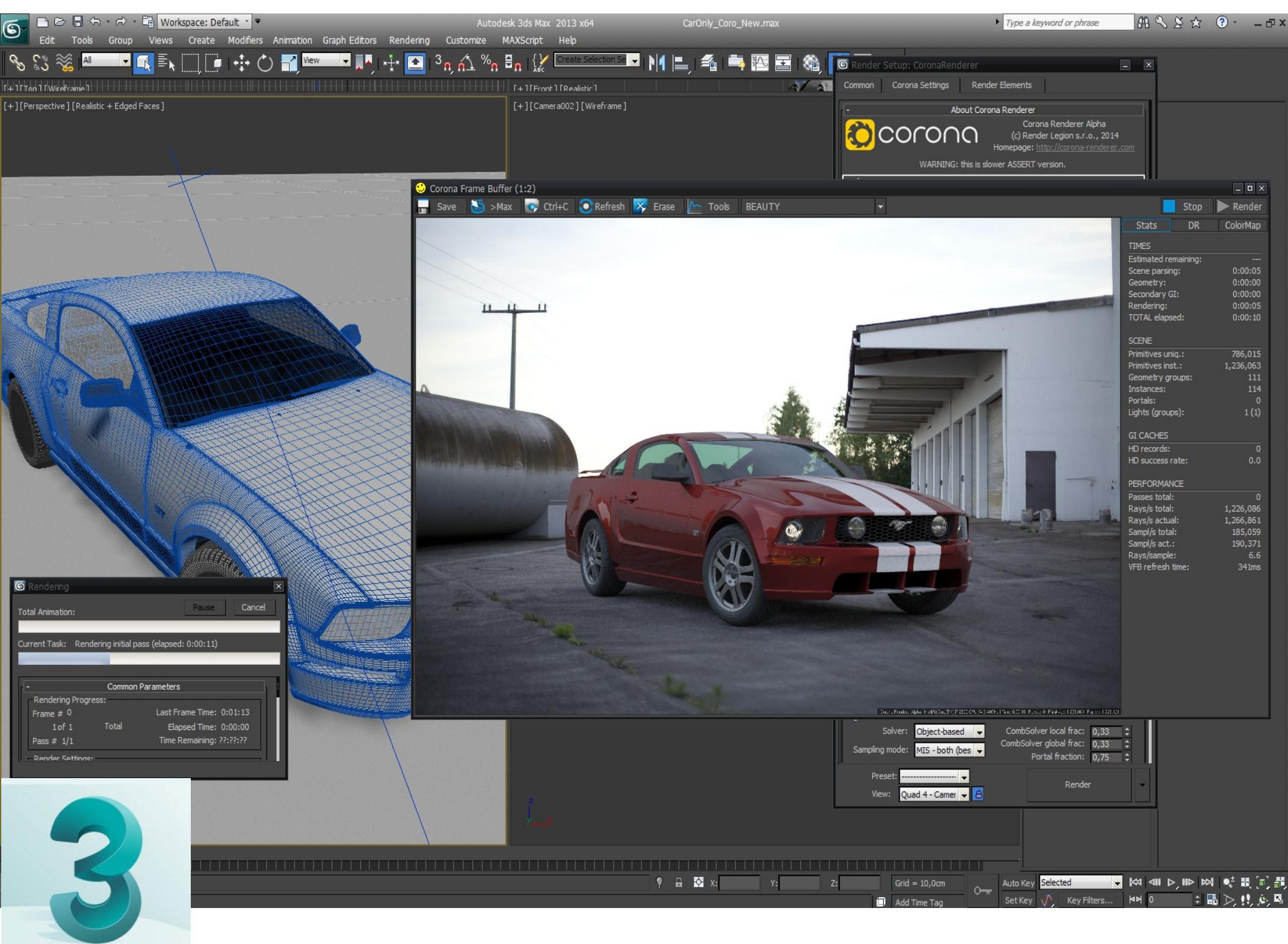


Rendering & Ray Tracing

© 1996-2024 Josef Pelikán
CGG MFF UK Praha

pepca@cgg.mff.cuni.cz
<https://cgg.mff.cuni.cz/~pepca/>





Applications

Design, architecture, art

- indoor light propagation



Entertainment

- cinema and TV (IL&M, Pixar, DreamWorks... "off-line")
- video games ("real-time")

Media

- television (virtual studios...)
- advertisement



Advertisement



© Bertrand Benoit

Architectural Visualization



© Pavel Stavila

created by Pavel Stavila
pavelstavila@live.com



Possible goals of realistic rendering

Accurately **mimic the world** around us (or a fantasy world)

- a virtual scene in a computer

Accurately **simulate the propagation of light** in a scene?

- "predictive rendering"

Or just "**believable rendering**"...?

- the layperson should not know that the image is artificial

Rendering speed

- "**offline**" rendering (advertising, film – computer farms, etc.)
- "**Real-time**" (min. 25 fps)



What we will cover in this course

Accurately mimic the world around us (or a fantasy world)

- a virtual scene in a computer

~~Accurately simulate the propagation of light in a scene?~~

- "predictive rendering"

Or just "believable rendering"....?

- the layperson should not know that the image is artificial
-

Rendering speed

- "offline" rendering (advertising, film – computer farms, etc.)
- ~~"Real-time"~~ (min. 25 fps)



Not covered!

Real-time graphics in video games

- although realistic rendering is getting here nowadays

GPU programming (one little exception – RTX)

3D scene modeling (Maya, 3DS MAX, Blender...)

Animation

Simulation of physical phenomena

- waves, explosions, sky, clouds...

Image analysis, computer vision, artificial intelligence

- nor the use of machine learning in rendering



History – Classical Rendering

Straßer, Catmull 1974: Z-buffer

Faceted model

- most often triangular meshes

Visibility calculation

- Z-buffer

Approximate lighting conditions

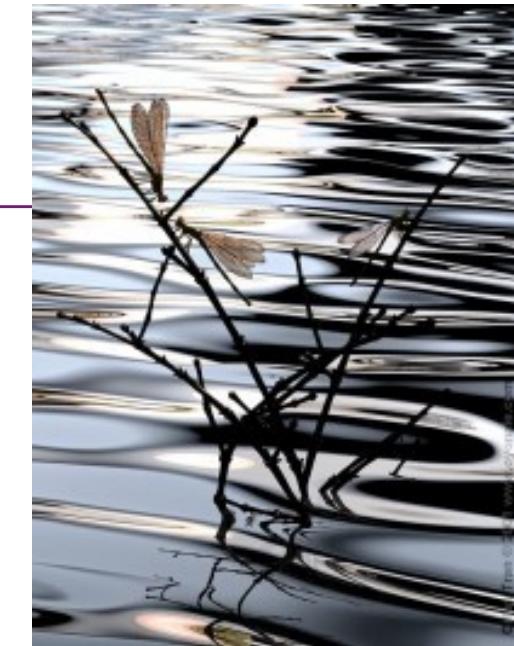
- local lighting model, shadow casting

Contemporary GPUs: **textures, shadows, shaders, multiple passes, deferred lighting...**



© Arkhivrag, Unity forum

History – Ray-tracing



Whitted 1979: **backward Ray-tracing**

Geometric approach

- only the ideally reflected ray is traced

Computationally very demanding **calculation of the intersection** of the ray with the scene

- >90% time → acceleration

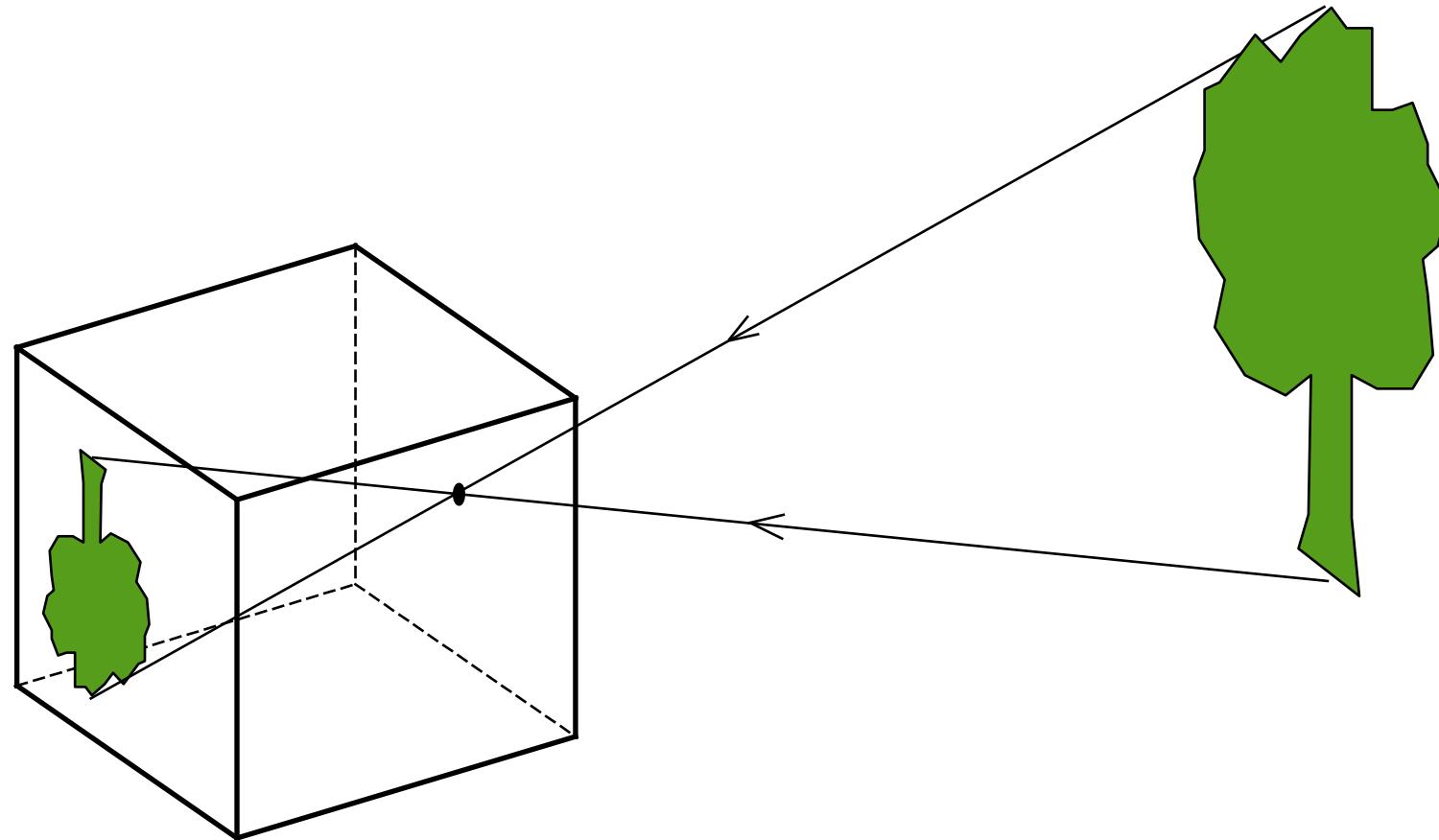
Easy appearance improvements

- textures, anti-aliasing, “shaders”
- distributed R-T (Monte-Carlo)



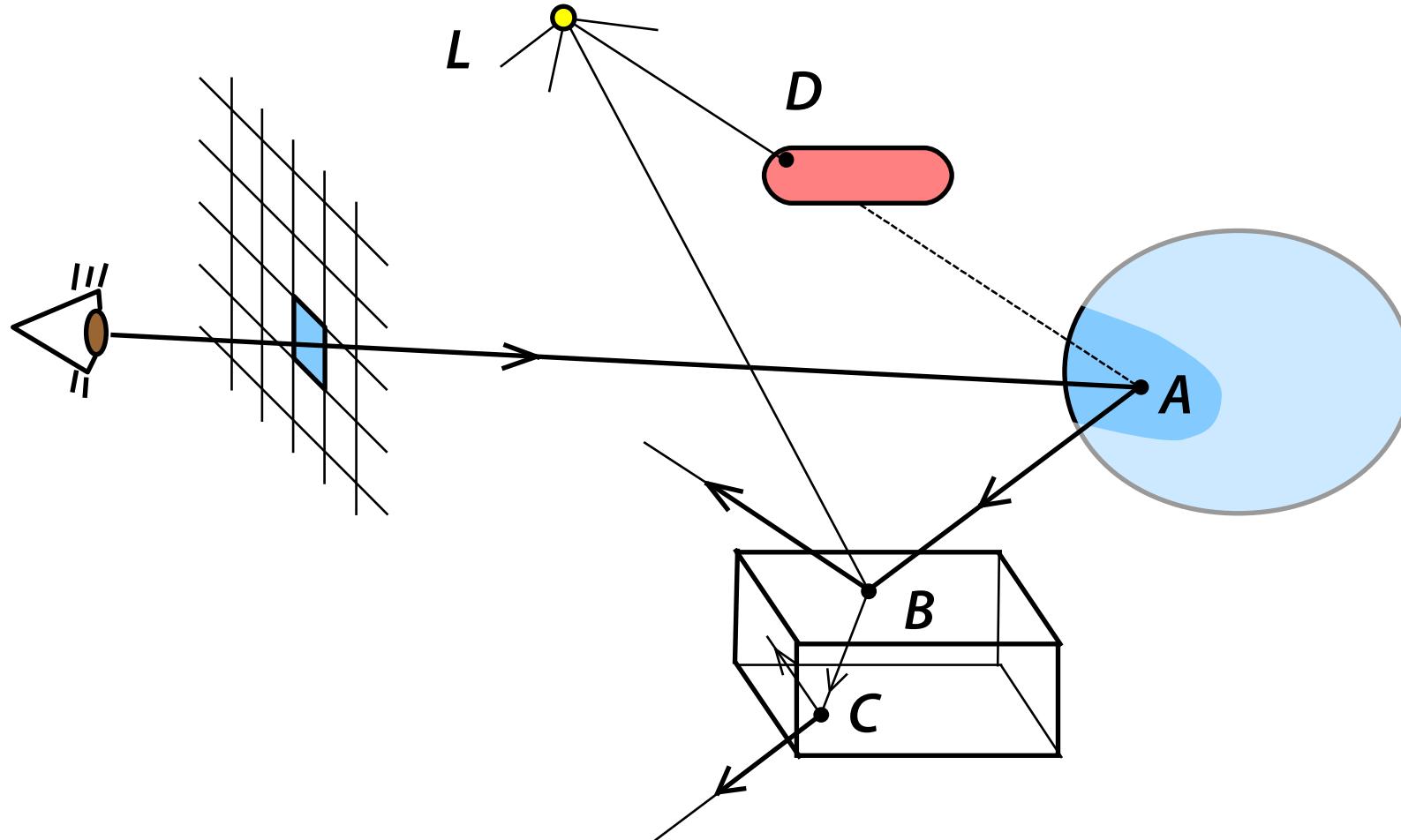


Pinhole Camera Model (Camera Obscura)



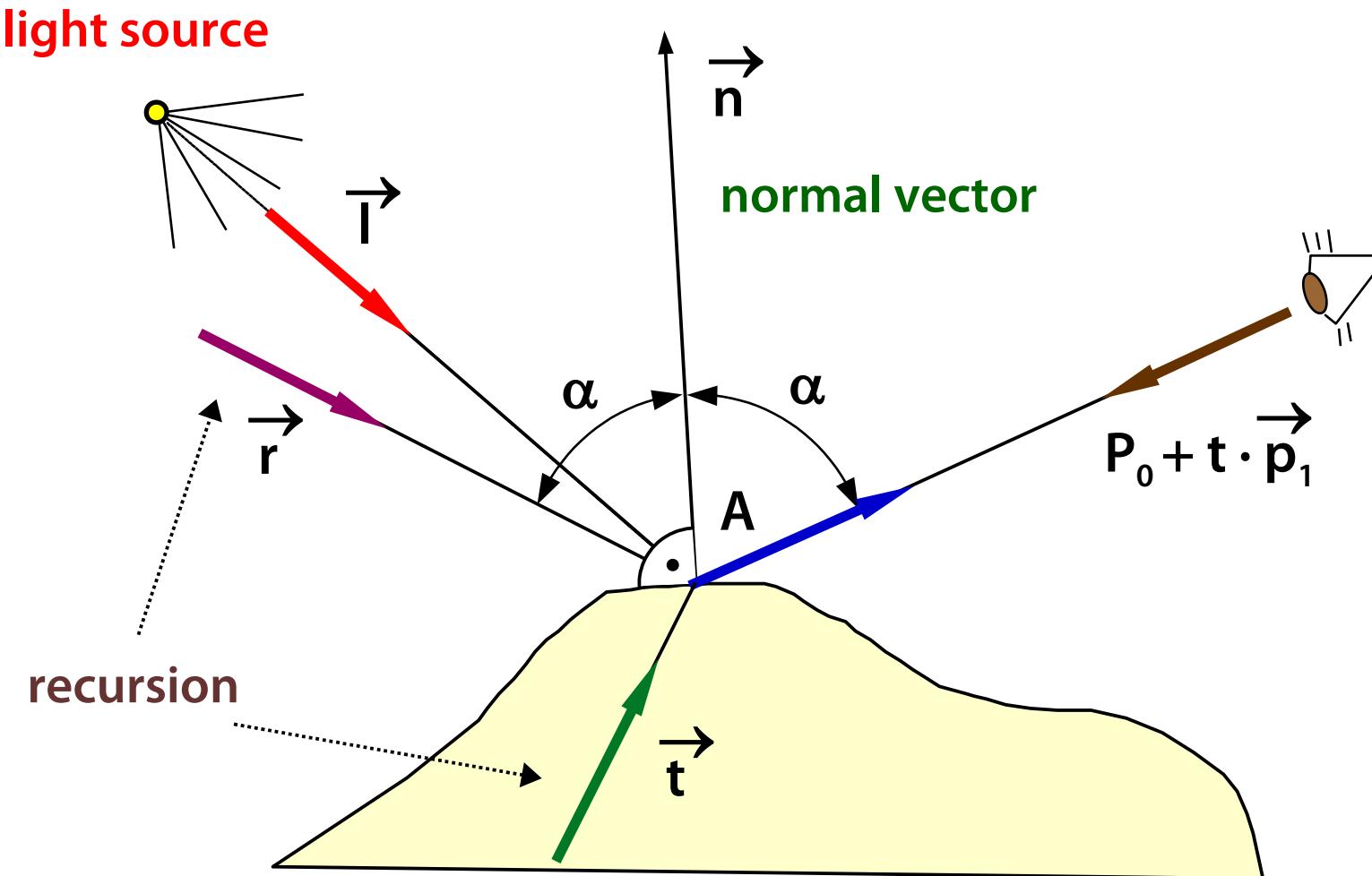


Backward Ray Tracing





Lighting Computations





Recursive implementation

```
int maxDepth = 10;                      // Maximum recursion level
RayScene scene;                          // Global scene object (geometry, materials, light sources...)
RGB shade (Vector3d P0, Vector3d p1, int depth)
// P0 - ray origin, p1 - ray direction, depth - interactions so far
{
    Vector3d A = intersection(scene, P0, p1);
    if (!isValid(A)) return scene.background; // No intersection at all

    RGB color{0};                      // Result color
    for (const auto& light : scene.lightSources)
        if (!isValid(intersection(scene, A, light.point - A)))
            color += scene.kL(A) * light.contribution(A, -p1, scene.material(A), scene.normal(A));

    if (++depth >= maxDepth) return color;

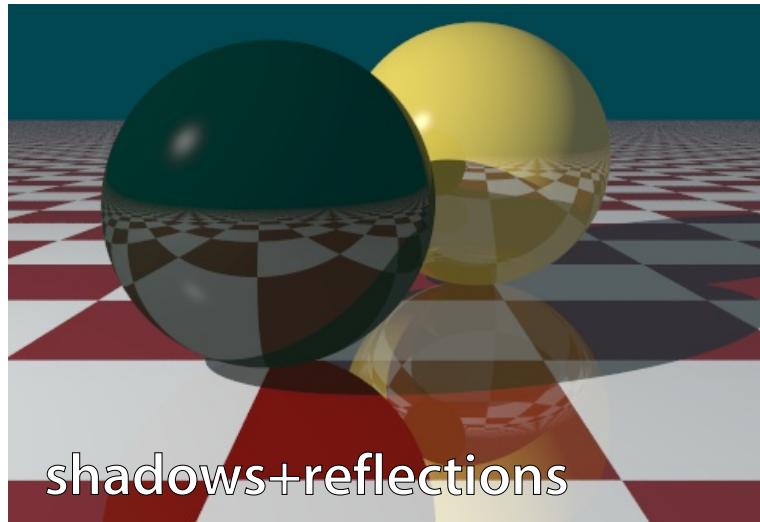
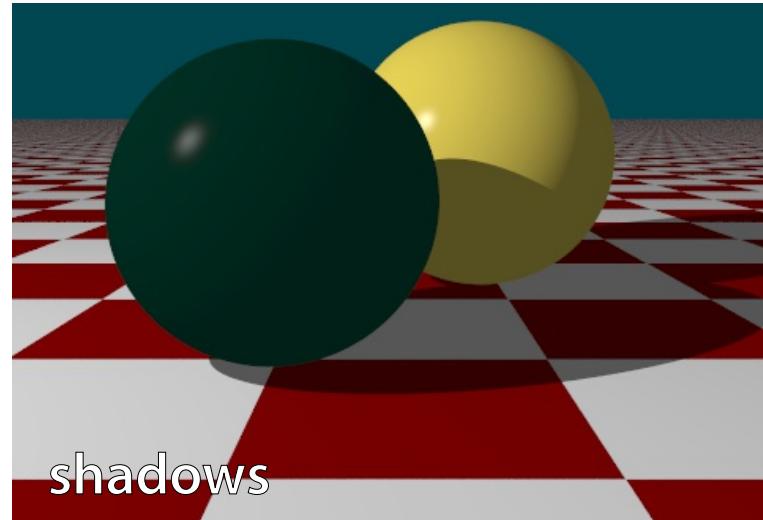
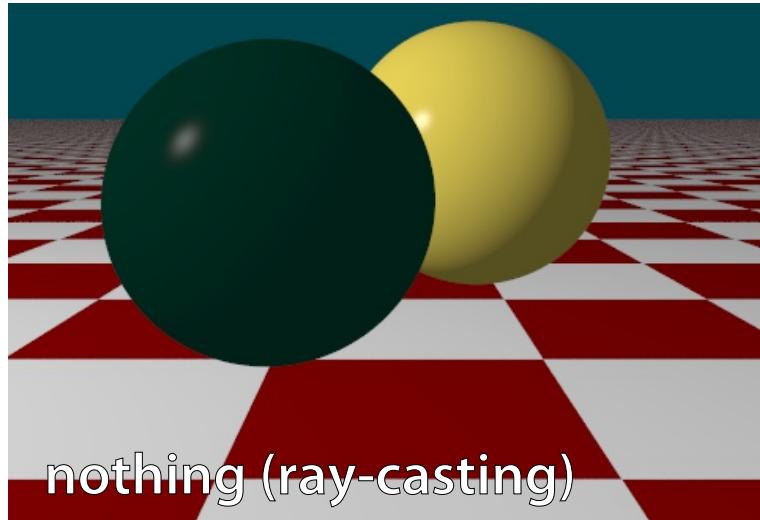
    if (scene.isGlossy(A))           // Recursion - reflection
    {
        Point3d r = reflection(p1, scene.normal(A));
        color += scene.kR(A) * shade(A, r, depth);
    }

    if (scene.isTransparent(A)) // Recursion - refraction
    {
        Point3d t = refraction(p1, scene.normal(A), scene.index(A));
        color += scene.kT(A) * shade(A, t, depth);
    }
}

return color;
}
```



Individual Components





Recursion Management

Static – limited by a constant (not suitable for scenes with many mirrors and less glossy surfaces simultaneously)

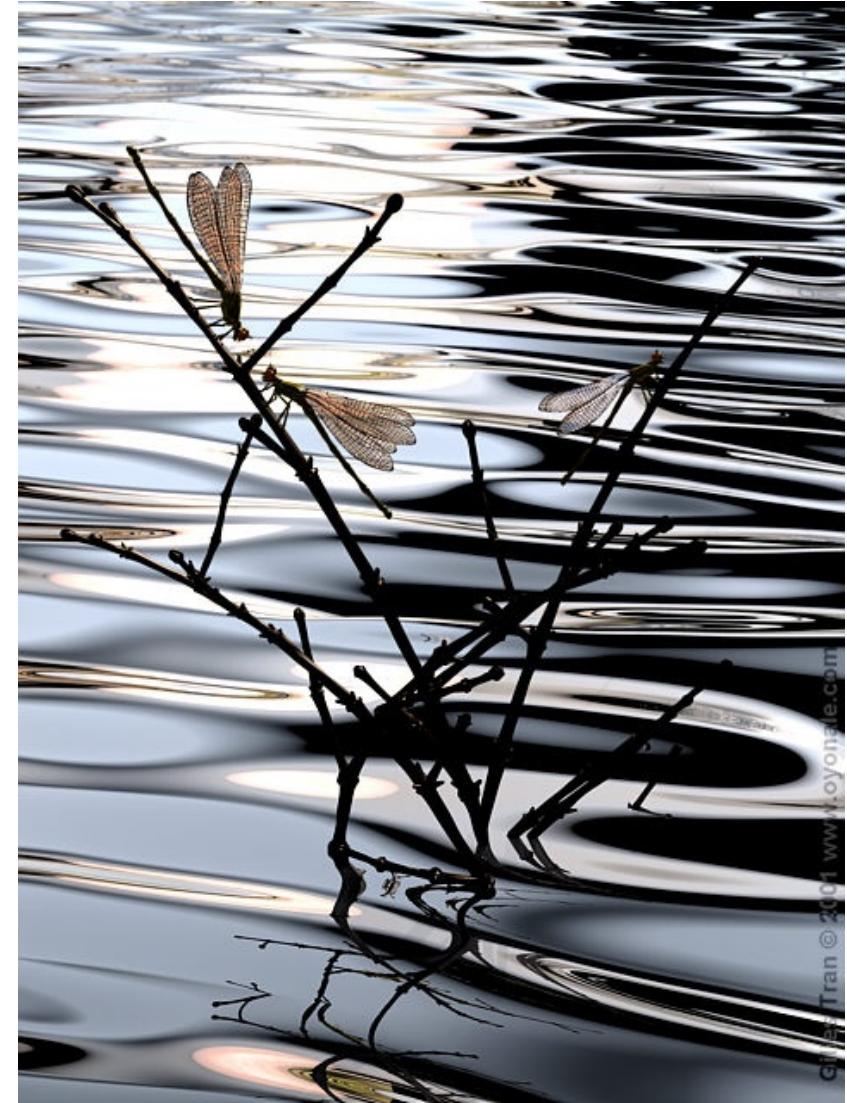
Dynamic – according to performance/importance of the ray

- “**performance**” is the percentage the ray can still contribute to the color of a given pixel (primary rays: 100%)
- limit on the “**performance**” constant (e.g. 1-2%)

Combined – limit on the recursion depth, and the “**performance**” of the ray



More Examples





More Examples





More Examples





More Examples





Intersection Computations

Geometric computation, result is composed of

- intersection coordinates (1D is enough, special value “infinity”)
- normal vector of the surface
- 2D texture coordinates
- “id” of the solid (surface) that was hit → color, material...

Time-consuming operation (90-95% of render time)

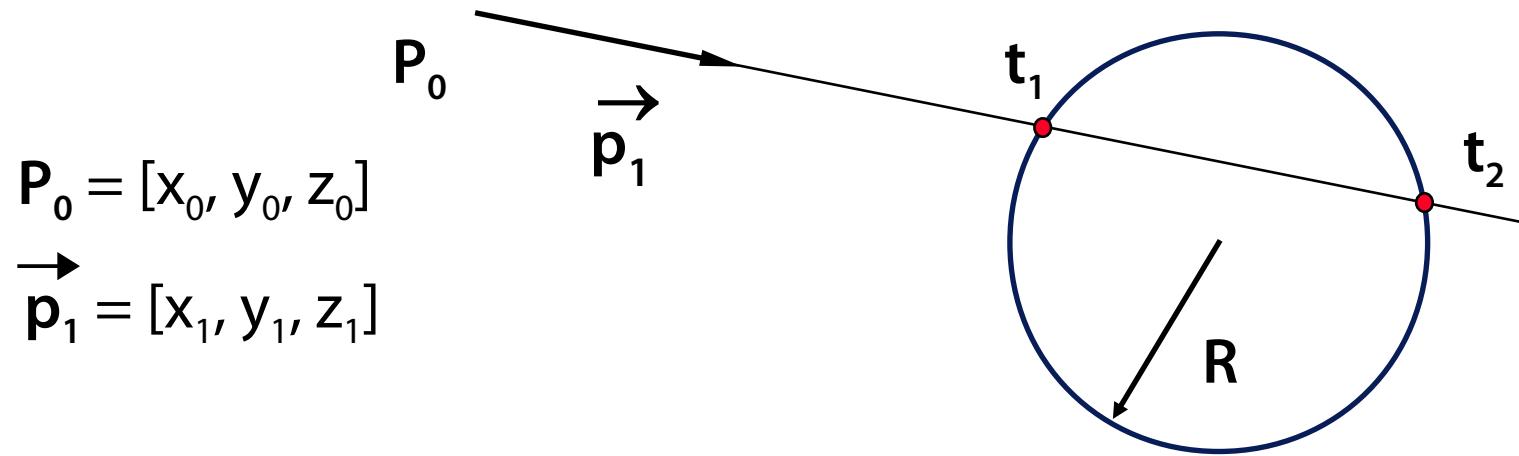
- acceleration techniques extremely important

Analytical solution (sphere, cylinder, cube, triangle...)

Numerical solution (subdivision surfaces, higher order surfaces, rotational surfaces, implicit surfaces...)



Ray-Sphere Intersections



$$P_0 = [x_0, y_0, z_0]$$

$$\vec{p}_1 = [x_1, y_1, z_1]$$

Ray:

$$P(t) = P_0 + t \vec{p}_1, \quad t > 0 \quad (1)$$

Sphere (at origin):

$$x^2 + y^2 + z^2 - R^2 = 0 \quad (2)$$

After substituting (1) into (2) we obtain a **quadratic equation (t)**

$$t^2 (x_1^2 + y_1^2 + z_1^2) + 2t (x_0 x_1 + y_0 y_1 + z_0 z_1) + x_1^2 + y_1^2 + z_1^2 - R^2 = 0$$



Ray Intersections with CSG

For **elementary solids**, intersections can be calculated

- start and end of ray traversal through a [convex] solid body

Set theoretic operations on all intersections along the ray

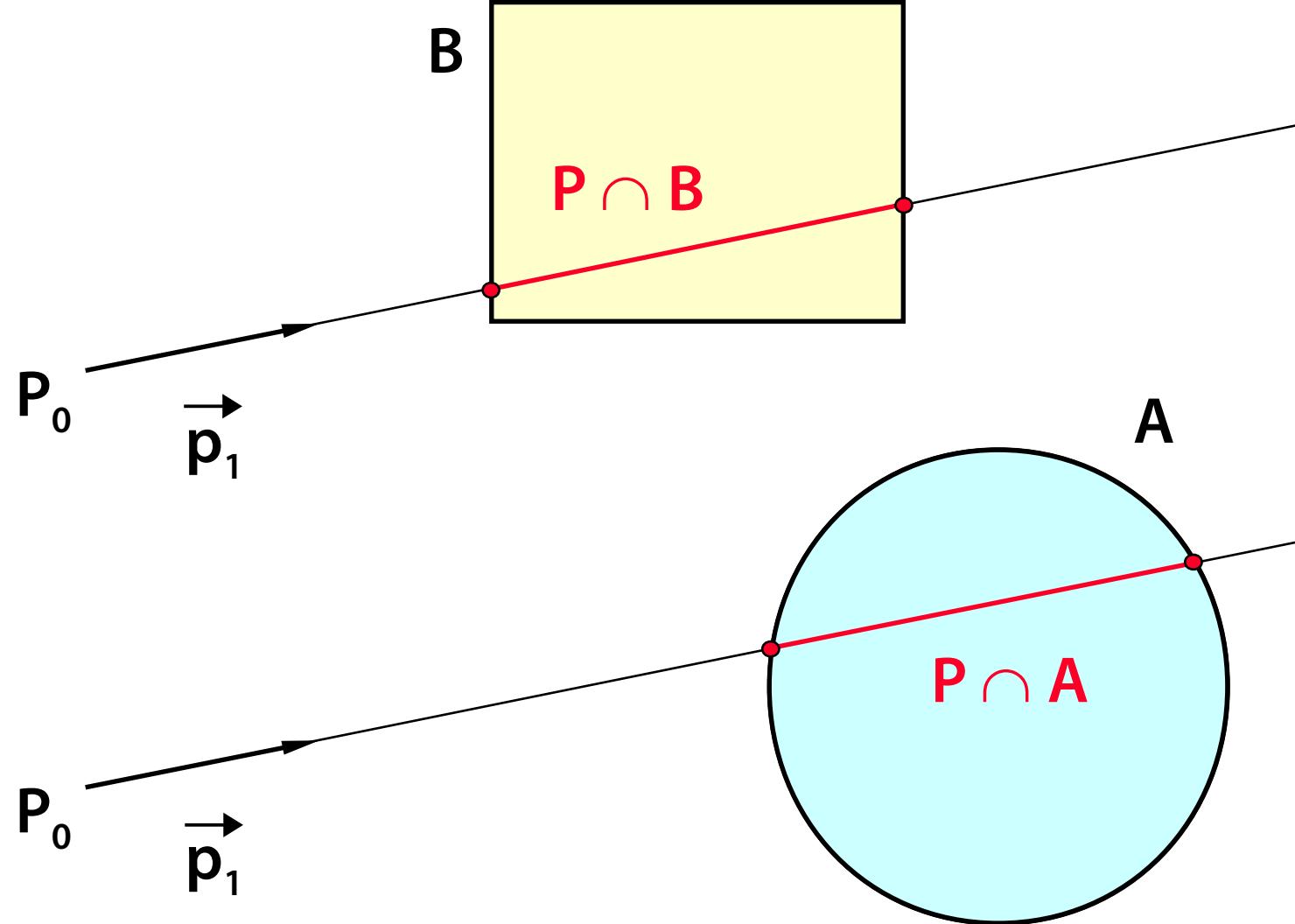
- distributive: $P \cap (A - B) = (P \cap A) - (P \cap B)$
- the usual ray-object intersection is a sequence of intervals

Geometric transformations

- the inverse transformation is applied to the ray

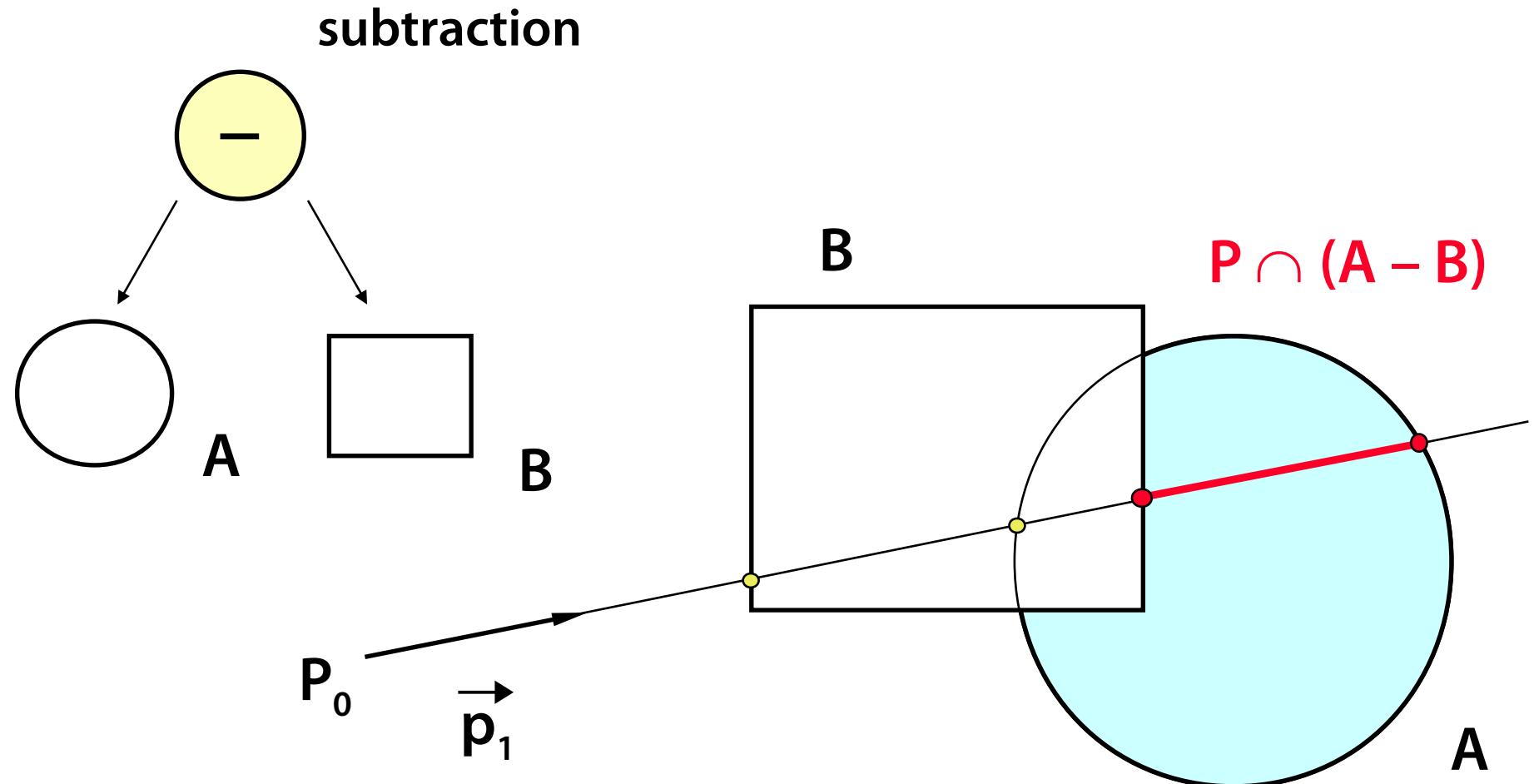


Intersections $P \cap A$, $P \cap B$





Intersection $P \cap (A - B)$





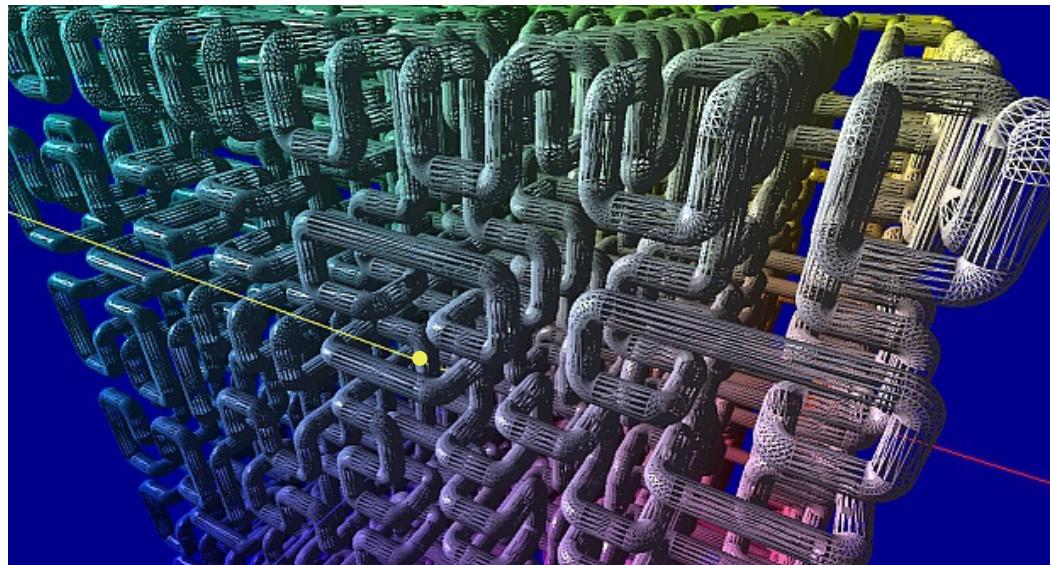
Intersections with Triangle Mesh

Scene = triangle mesh

- simple idea (simple API, even for GPU)
- any useful scene geometry can be approximated in this way

Simple test “Ray – triangle”

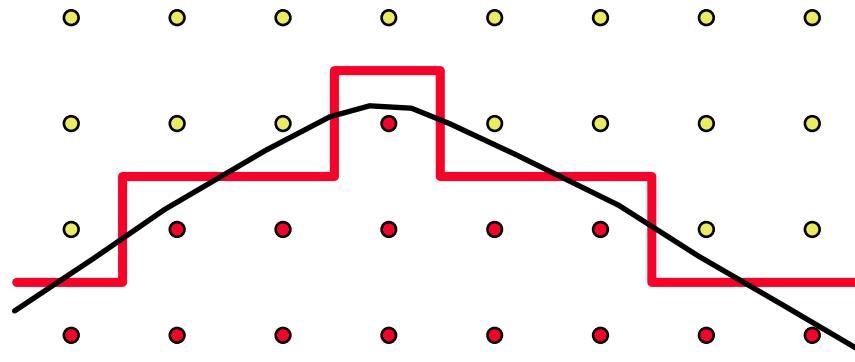
- huge amount of triangles (10^6 to 10^{10}), $O(N)$ is too slow
- acceleration methods try to get better complexity: $O(\log N)$



$N \approx 10^6$



Anti-aliasing



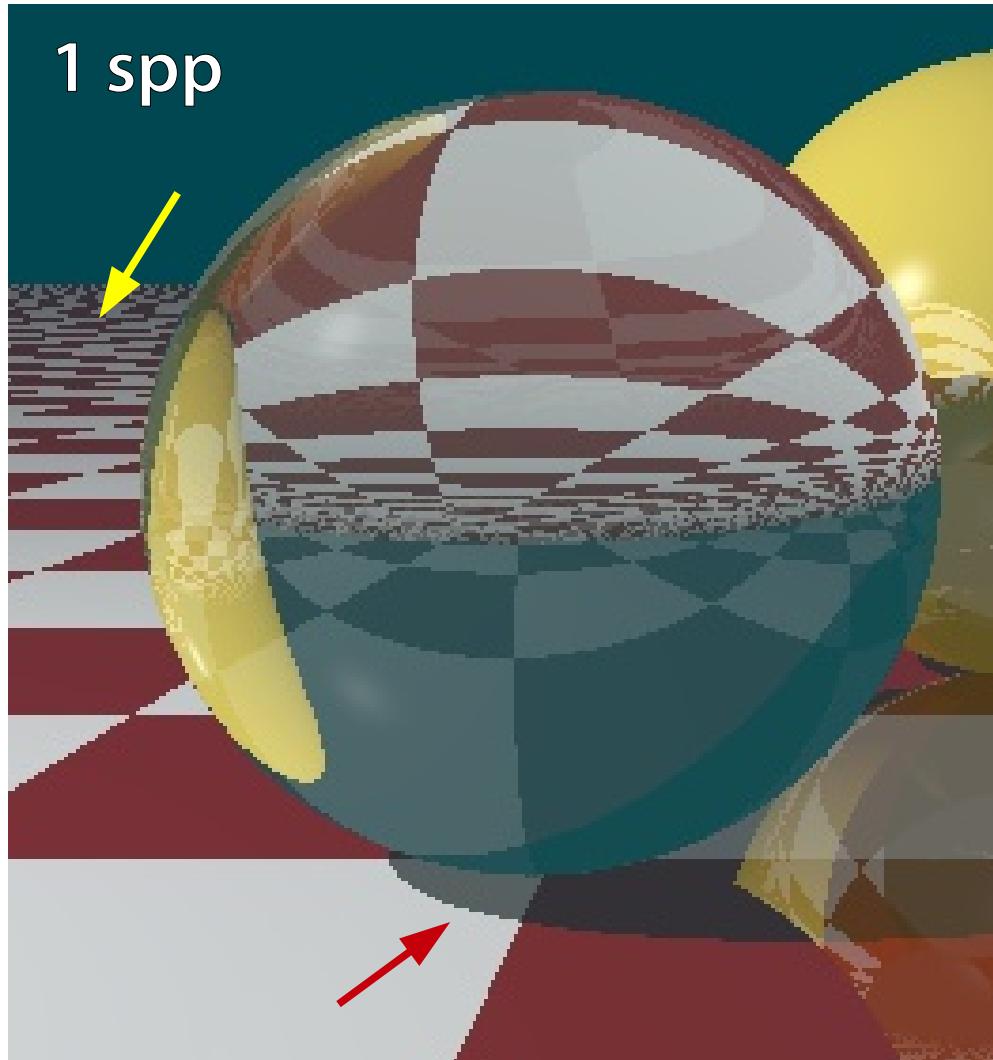
Only one ray per pixel leads to "aliasing"

- jagged edges
- interference

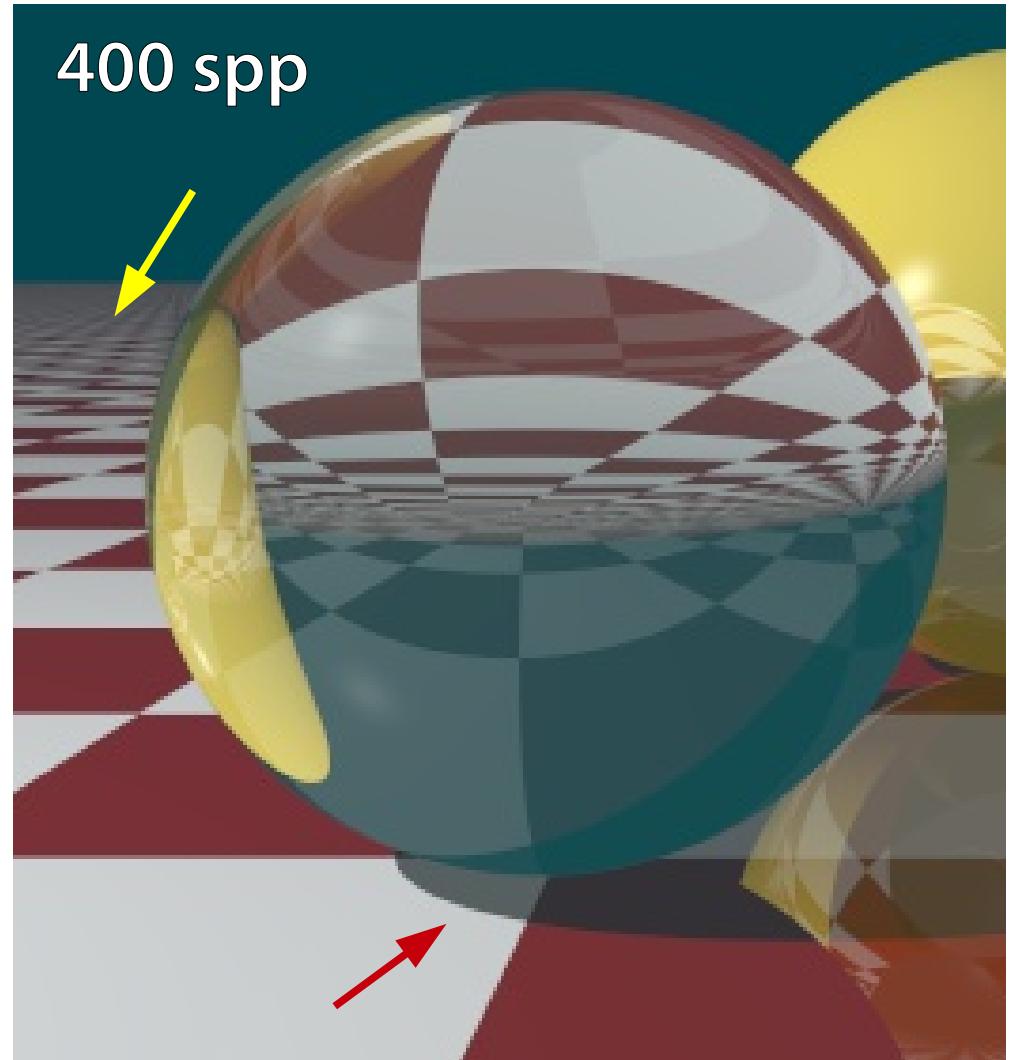
Increased resolution only partially solves the problem (and at great cost)



Anti-aliasing (Super-sampling)

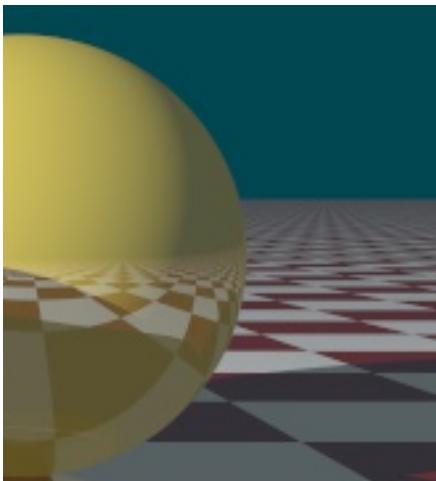
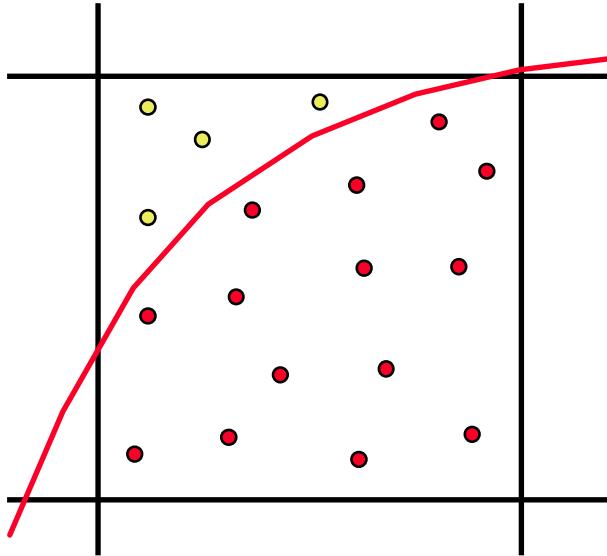


spp = samples per pixel





Multiple Sampling



Multiple rays are fired into each pixel
Resulting color is an arithmetic average
Transitions are smoother (no jaggies)
The rays should cover the pixel area evenly, but not regularly!



Textures

Changing the **color** on object surfaces

They can also affect **reflectivity** (k_D and k_S), **normal vectors** (“normal map”)...

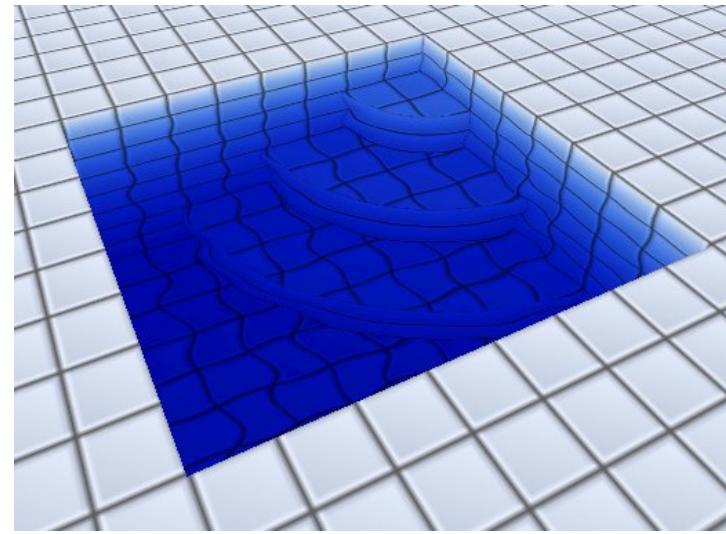
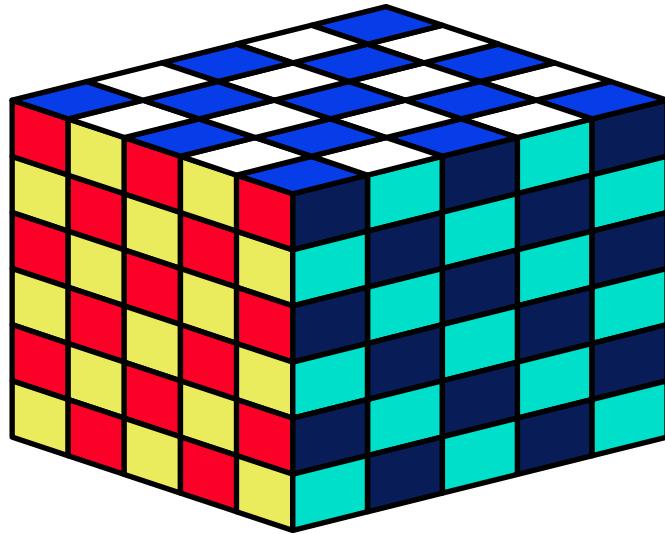
Realistic capture of **material properties** (color pattern, micro- and macro-structure)

- wood, orange/lemon peel, polished metal, plaster...

Replaces complex **geometry** (water waves...)



2D Textures



Covers the **object surface** (like wallpaper or decal)

Texture mapping: $[x, y, z] \rightarrow [u, v]$

Custom texture: $[u, v] \rightarrow \text{color}$ (normal, material...)



3D Textures

Mimics the **internal structure of materials**

- wood, marble...

Mapping is **not necessary**

3D texture: $[x, y, z] \rightarrow \text{color}$ (reflectance...)

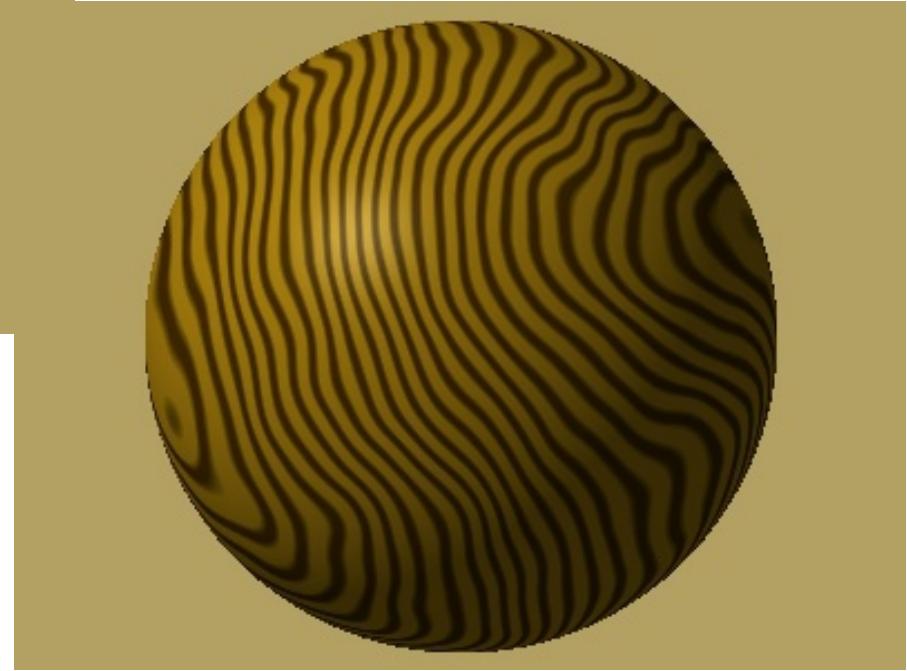
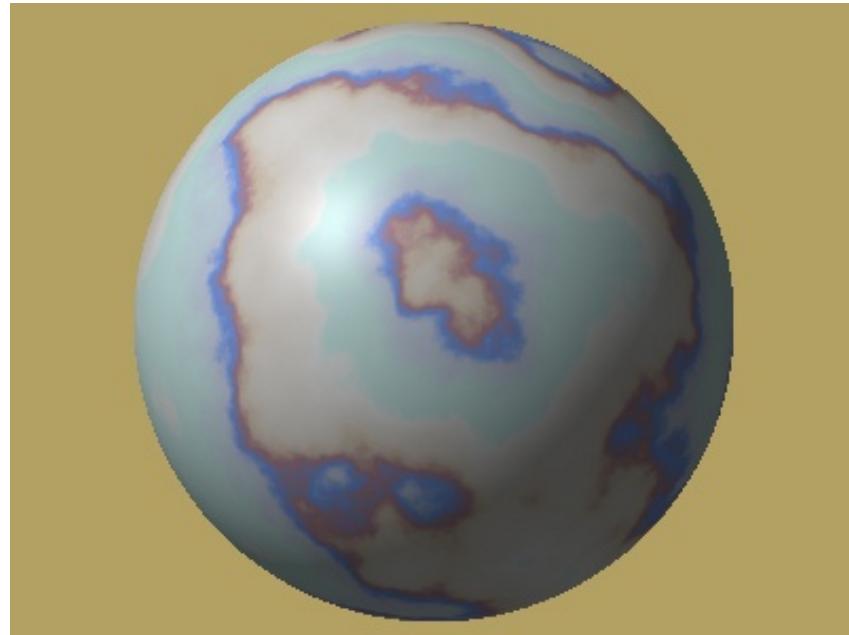
3D noise functions are often used

- simulation of natural phenomena ... turbulence, wrinkling





More 3D Texture Examples





References

A. Glassner: *An Introduction to Ray Tracing*, Academic Press, London 1989, 1-31

A. Glassner: *Principles of Digital Image Synthesis*, Morgan Kaufmann, 1995

Jiří Žára a kol.: *Počítačová grafika, principy a algoritmy*, 374-378