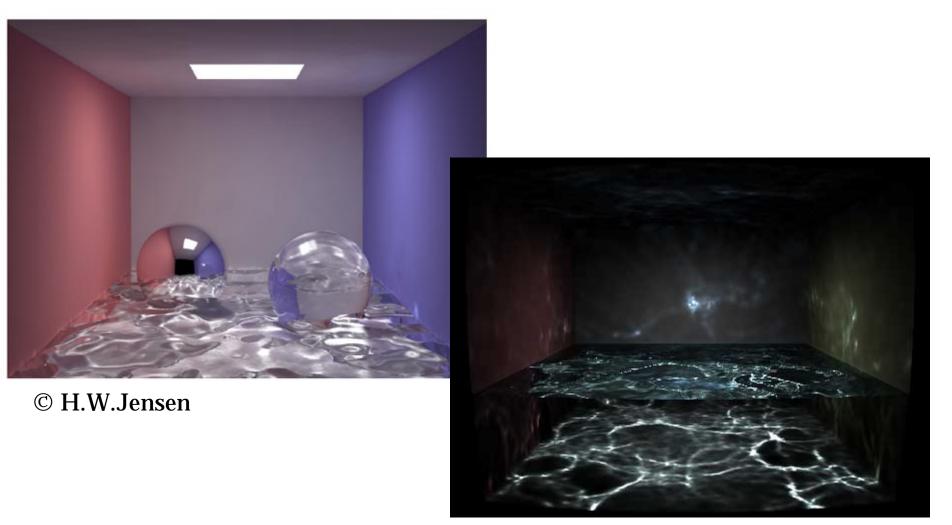
200 000 photons in the global map

What is photon mapping good at?

- Directly and indirectly visible caustics
- More generally: SDS paths (like light on the pool bottom)
 - Classic MC algorithms fail in such cases (path tracing, bidirectional path tracing, metropolis light transport)

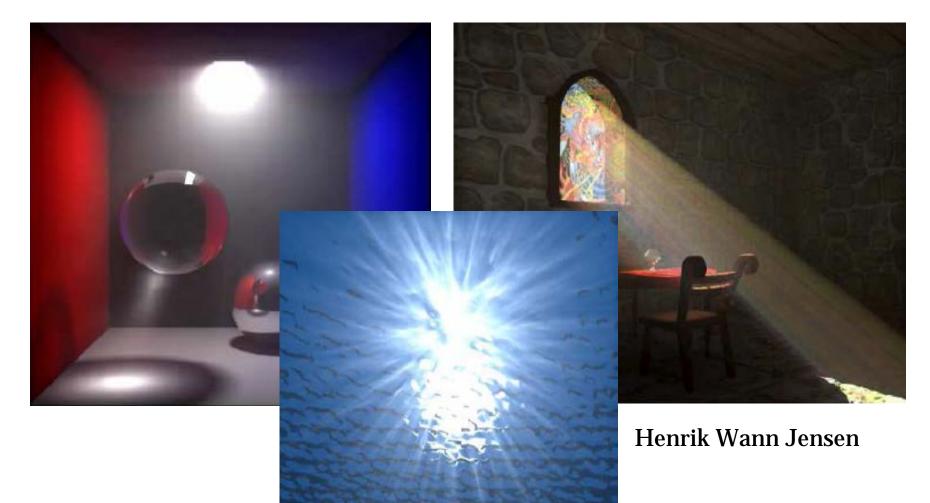


SDS paths



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Photon mapping can be easily extended to handle scattering in media



... and subsurface scattering



Photon mapping problems

Does not work well on glossy surfaces



Photon mapping problems

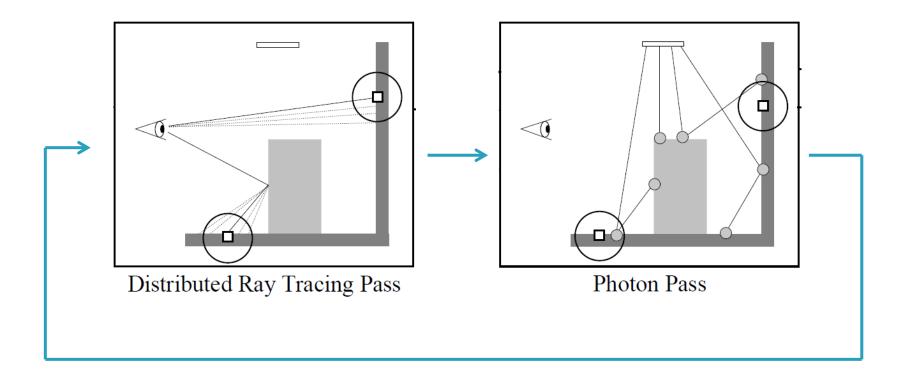
- Does not work well on glossy surfaces
- So, what's wrong?
 - Radiance estimate from the photon map on a glossy surface suffers from high variance

Theoretical problems of photon mapping

- Result is not unbiased
 - Contains systematic error
- Result is **consistent**
 - It theoretically converges as the photon count goes to infinity
 - **But this is practically unachievable**
 - **Solution: progressive photon mapping**

- Rendering in iterations
- In each iteration, reduce the photon search radius such that:
 - **•** Total **bias goes to zero**, and
 - Total variance goes to zero
 - (i.e. the resulting estimator is consistent)

Iterative procedure



© Hachisuka et al.

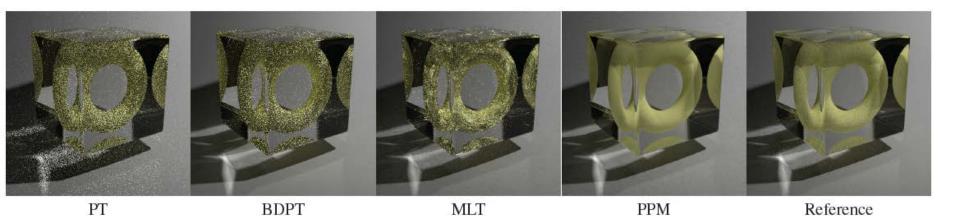


Figure 7: Torus embedded in a glass cube. The reference image on the far right have been rendered using path tracing with 51500 samples per pixel. The Monte Carlo ray tracing methods fail to capture the lighting within the glass cube, while progressive photon mapping provides a smooth result using the same rendering time.

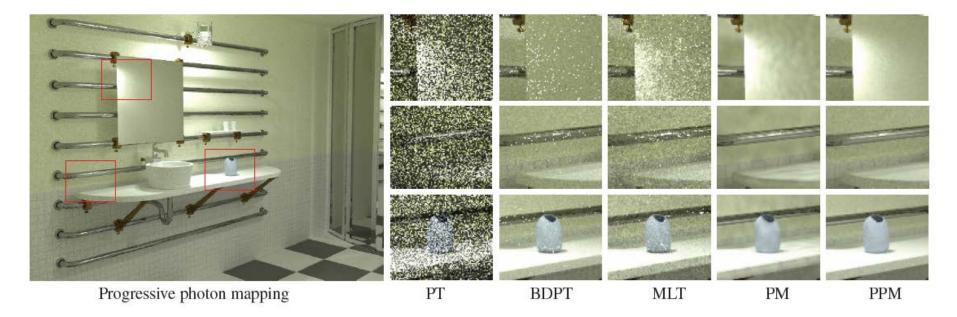
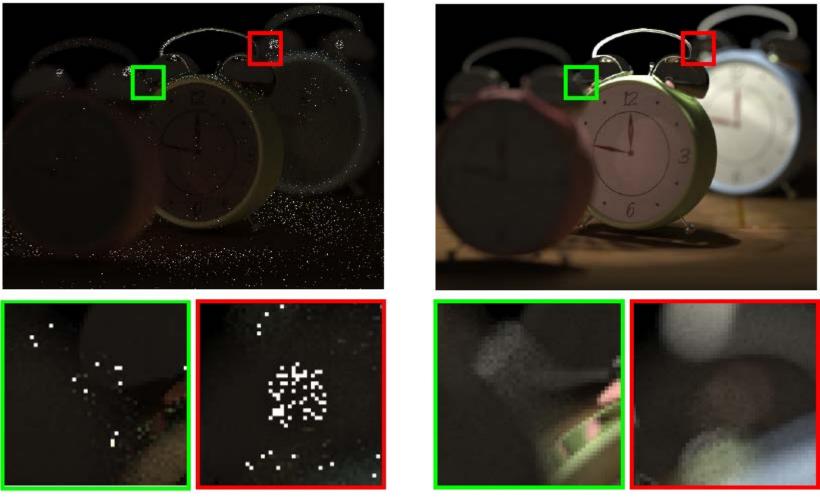


Figure 8: Lighting simulation in a bathroom. The scene is illuminated by a small lighting fixture consisting of a light source embedded in glass. The illumination in the mirror cannot be resolved using Monte Carlo ray tracing. Photon mapping with 20 million photons results in a noisy and blurry image, while progressive photon mapping is able to resolve the details in the mirror and in the illumination without noise.



BDPT

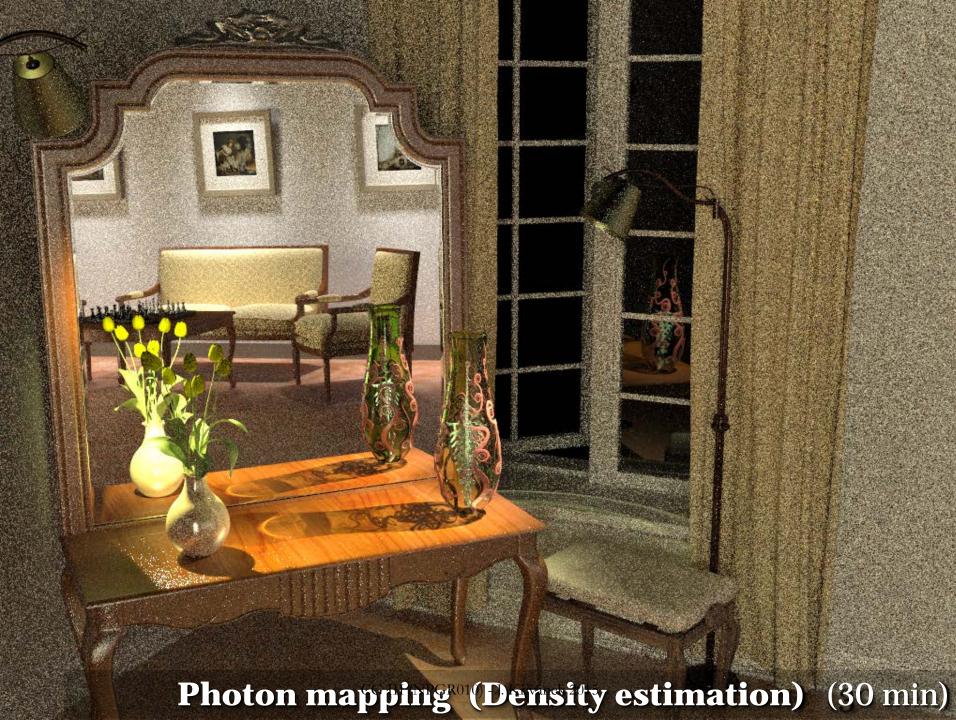
PPM

Our work: Vertex Connection and Merging

Robust photon mapping

- Where exactly on the camera sub-path should we lookup the photons?
- Commonly solved via a **heuristic**:
 - Diffuse surface ... make the look-up right away
 - Specular surface ... continue tracing and make the look-up later
- But what exactly should be classified as "diffuse" and "specular"?
 - We need a more universal and robust solution
 - **Solution:**
 - Bidirectional photon mapping [Vorba 2011]
 - Vertex Connection and Merging [Georgiev et al., 2012]

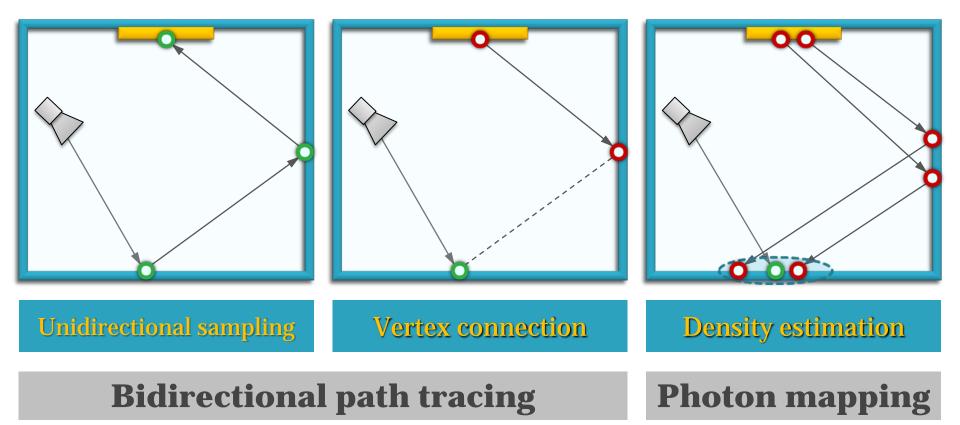
^{cc} **Bidfrectional path tracing** (30 min)



Vertex commection and merging (30 min)

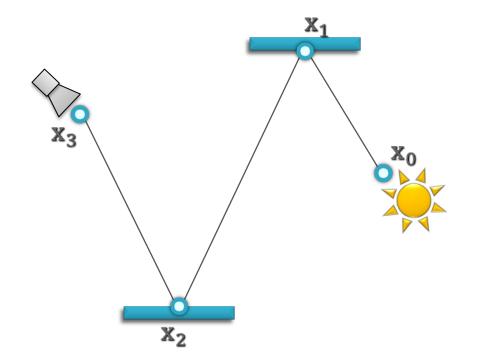
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BPT vs PM

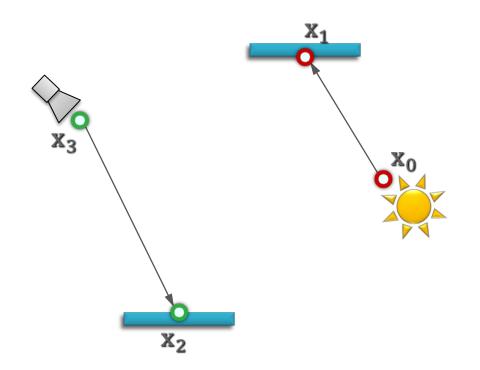


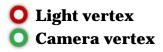
Overview

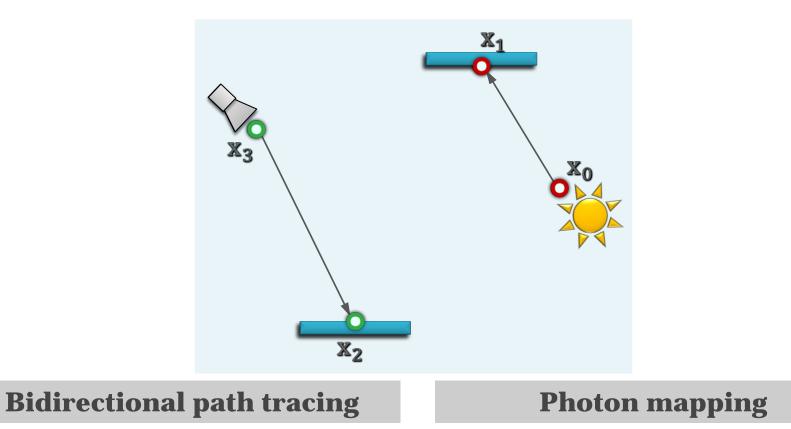
- Problem: different mathematical frameworks
 - **BPT**: Monte Carlo estimator of a path integral
 - **PM**: Density estimation
- Key contribution: Reformulate photon mapping in Veach's path integral framework
 - Formalize as path sampling technique
 - 2) Derive path probability density
- Combination of BPT and PM into a robust algorithm



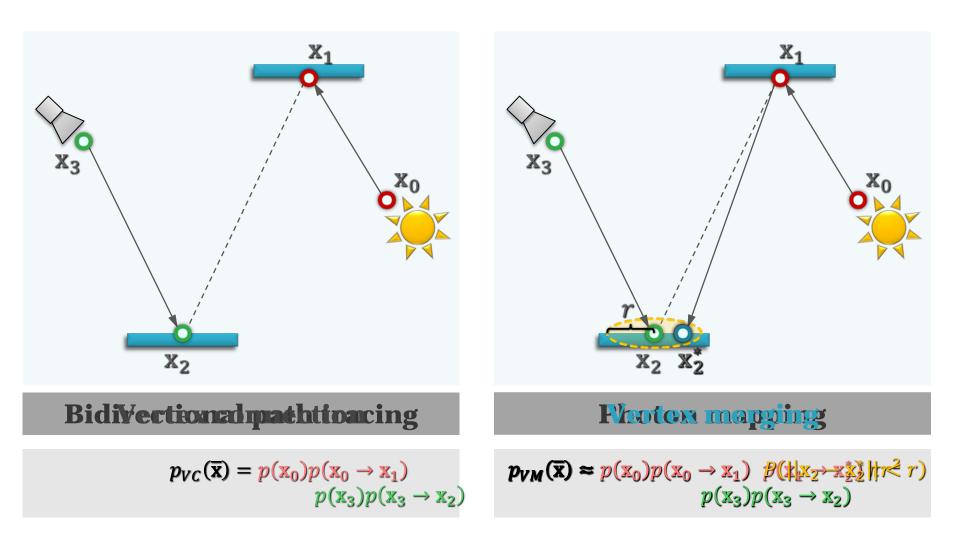






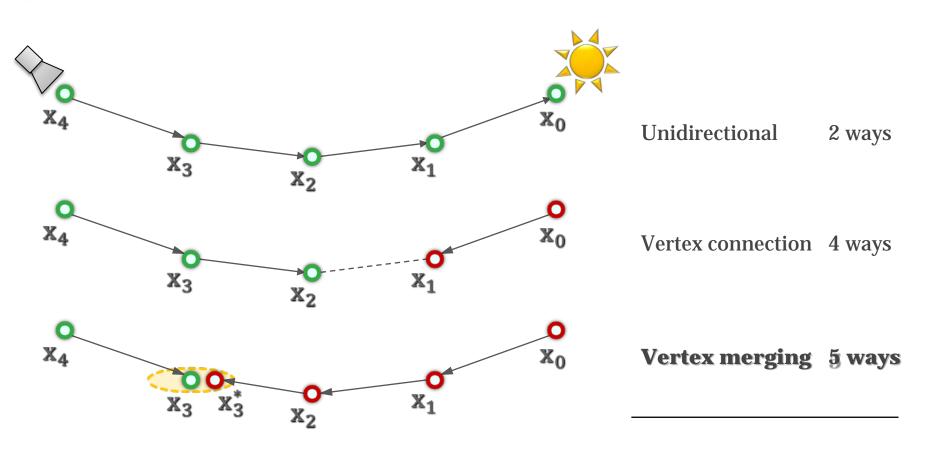


Light vertexCamera vertex



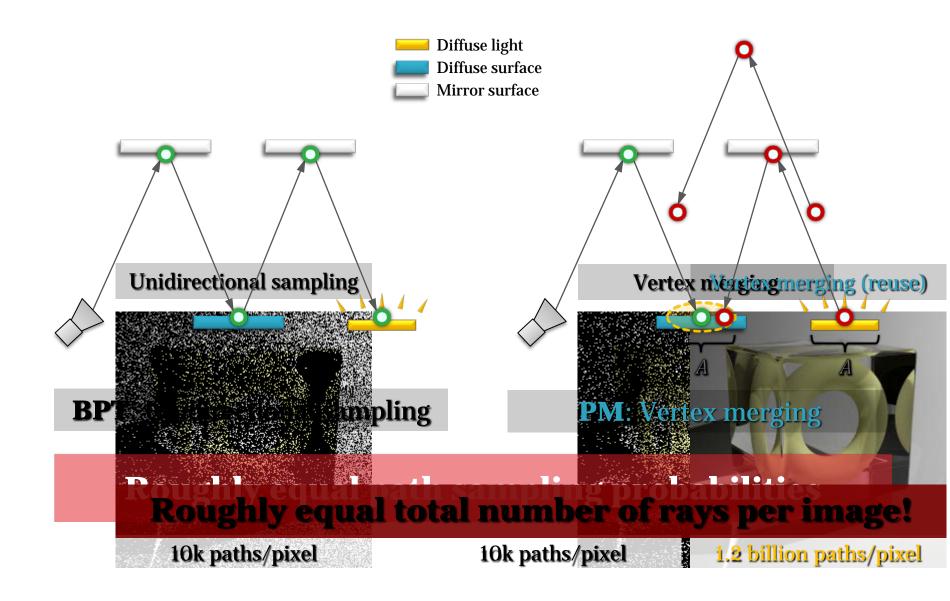
Sampling techniques

Light vertexCamera vertex



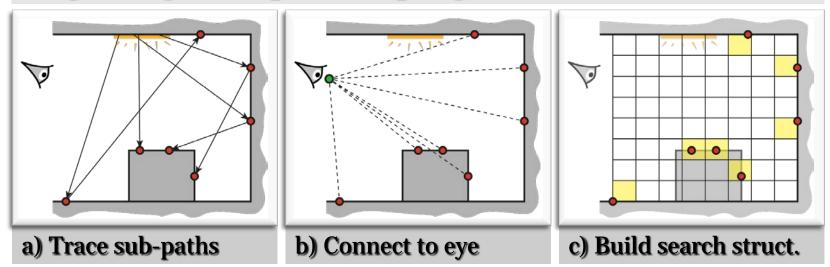
Total 11 ways

Technique comparison – SDS Paths

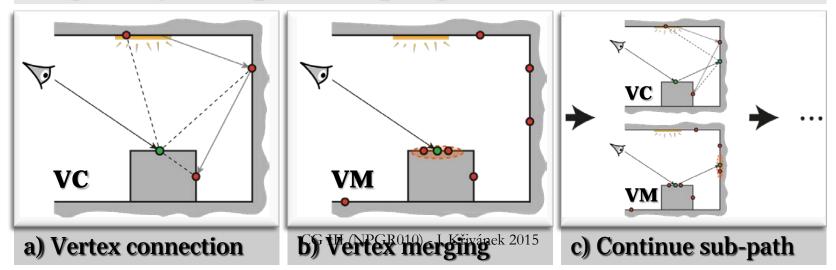


VCM – Algorithm overview

Stage 1: Light sub-path sampling



Stage 2: Eye sub-path sampling



^{cc} **Bidirectional path tracing** (30 min)

Stochastic progressive photon mapping (30 min)

Vertex connection and merging (30 min)

CG III Reliativé téchnique contributions

VM





Stochastic progressive piloton mapping (30 min)



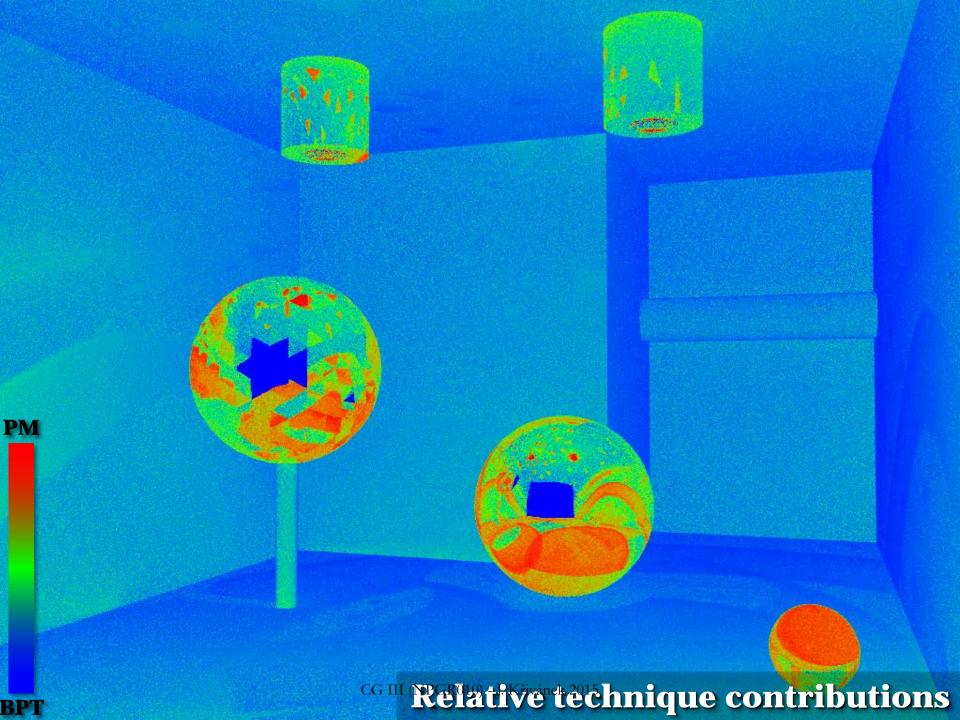




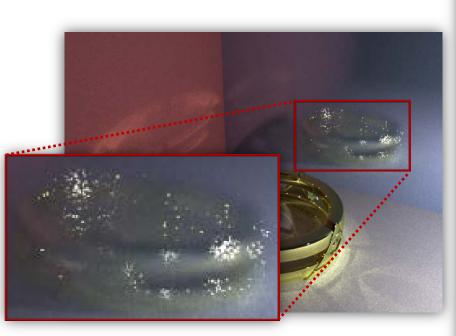
^{CG I}Bidiffection and path tracing (30 min)

Stochastic progressive ploton mapping (30 min)

Vertex connection and merging (30 min)



Remaining challenges





- Georgiev et al., "Light Transport Simulation with Vertex Connection and Merging"
- Hachisuka et al. "A Path Space Extension for Robust Light Transport Simulation"
 - **Same algorithm, different theoretical derivations**

VCM in production









References

- Jensen H.W.: Realistic Image Synthesis using Photon Mapping. A.K. Peters, 2001
- Hachisuka & Jensen. Stochastic Progressive Photon Mapping, ACM Trans. Graph. (SIGGRAPH Asia 2009). <u>link</u>
- Knaus & Zwicker. Progressive photon mapping: A probabilistic approach. ACM Trans. Graph., 2011. link
- Georgiev, Křivánek, Davidovič, Slusallek. Light Transport Simulation with Vertex Connection and Merging. ACM Trans. Graph. (SIGGRAPH Asia 2012). <u>link</u>
- Hachisuka, Pantaleoni, Jensen. A Path Space Extension for Robust Light Transport Simulation. ACM Trans. Graph. (SIGGRAPH Asia 2012). <u>link</u>