

Distributed Ray Tracing

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Distributed ray tracing

Better image quality (fidelity)

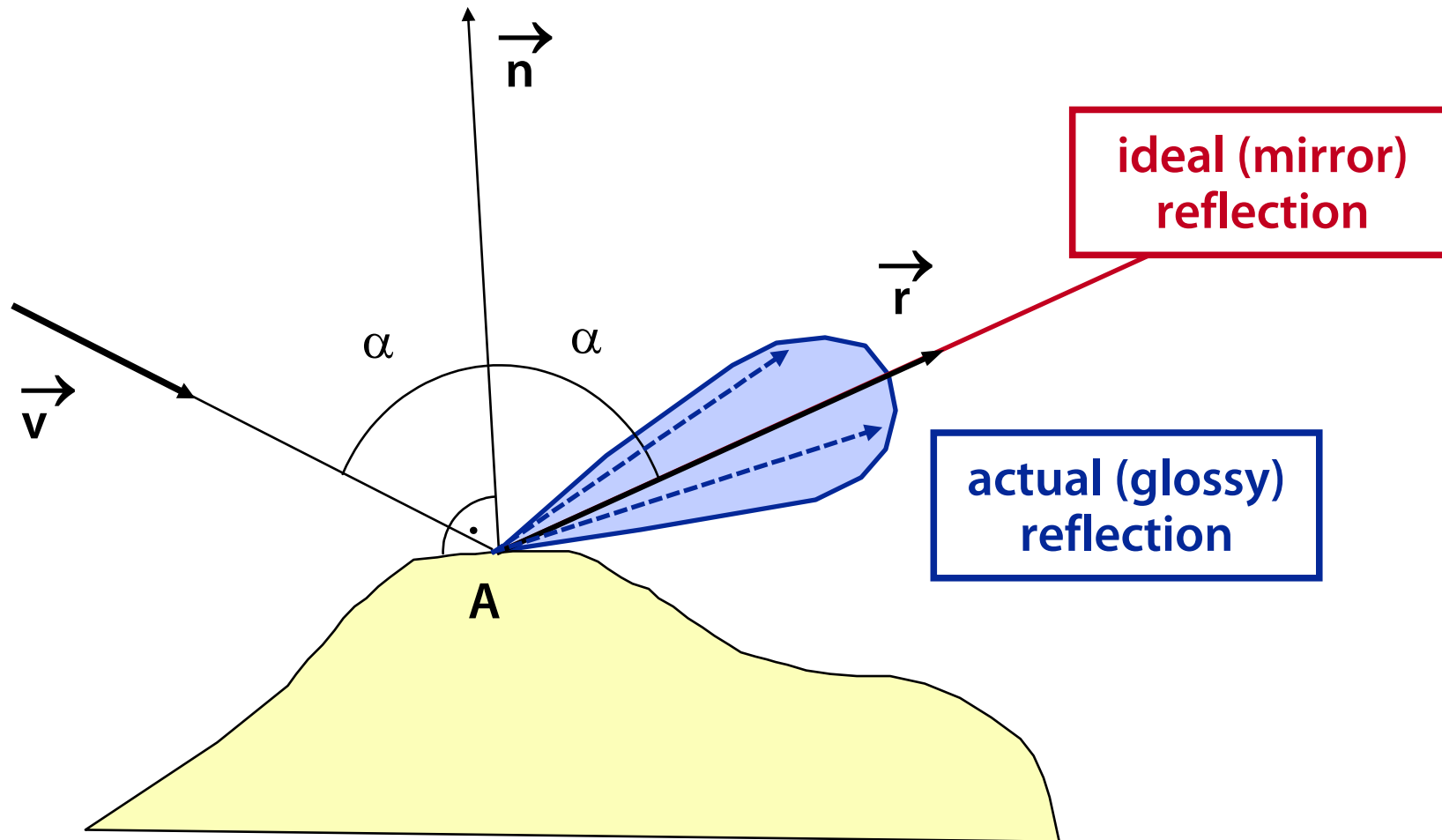
- soft shadows, glossy reflections, soft refractions
- motion blur
- depth of field imitation
- light dispersion (index of refraction depends on λ)

Introducing **new variables** to an image function

- reflection or refraction angle, wavelength, light source point, lens entry point, time...



Glossy reflection





Glossy reflection computation

Sharp reflection

$$\mathbf{I}(\mathbf{V}) = \mathbf{I}(\mathbf{R})$$

(one reflected ray)

Glossy reflection

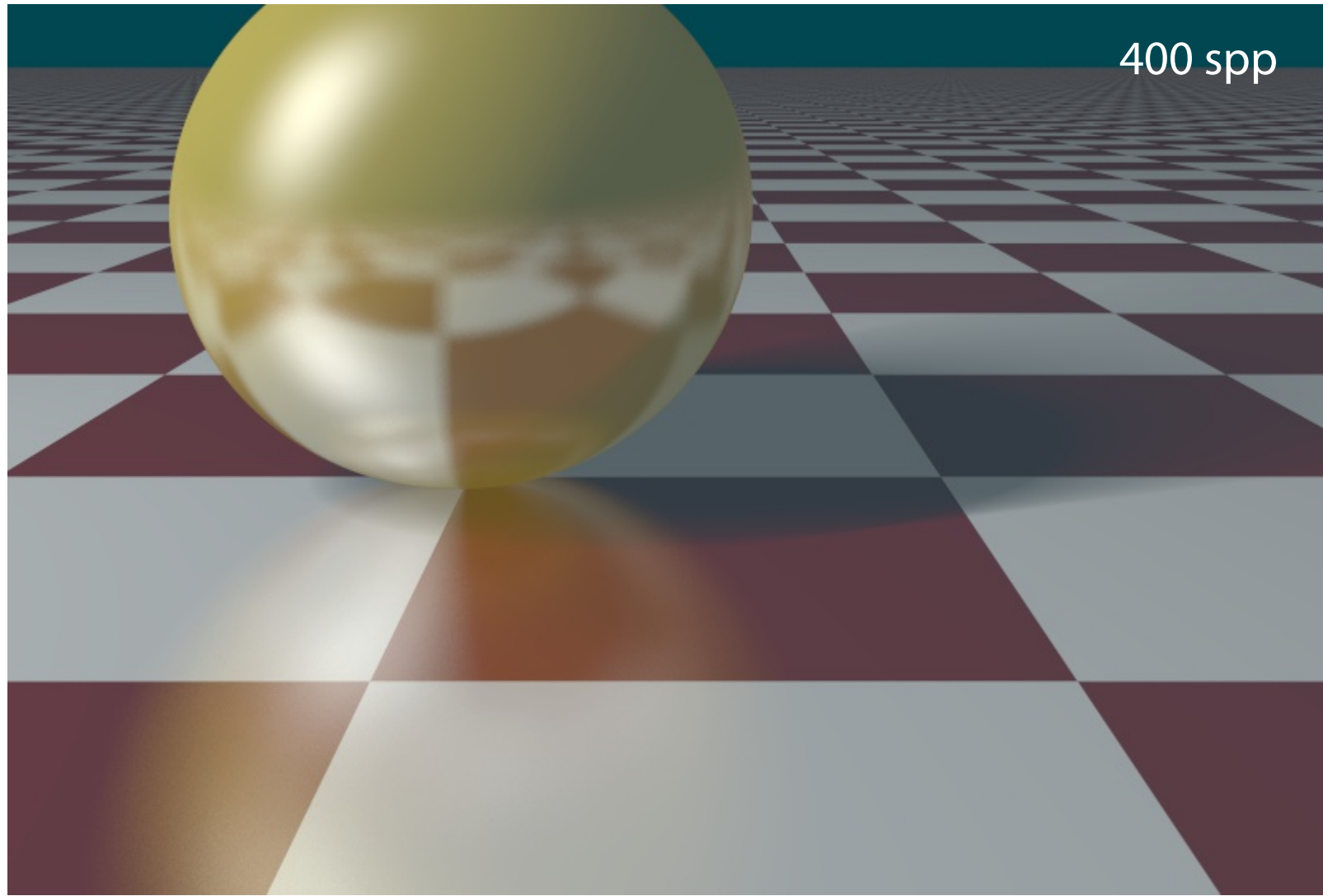
$$\mathbf{I}(\mathbf{V}) = \iint_{\text{sphere}} \mathbf{I}(\mathbf{R}(\varphi, \theta)) \cdot \text{BRDF}(\alpha, \beta, \varphi, \theta) \, d\varphi \, d\theta$$

reflectance function

(weighted integral average ... over all reflection angles)

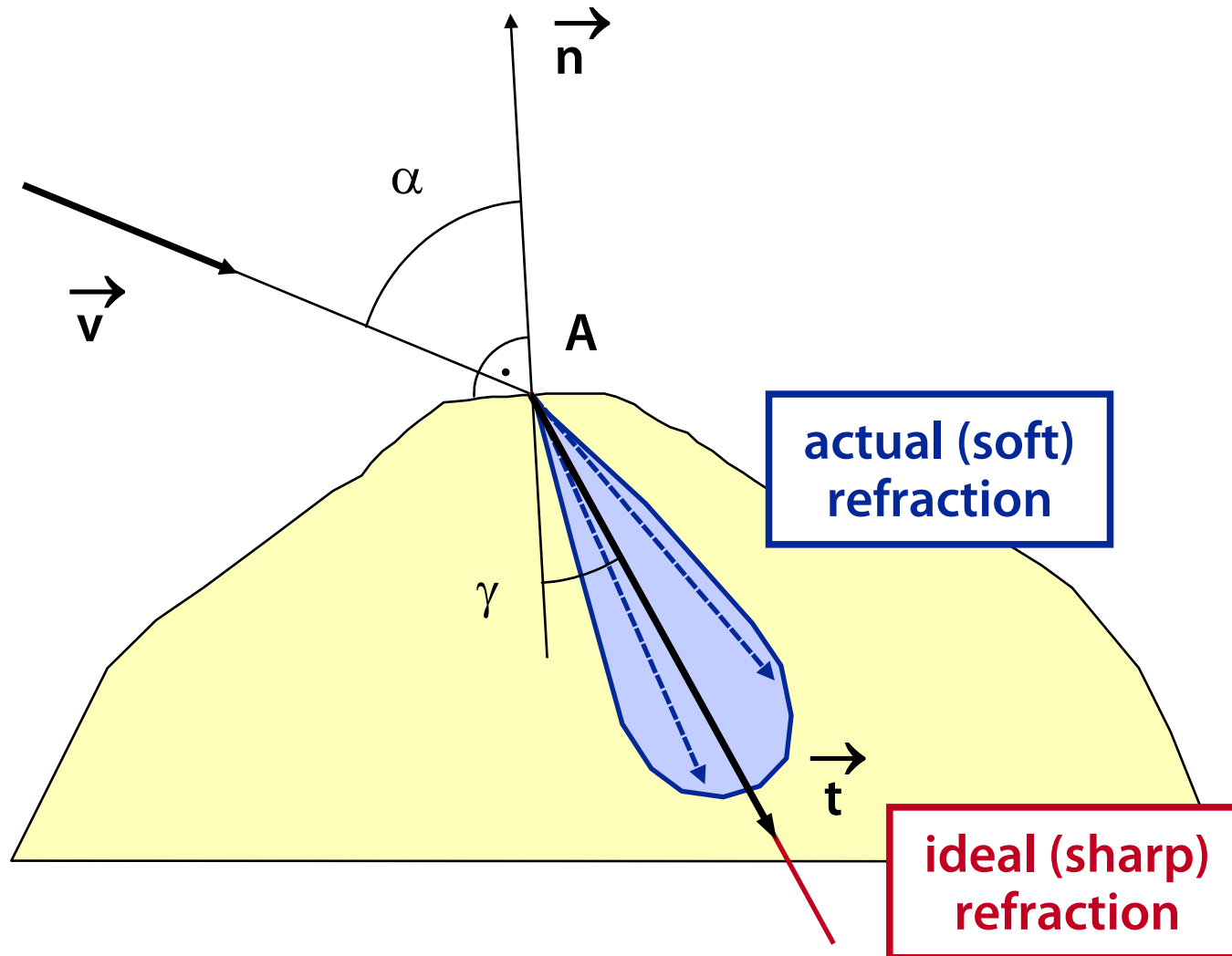


Glossy reflection – example



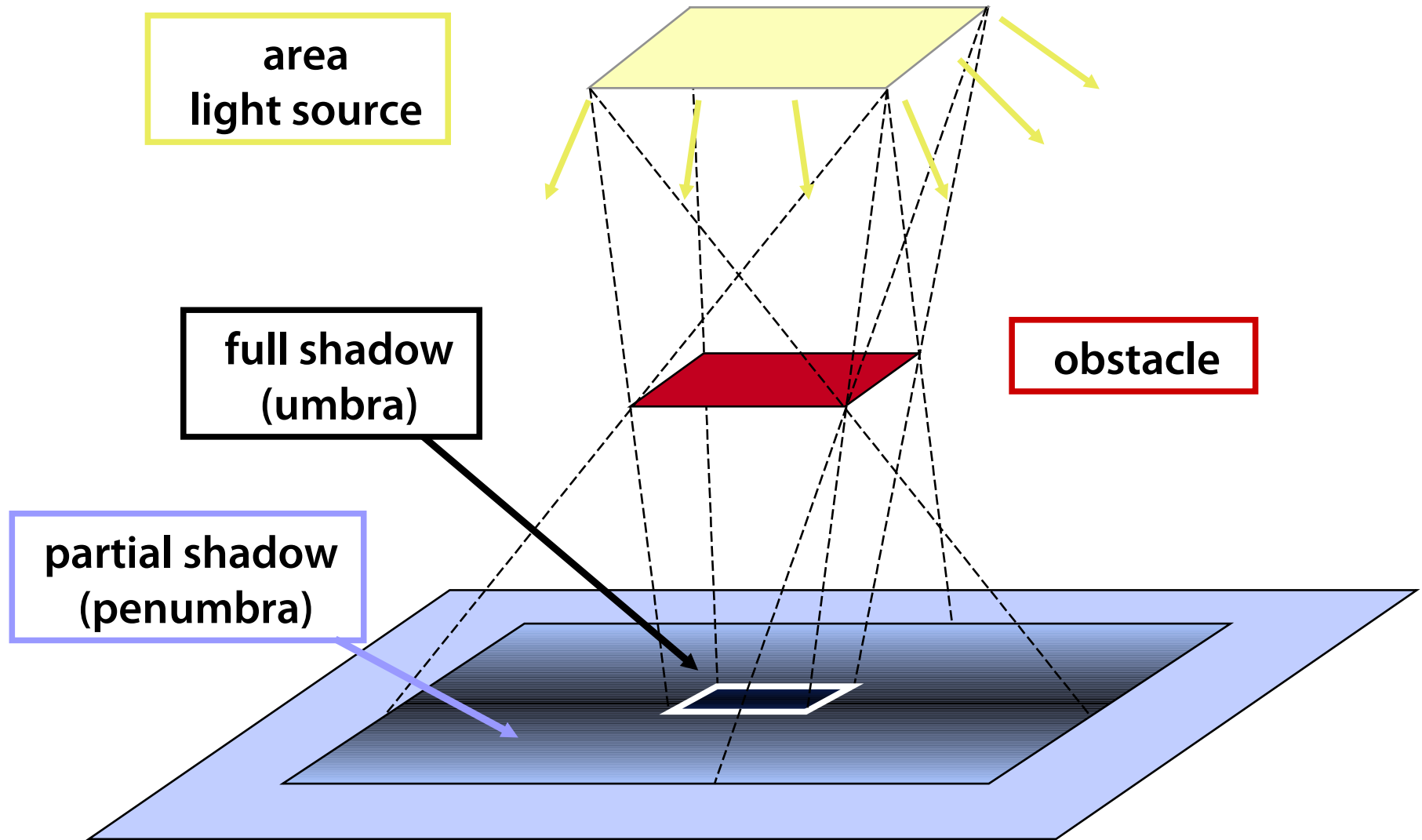


Soft refraction





Soft shadow





Soft shadow computation

Contribution of a point light source

$$I(A) = \begin{cases} I_L & \text{if source is visible from A} \\ 0 & \text{else} \end{cases}$$

Contribution of an area light source

$$I(A) = I_L \cdot S[\%]$$

visible portion of a light source



Soft shadow computation

Contribution of an inhomogenous light source

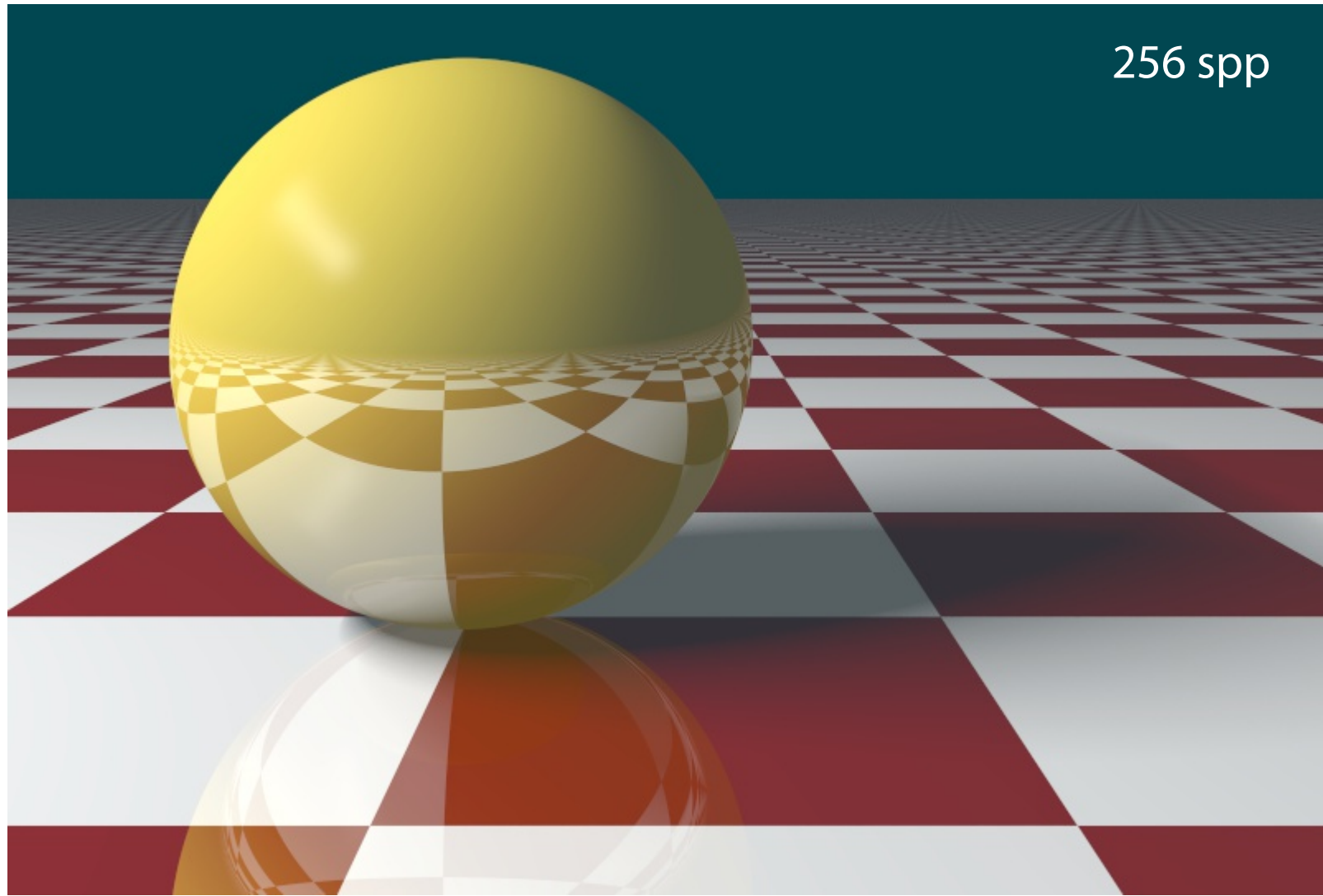
$$I(A) = \iint_{\text{light source area}} I_L(u, v) \cdot \text{vis}(A, u, v) \, du \, dv$$

visibility function

$$\text{vis}(A, u, v) = \begin{cases} 1 & \text{if } S(u, v) \text{ is visible from } A \\ 0 & \text{else} \end{cases}$$

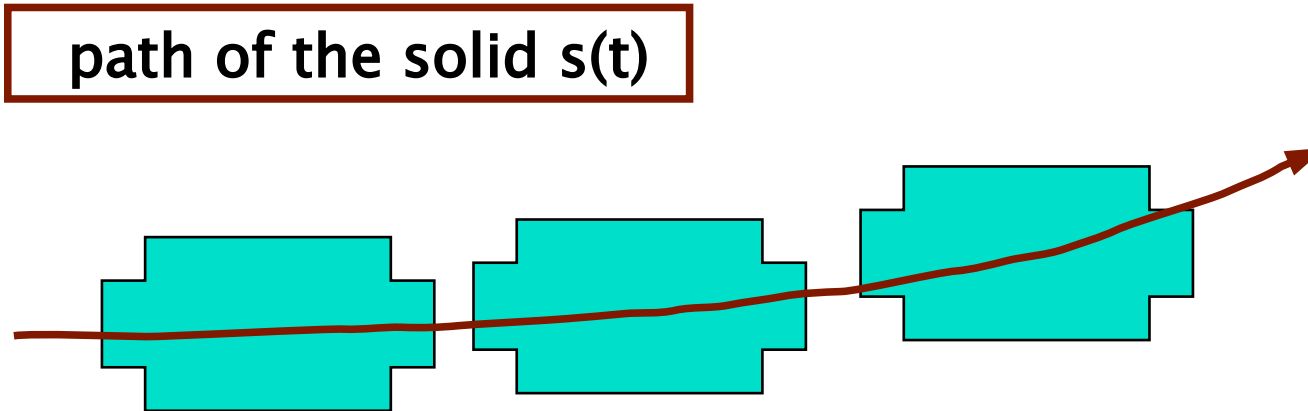


Soft shadow – example





Motion blur



Rendered interval
(shutter open time)

$[t_1, t_2]$

Scene rendering in time t

$f(t) = f(x, y, t)$



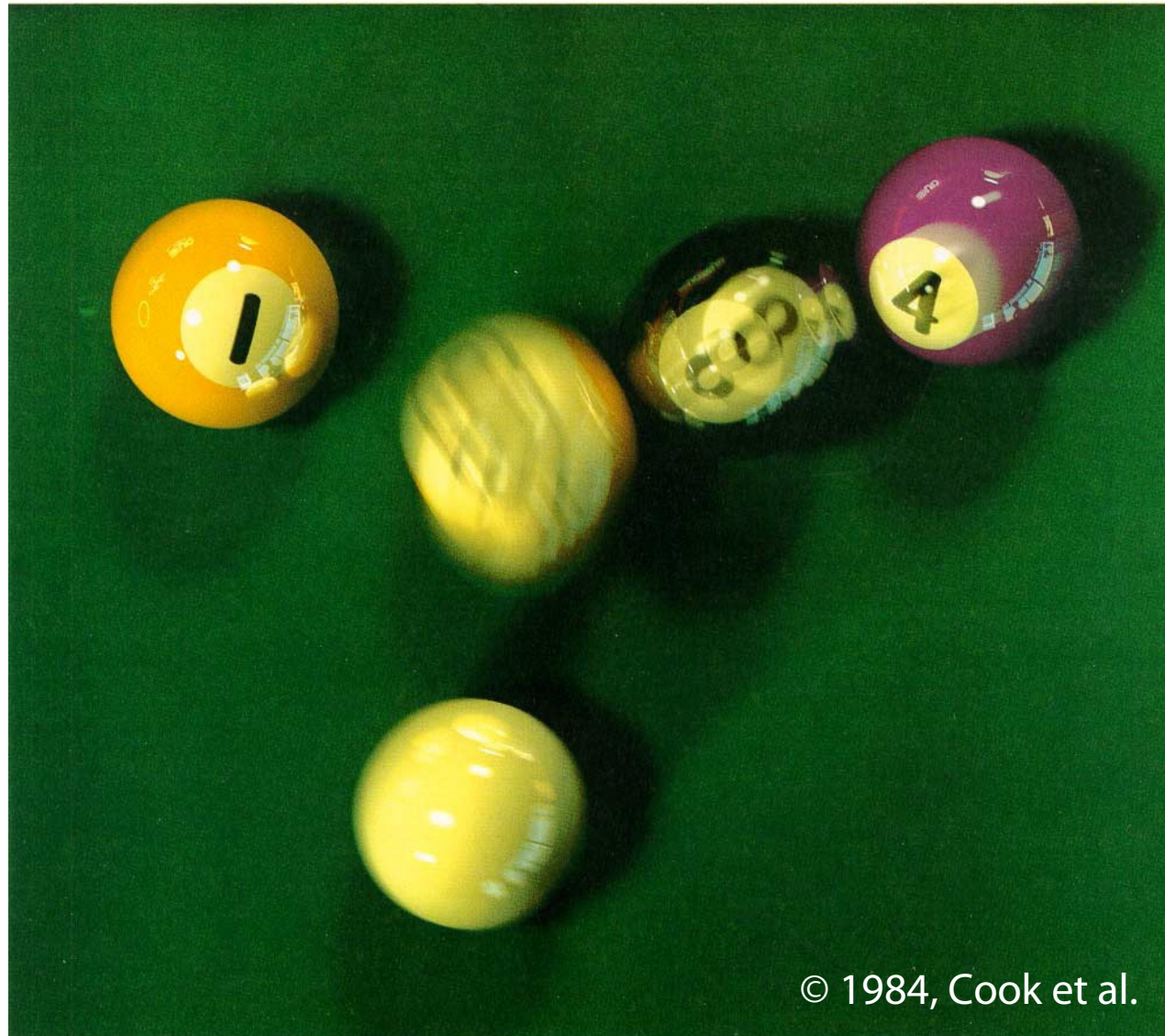
Motion blur

General motion blur

$$\mathbf{f}_{\text{blurr}} = \int_{t_1}^{t_2} \mathbf{f}(t) dt$$

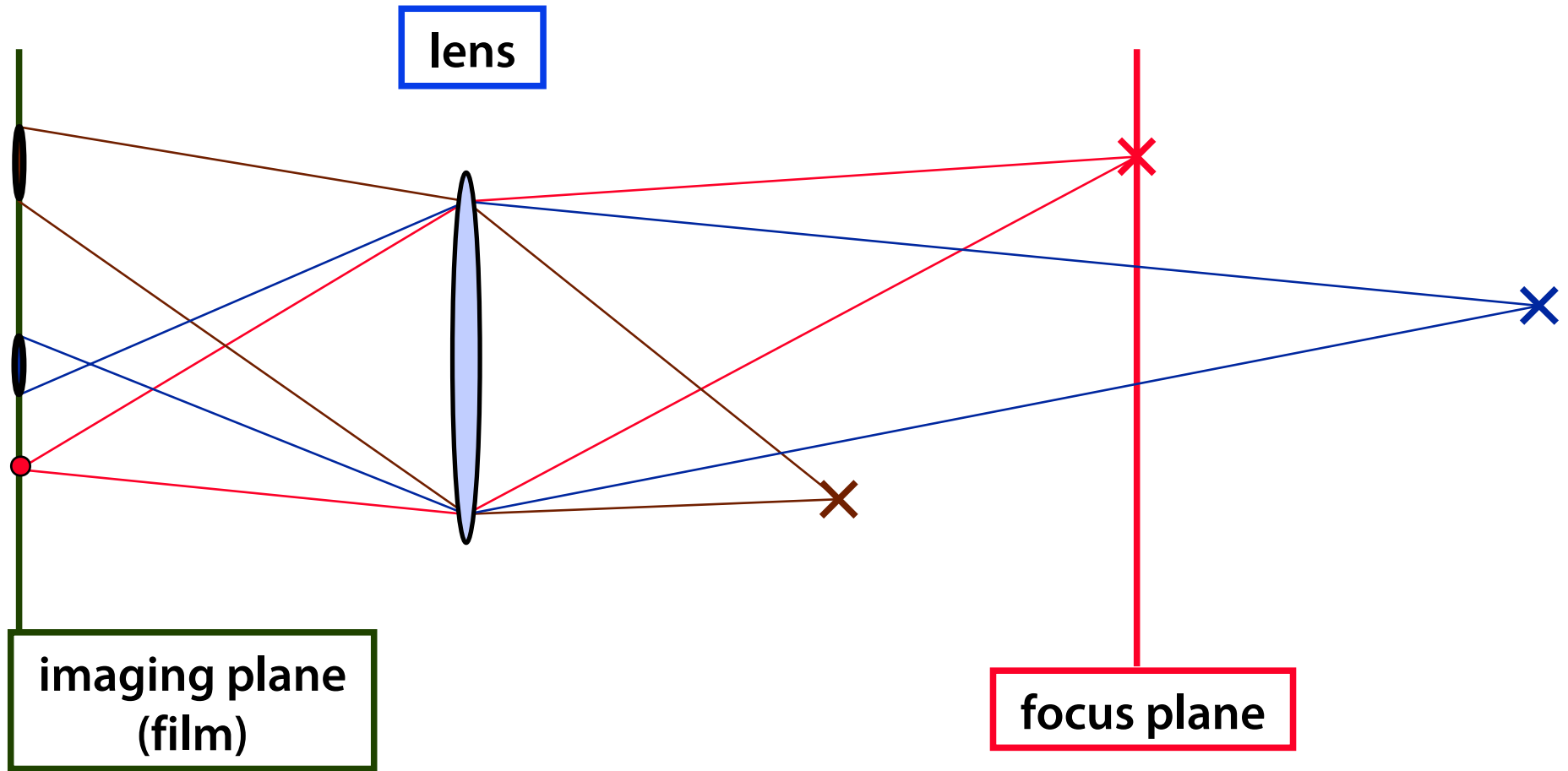


Motion blur – famous example



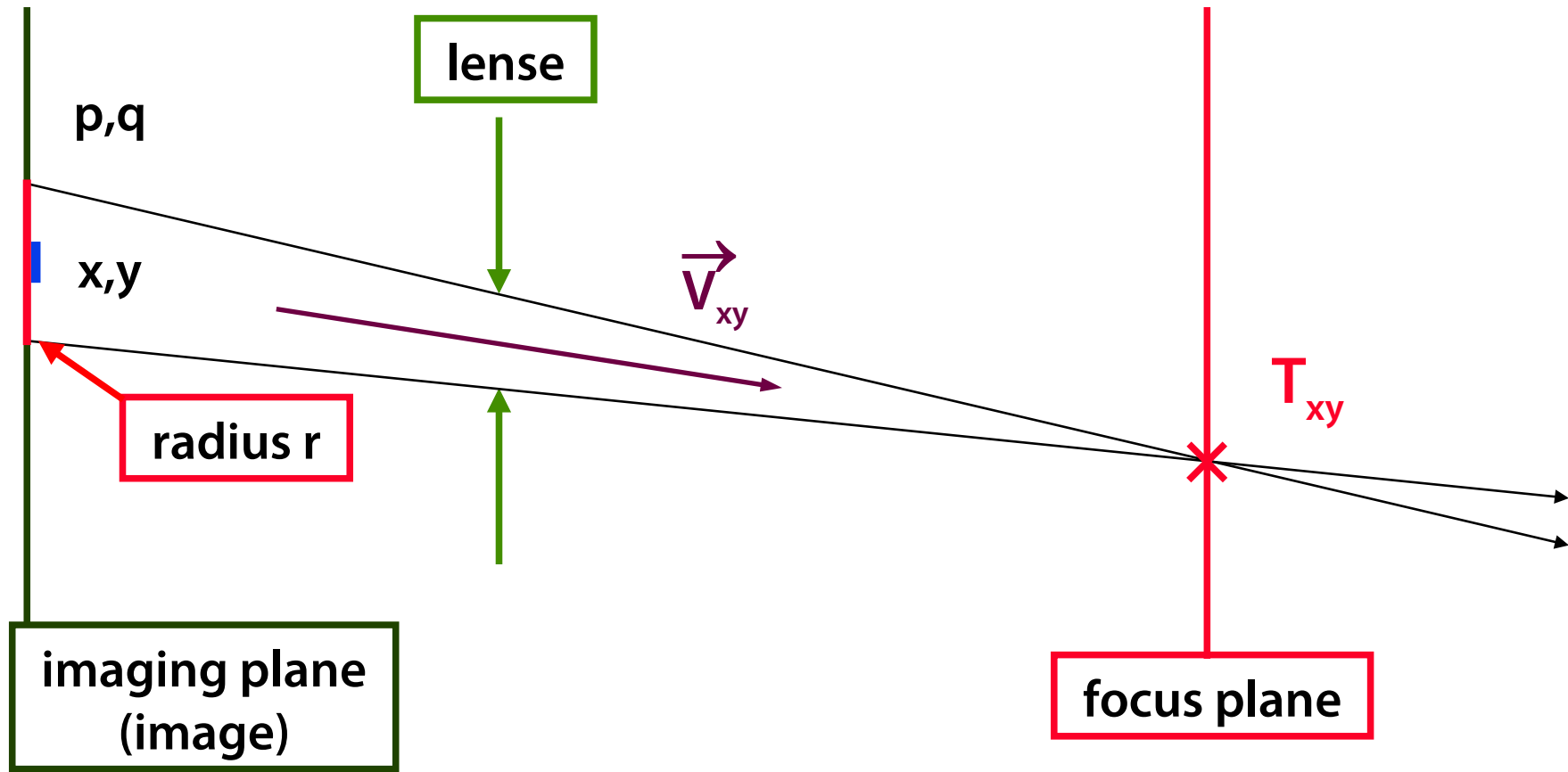


Depth of field





Geometric simplification





Depth of field computation

Pinhole camera model

$$f(\mathbf{x}, \mathbf{y}) = I(\mathbf{V}_{xy})$$

$$\mathbf{V}_{xy} = \mathbf{T}_{xy} - [\mathbf{x}, \mathbf{y}, 0]$$

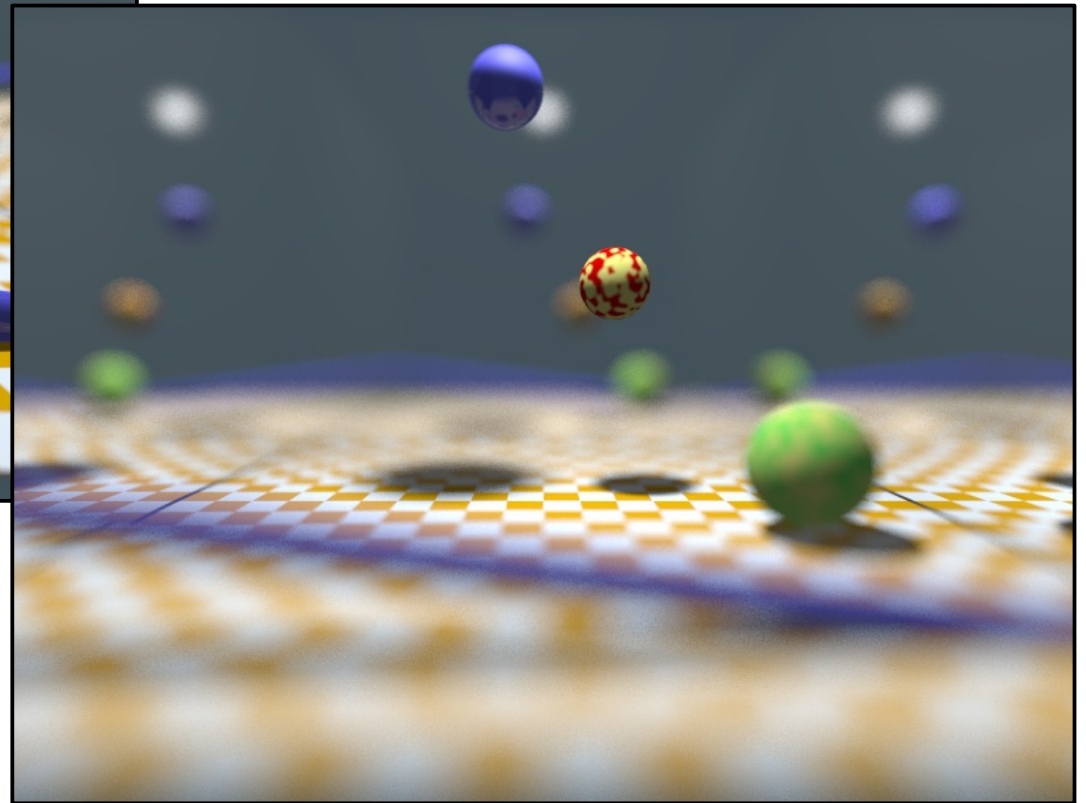
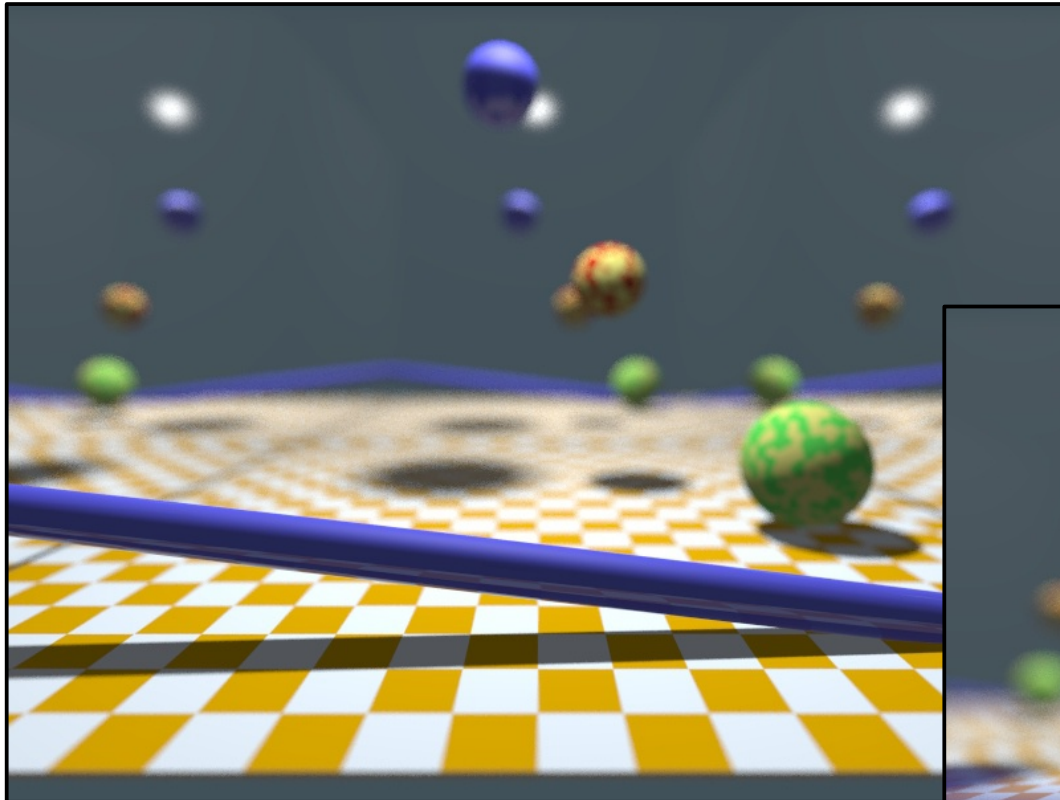
$$\mathbf{V}_{pq} = \mathbf{T}_{xy} - [\mathbf{p}, \mathbf{q}, 0]$$

Lens with finite aperture

$$f(\mathbf{x}, \mathbf{y}) = \int_{\text{circle around } [\mathbf{x}, \mathbf{y}]} I(\mathbf{V}_{pq}) dp dq$$



Depth of field – examples





Light dispersion

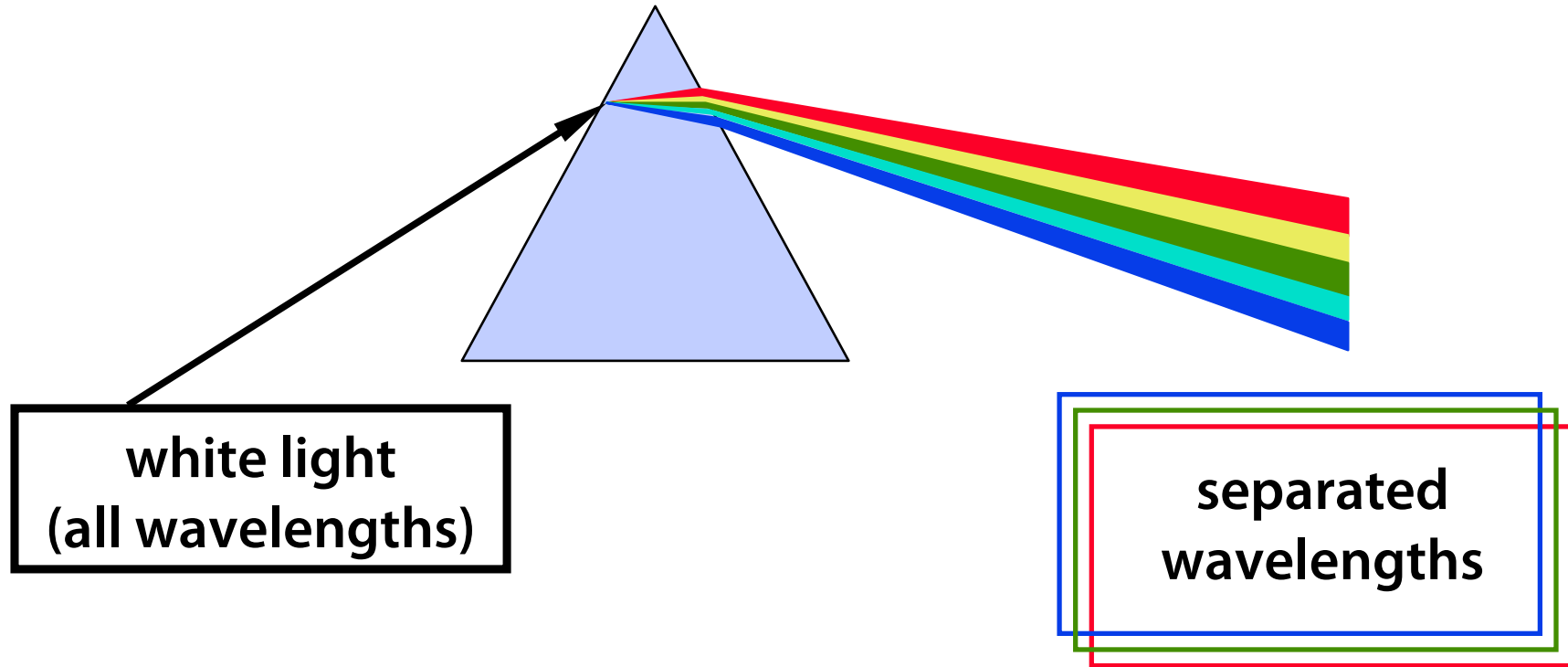


image function $f(\lambda) = f(x, y, \lambda)$



Light dispersion computation

Pixel RGB color from spectral distribution

$$\mathbf{R}(\mathbf{x}, \mathbf{y}) = \int \mathbf{f}(\mathbf{x}, \mathbf{y}, \lambda) \cdot \mathbf{R}(\lambda) d\lambda$$

spectrum

$$\mathbf{G}(\mathbf{x}, \mathbf{y}) = \int \mathbf{f}(\mathbf{x}, \mathbf{y}, \lambda) \cdot \mathbf{G}(\lambda) d\lambda$$

spectrum

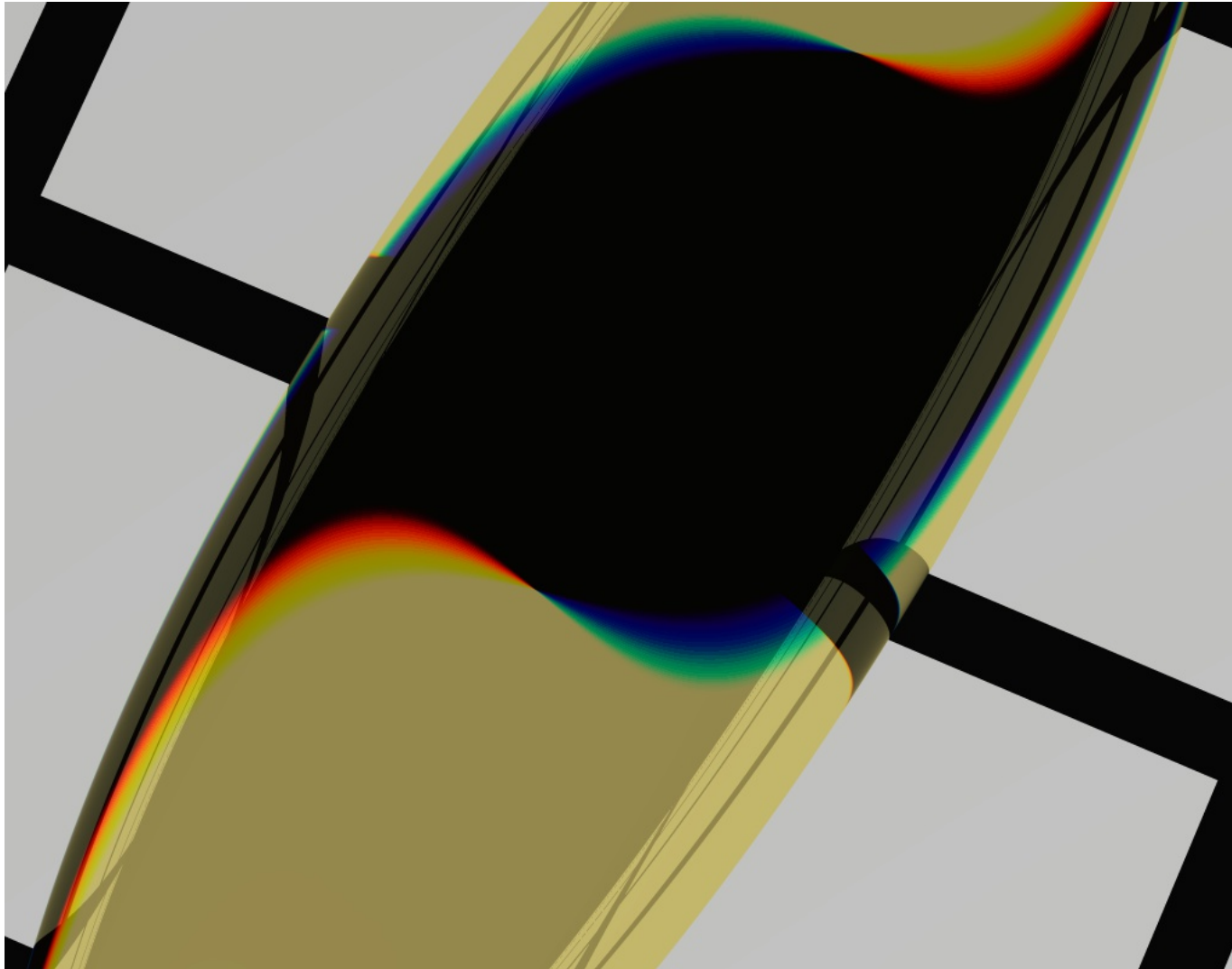
$$\mathbf{B}(\mathbf{x}, \mathbf{y}) = \int \mathbf{f}(\mathbf{x}, \mathbf{y}, \lambda) \cdot \mathbf{B}(\lambda) d\lambda$$

spectrum

trichromatic
spectral
coefficients



Light dispersion – example





Implementation

Integral averaging is done **stochastically** (Monte-Carlo methods)

- finite number of point samples (rays)
- integral is estimated by a [weighted] sum

Weighted integral average

- uniform sampling and appropriate weight function
- nonuniform sampling (using the right density/PDF)



Combining methods

Any methods can be **combined**

- with anti-aliasing as well
- higher order integrals – e.g. dimension 10:
 - anti-aliasing (2), depth of field (2), glossy reflection (2),
soft shadows (2), motion blur (1), light dispersion (1)

Sampling method

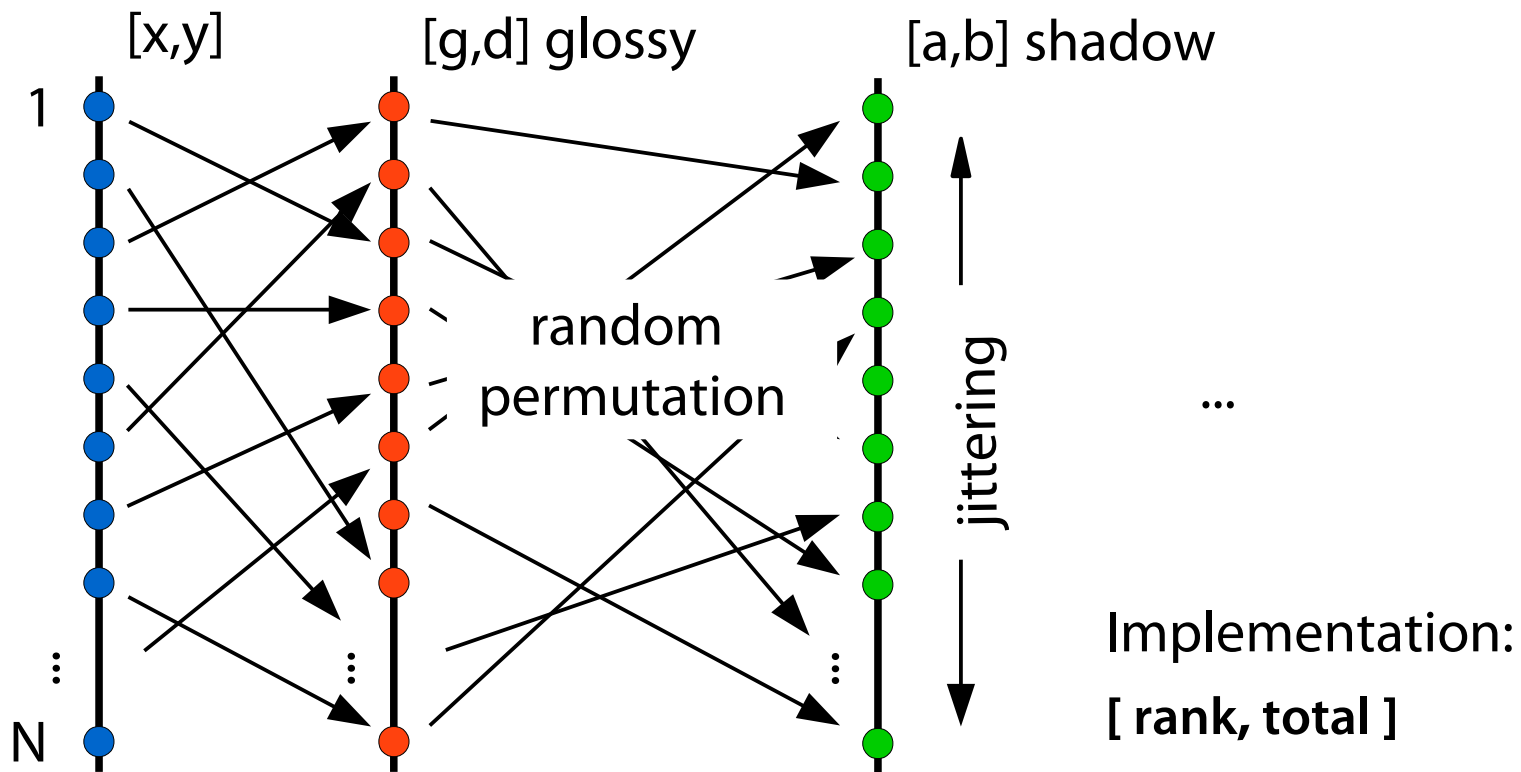
- jittering
- independent jittering (“N rooks”) in form of **hidden sampling**
- adaptive sampling



Hidden sampling

Number of **samples per pix** (primary rays) is defined

- every inner component is sampling independently
- arbitrary number of additional (sampled) dimensions





Literature

A. Glassner: *An Introduction to Ray Tracing*, Academic Press, London 1989, 171-199

A. Watt, M. Watt: *Advanced Animation and Rendering Techniques*, Addison-Wesley, Wokingham 1992, 262-265