

# Image transparency, composition by $\alpha$ -blending

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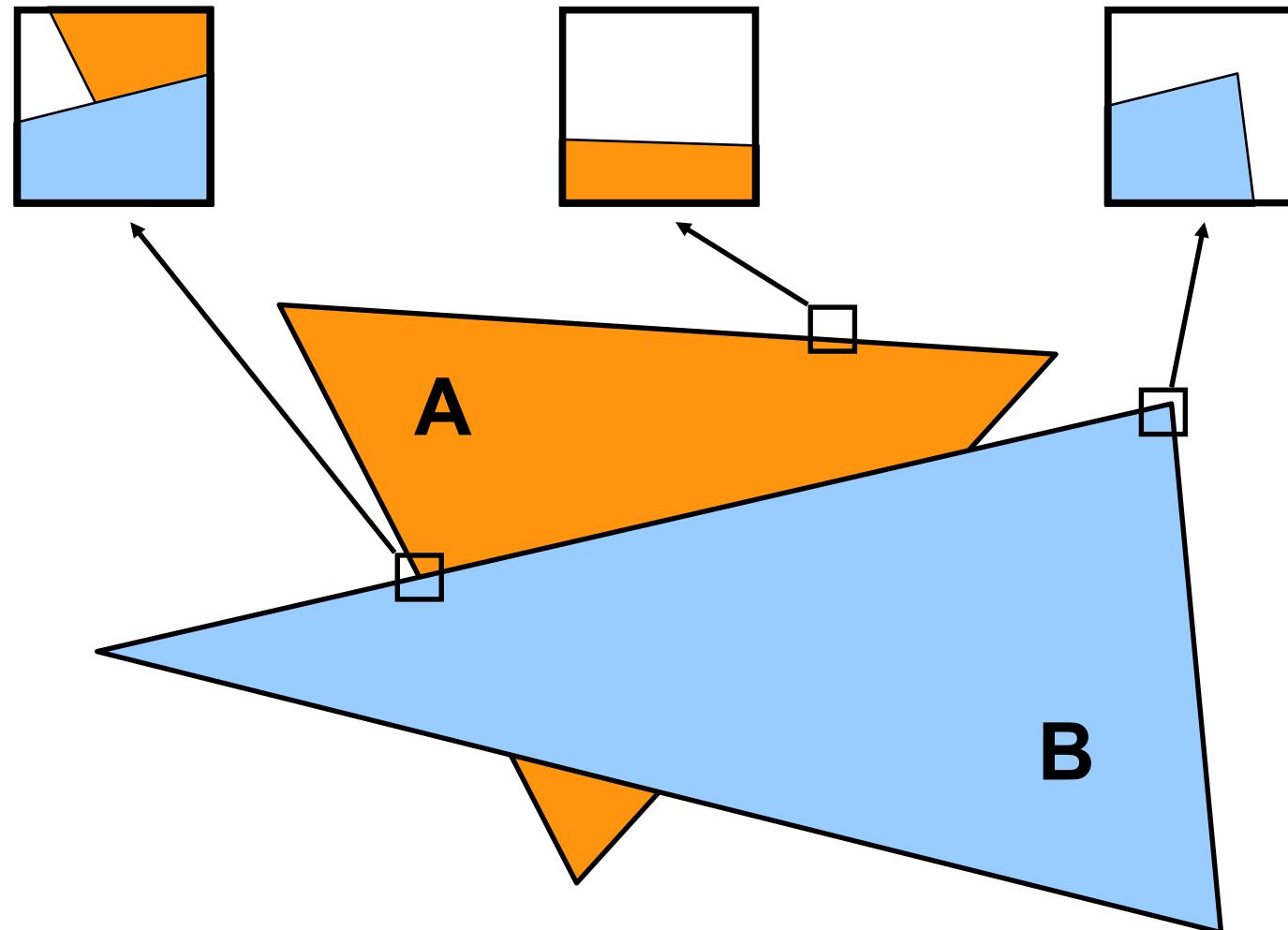


# Image composition

- composition using **real images**
  - changing (tampering with) image background, ..
- **image fading („fade-in”, „fade-out”)**
  - animation, video cutting
- **image synthesis**
  - picture can be assembled from several independent parts (e.g. background, foreground, flames, mist, clouds, ..)



# Pixel-area coverage





# $\alpha$ channel

- ◆ percentual **pixel-area coverage** („opaque paint“)
  - complementary to „transparency“
  - $\alpha = 0$  ... absolutely transparent (no effect on result)
  - $\alpha = 1$  ... completely opaque („nothing shows through“)
- ◆  **$\alpha$  value** stored in every pixel
  - integer representation ( $0 \div 255$ )
  - quadruple [ R, G, B,  $\alpha$  ]
  - more practical format [ Ra, Ga, Ba,  $\alpha$  ]

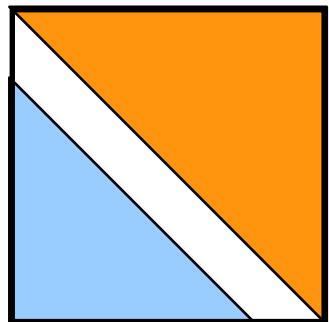


# Composition of two images

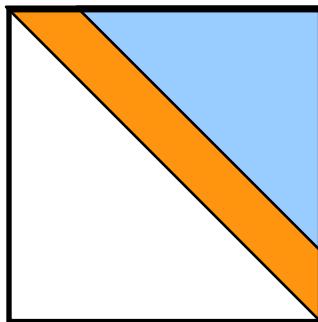
- two source pixels:  $[A, \alpha_A]$  and  $[B, \alpha_B]$ 
  - need to define result  $[C, \alpha_C]$
- ? composition model ?

$$\alpha_A = 0.5$$

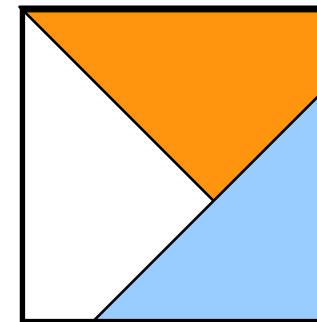
$$\alpha_B = 0.4$$



?



?

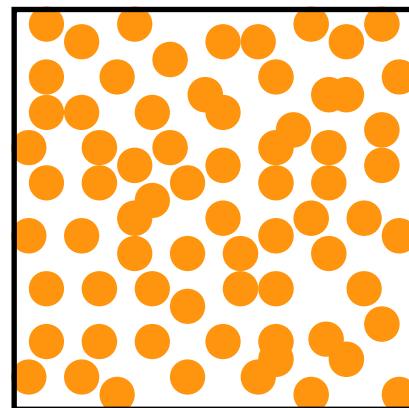




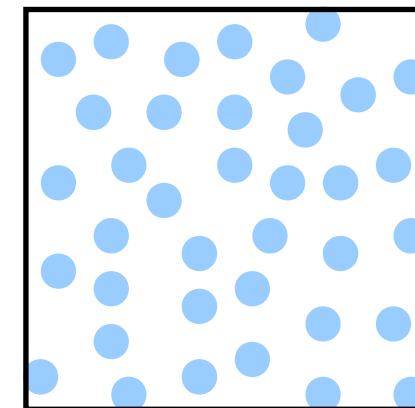
# Pixel-area coverage model

- pixel  $[A, \alpha_A]$  is **randomly covered** by an opaque paint  $A$  (with **uniform probability**  $\alpha_A$ )
  - composition of arbitrary geometric. independent shapes
  - sufficient in most cases

$\alpha = 0.5$



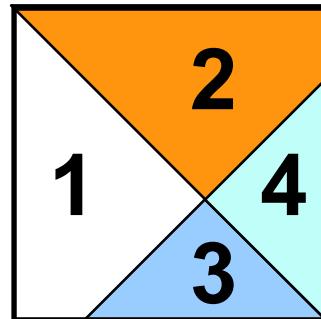
$\alpha = 0.2$





# Superimposition of two pixels

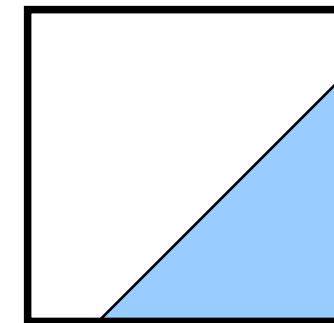
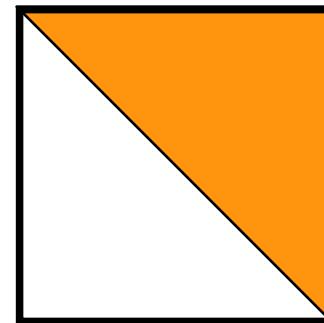
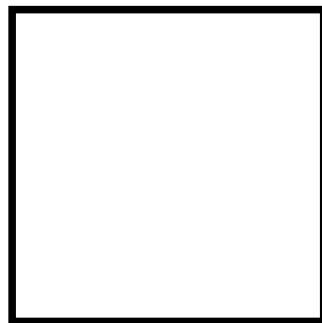
segment	area	color
1	<b>void</b>	$(1 - \alpha_A)(1 - \alpha_B)$
2	<b>A</b>	$\alpha_A(1 - \alpha_B)$
3	<b>B</b>	$\alpha_B(1 - \alpha_A)$
4	<b>A i B</b>	$\alpha_A\alpha_B$



total 12 combinations



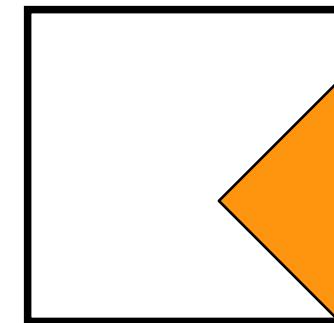
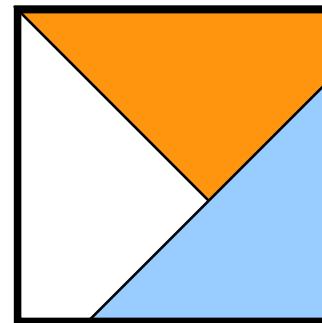
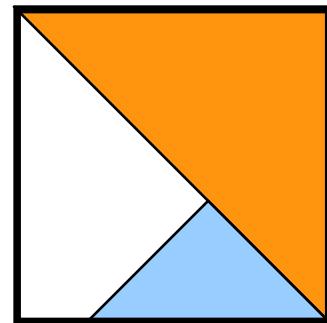
# Superimposition of two pixels



<b>op.</b>	<b>clear</b>	<b>A</b>	<b>B</b>
<b>colors</b>	<b>(0,0,0,0)</b>	<b>(0,A,0,A)</b>	<b>(0,0,B,B)</b>
$F_A$	0	1	0
$F_B$	0	0	1



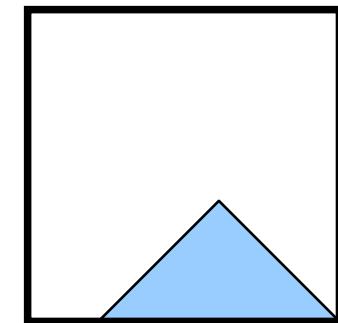
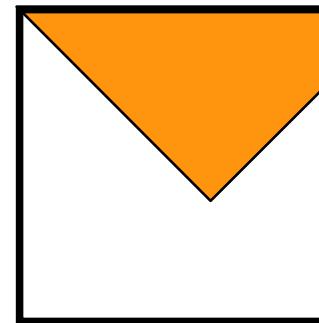
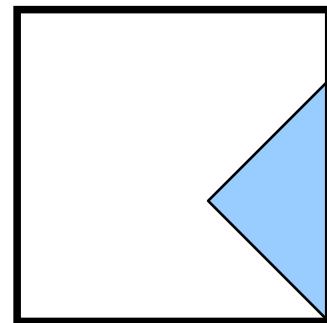
# Superimposition of two pixels



<b>op.</b>	<b>A over B</b>	<b>B over A</b>	<b>A in B</b>
<b>colors</b>	<b>(0,A,B,A)</b>	<b>(0,A,B,B)</b>	<b>(0,0,0,A)</b>
$F_A$	1	$(1 - \alpha_B)$	$\alpha_B$
$F_B$	$(1 - \alpha_A)$	1	0



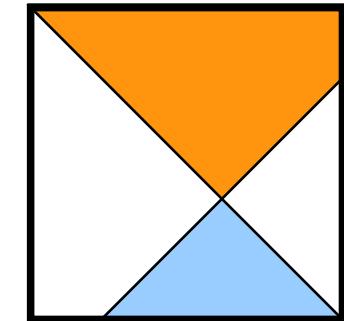
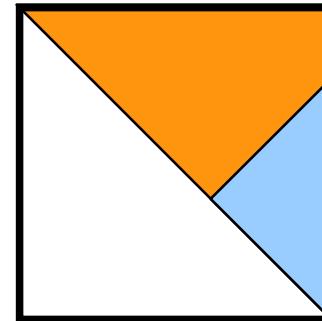
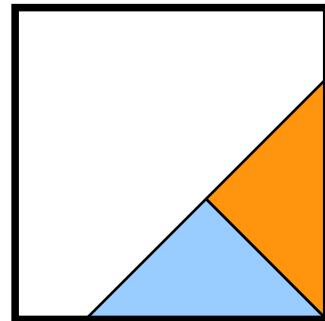
# Superimposition of two pixels



op.	B in A	A out B	B out A
colors	(0,0,0,B)	(0,A,0,0)	(0,0,B,0)
$F_A$	0	$(1 - \alpha_B)$	0
$F_B$	$\alpha_A$	0	$(1 - \alpha_A)$



# Superimposition of two pixels



<b>op.</b>	<b>A atop B</b>	<b>B atop A</b>	<b>A xor B</b>
<b>colors</b>	<b>(0,0,B,A)</b>	<b>(0,A,0,B)</b>	<b>(0,A,B,0)</b>
$F_A$	$\alpha_B$	$(1 - \alpha_B)$	$(1 - \alpha_B)$
$F_B$	$(1 - \alpha_A)$	$\alpha_A$	$(1 - \alpha_A)$



# Implementation

- ◆ quadruples **RGB $\alpha$**  are stored as [ **R $\alpha$ , G $\alpha$ , B $\alpha$ ,  $\alpha$  ]
  - $\alpha$ -channel will be multiplied in any case**
- ◆ conversion back to RGB .. **dividing by  $\alpha$** 
  - rare operation
  - just throwing away the 4<sup>th</sup> component looks much better
- ◆ **superimposition of two pixels**
  - all four components are multiplied by the factor **F<sub>x</sub>**
  - linear blending operation on quadruples (fast SSE, GPU instructions..)



# Operator summary

- ◆ general binary superimposition  $A \text{ op } B:$

$$[ F_A R_A + F_B R_B, F_A G_A + F_B G_B, F_A B_A + F_B B_B, F_A \alpha_A + F_B \alpha_B ]$$

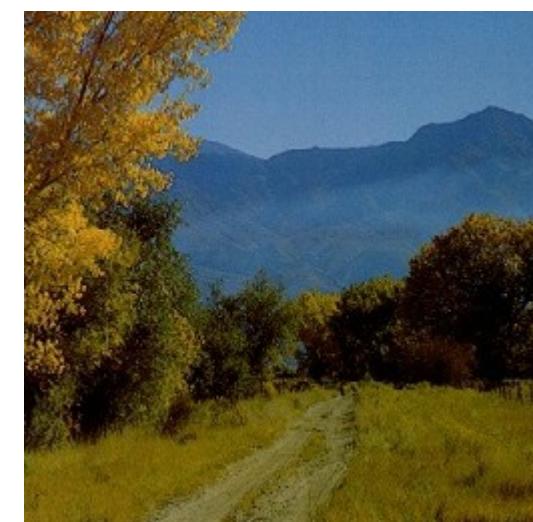
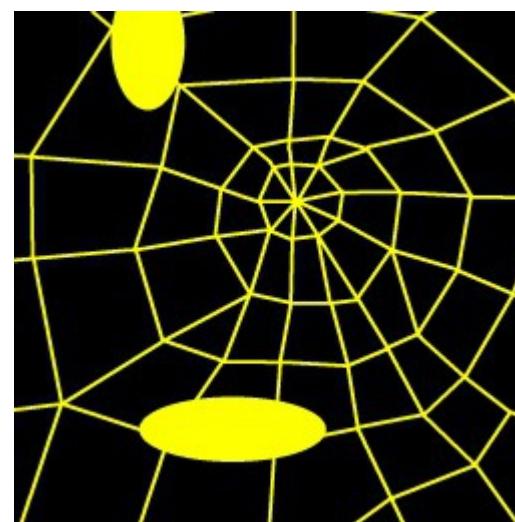
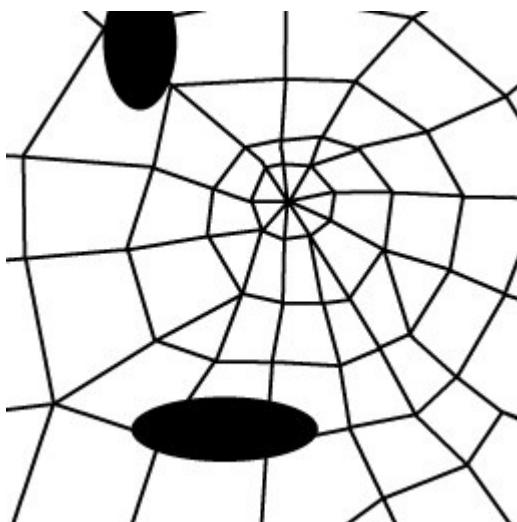
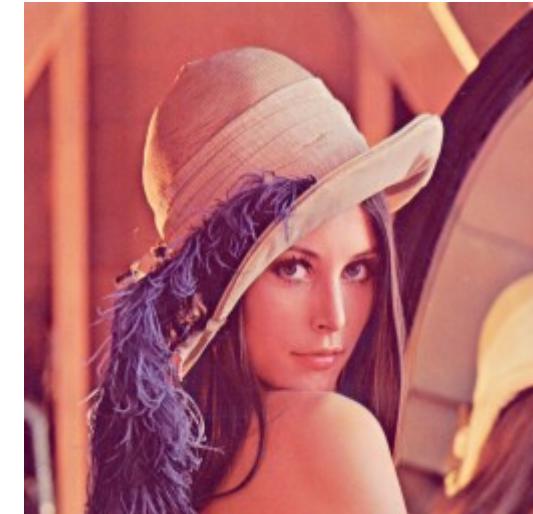
- ◆ **darken** (  $A, \rho$  ) =  $[ \rho R_A, \rho G_A, \rho B_A, \alpha_A ]$

- ◆ **fade** (  $A, \delta$  ) =  $[ \delta R_A, \delta G_A, \delta B_A, \delta \alpha_A ]$

- ◆ **opaque** (  $A, \omega$  ) =  $[ R_A, G_A, B_A, \omega \alpha_A ]$

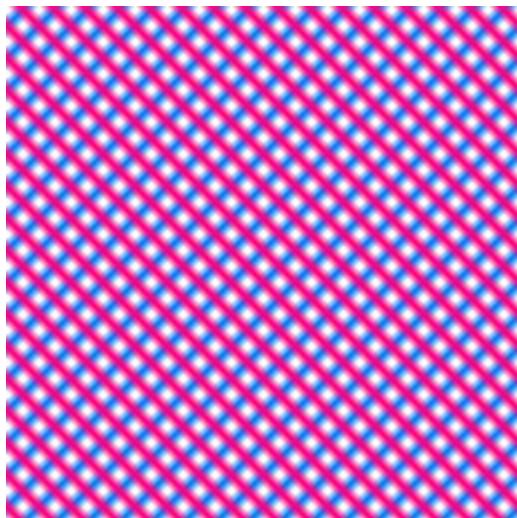


# Examples – inputs





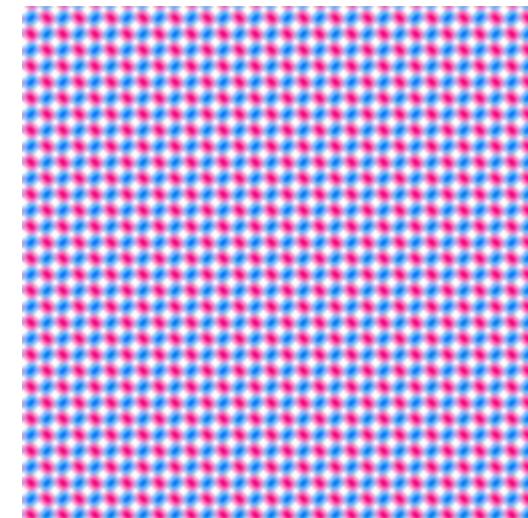
# Examples – binary op. I



1 over 2



1 atop 2



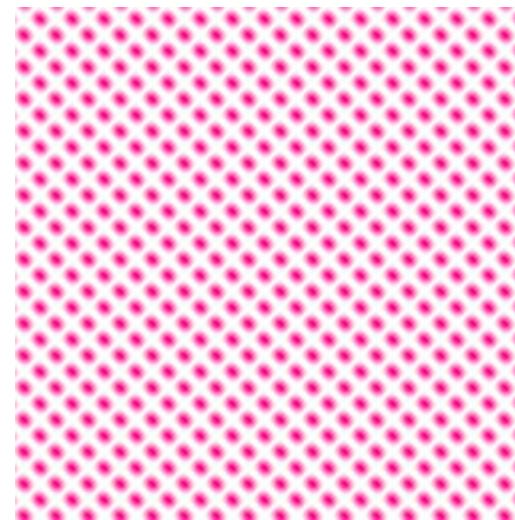
1 xor 2



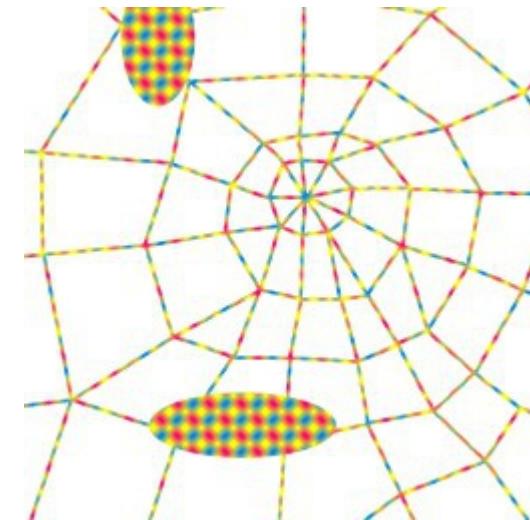
# Examples – binary op. II



1 in 2



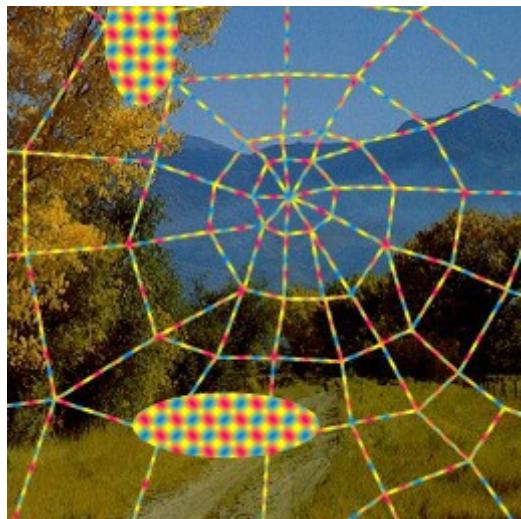
1 out 2



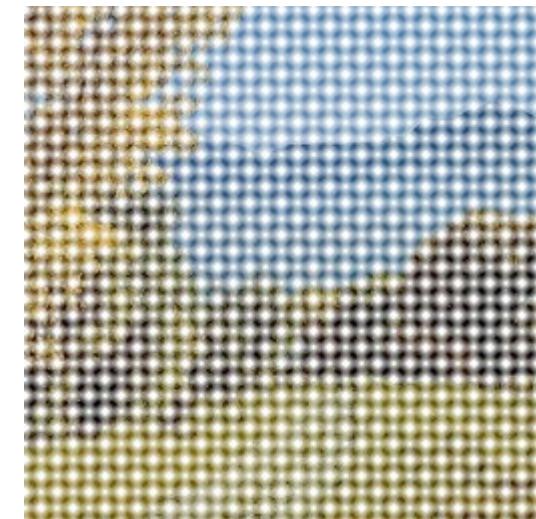
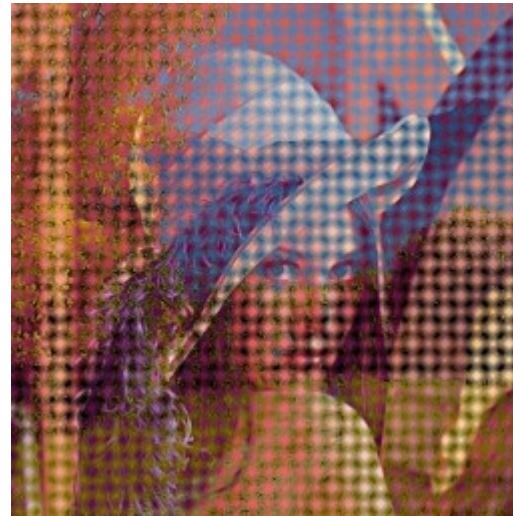
(1 xor 2) atop W



# Examples – binary op. III



$((1 \text{ xor } 2) \text{ atop } W) \text{ over } V$



$V \text{ atop } (1 \text{ xor } 2)$

$(V \text{ atop } (1 \text{ xor } 2)) \text{ over } L$



# Examples – image fading



`fade( L, horiz )`



`fade( L, horiz ) over V`



# Operator „plus”

- ➊ additive operator **A plus B:**  
**[  $R_A + R_B$ ,  $G_A + G_B$ ,  $B_A + B_B$ ,  $\alpha_A + \alpha_B$  ]**
  - carefully! (can cause overflow)
- ➋ example 1: **fading** of two images  
**fade(A,t) plus fade(B,1 - t)**
- ➌ example 2: **tree on fire**  
**(FFire plus (BFire out Tree)) over darken(Tree,0.8)**  
**over Background**

Originally from the movie „Star Trek II“ (1982) – „Genesis Effect“:  
<https://www.youtube.com/watch?v=Qe9qSLYK5q4>



# The End

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More info:

- **J. Foley, A. van Dam, S. Feiner, J. Hughes:** *Computer Graphics, Principles and Practice*, 835-843
- **T. Porter, T. Duff** (Lucasfilm): *Compositing Digital Images*, Computer Graphics 18(3), 1984  
<https://keithp.com/~keithp/porterduff/p253-porter.pdf>